

# Experimental and numerical investigations on the seismic behavior of bridge piers with vertical unbonded prestressing strands

Zhiguo Sun<sup>1</sup>, Dongsheng Wang<sup>2</sup>, Kaiming Bi<sup>3</sup> and Bingjun Si<sup>4</sup>

<sup>1</sup>Faculty of Infrastructure Engineering, Dalian University of Technology, Dalian, Liaoning 116024, People's Republic of China. E-mail: szg\_1999\_1999@163.com.

<sup>2</sup>Faculty of Infrastructure Engineering, Dalian University of Technology, Dalian, Liaoning 116024, People's Republic of China. (Corresponding author). E-mail: dswang@dlmu.edu.cn.

<sup>3</sup>Centre for Infrastructural Monitoring and Protection, School of Civil and Mechanical Engineering, Curtin University, Kent Street, Bentley, WA 6102, Australia. E-mail: kaiming.bi@curtin.edu.au.

<sup>4</sup>Faculty of Infrastructure Engineering, Dalian University of Technology, Dalian, Liaoning 116024, People's Republic of China. E-mail: sibingjun@sina.com.

## Abstract

In the performance-based seismic bridge design, piers are expected to undergo large inelastic deformations during severe earthquakes, which in turn can result in large residual drift and concrete crack in the bridge piers. In this paper, longitudinal unbonded prestressing strands are used to minimize residual drift and residual concrete crack width in reinforced concrete (RC) bridge piers. Seven pier specimens were designed and tested quasi-statically and the numerical simulations were carried out. The effectiveness of using vertical unbonded prestressing strands to mitigate the residual drift and concrete crack width of RC bridge piers are examined and discussed in detail. It is found that the residual drift and residual concrete crack width of the piers can be reduced significantly by using the prestressing strands. Moreover, the strands can increase the lateral strength of the piers while have little influence on the ductility capacity of the piers. The hysteretic

26 curves, residual drifts and strand stress of the piers predicted by the numerical model agree well  
27 with the testing data and can be used to assess the cyclic behavior of the piers.

28

29 **Keywords** Seismic design of bridges piers, Unbonded prestressing strands, Residual drift, Residual  
30 concrete crack width, Quasi-static test, Numerical simulation

31

## 32 **1 Introduction**

33 Bridges are key components in the transportation network, they can provide immediate emergency  
34 services following an earthquake. It is of particular importance to ensure the seismic safety of  
35 bridge structures during severe earthquakes. In the performance-based seismic design of bridge  
36 structures, bridge piers are expected to undergo large inelastic deformations during severe  
37 earthquakes, which in turn can result in large residual displacement and concrete crack width and  
38 lead to malfunction of the bridge structures. For example, following the 1995 Kobe earthquake,  
39 many reinforced concrete (RC) bridge piers with a residual drift ratio (pier residual lateral  
40 displacement divided by the pier height) larger than 1.75% were demolished in spite of the apparent  
41 light damage (Fujino et al. 2005; Kawashima et al. 1998). During the 2008 Wenchuan earthquake,  
42 the maximum residual concrete crack width in the No. 5 pier of the Miaoziping bridge reached as  
43 much as 0.8 mm. With such a wide crack, the piers under the water have to be retrofitted to protect  
44 them from corrosion attack. The cost of retrofitting was significantly high due to underwater  
45 construction of the concrete (Zhuang et al. 2009). Recently, a growing number of high speed  
46 railway bridges and cross sea bridges are designed and constructed in China. In the seismic design  
47 of high speed railway bridges, it is especially important to reduce the residual drift of the piers to  
48 ensure the safety and stability of the high speed trains. On the other hand, concrete cracking can

49 seriously threaten the long-term durability of the cross sea bridge piers, which should be adequately  
50 considered in seismic design of these piers (Guo et al. 2015; Moshref et al. 2015).

51 To minimize the residual drift in bridge piers, a new pier design concept by using longitudinal  
52 prestressing strands was proposed. For example, Zatar and Mutsuyoshi (2002) suggested using  
53 partially prestressed concrete for the bridge piers and a series of quasi-static and pseudo-dynamic  
54 tests were carried out to examine its efficiency. It was found that employing prestressing strands in  
55 RC bridge piers could result in substantial reductions of residual drift after an earthquake. Sakai and  
56 Mahin (2004a, 2004b) proposed a similar design to minimize residual drift of RC bridge piers by  
57 using longitudinal prestressing strands to replace some of common longitudinal mild bars. The  
58 seismic behavior of such prestressed piers was investigated through a series of quasi-static and  
59 dynamic analyses. Moreover, a series of earthquake simulator tests were conducted to validate the  
60 effectiveness of using prestressing strands in mitigating the residual drift of the piers (Mahin et al.  
61 2006). The Unbonded Bar Reinforced Concrete (UBRC) structure, which consists of a conventional  
62 RC structure and vertical unbonded prestressing bars, was proposed by Iemura et al. (2004). To  
63 evaluate the seismic behavior of the UBRC structures, cyclic loading and pseudo-dynamic tests for  
64 pier specimens were carried out. It was found that UBRC piers exhibit stable seismic response even  
65 under strong earthquakes and the residual drift was small. In recent years, a new design concept of  
66 segmental precast concrete bridge pier was proposed to accelerate bridge construction (Shim et al.  
67 2008; Wang et al. 2008; Yamashita and Sanders, 2009; Ou et al. 2010), in which the unbonded  
68 prestressing strands were used to hold the pier segments together and bring the piers back to their  
69 original position under lateral loads.

70 According to the previous studies, it is clear that the residual drift of bridge piers can be decreased  
71 evidently by employing longitudinal unbonded prestressing strands. It should be noted that the  
72 residual crack width of the piers will be restricted as well as a result of the restoring force provided

73 by the prestressing strands. Thus, the use of prestressing strands would bring great benefit for the  
74 seismic design of the bridge piers in view of mitigating residual drift and concrete crack width.  
75 Until recently, studies on the seismic behavior of cast in place bridge piers with longitudinal  
76 unbonded strands are limited, and most of previous studies focused on the residual drift. Very little  
77 effort has been devoted to study the residual concrete crack widths of the piers after an earthquake,  
78 which is especially important for the long-term durability of the piers. In this study, the longitudinal  
79 unbonded prestressing strands are used to minimize residual drift and residual concrete crack width  
80 in RC bridge piers. Both experimental and numerical investigations are carried out to investigate the  
81 seismic behavior of the proposed bridge piers. Seven pier specimens were designed and tested  
82 quasi-statically to evaluate the effect of the prestressing strands on mitigation the residual drift and  
83 residual concrete crack width of the piers after an earthquake. The influences of various parameters  
84 including the prestressing force ratio, the mechanical prestressing ratio and the location of the  
85 prestressing strands, on the residual drift and residual concrete crack width, were experimentally  
86 investigated. Finally, a finite element (FE) model was developed and calibrated by using the  
87 open-source finite element code OpenSees (Mazzoni et al. 2007) based on the testing data.

88

## 89 **2 Experimental program**

### 90 2.1 Test specimens

91 To experimentally evaluate the seismic behavior of the RC bridge piers with vertical unbonded  
92 strands under cyclic loading, seven 1:4 scaled pier specimens with a cantilever scheme were  
93 designed and tested. Fig. 1 and Table 1 show the design details of the pier specimens. All the  
94 specimens had a circular section with a diameter of 300 mm and with a heavy RC footing. As  
95 shown in Fig. 1(a), the height of the specimens measured from the top surface of the footing to the

96 point where lateral loading was applied was 1100 mm, corresponding to an aspect ratio of 3.67,  
97 which normally leads to flexural failure of the specimens (Hashimoto et al. 2005; Sun et al. 2012).  
98 Fig. 1(b) summarizes the reinforcement layout. As shown in Fig. 1(b)-1, specimen RC-1  
99 represented a conventional RC bridge pier without prestressing strands. This specimen was used as  
100 a reference for comparison with results obtained from specimens with prestressing strands. This  
101 specimen was reinforced with eight 12 mm-diameter longitudinal mild bars evenly distributed  
102 around the perimeter. Mild bars of 8 mm in diameter were used as transverse reinforcement and  
103 spaced at a distance of 75 mm along the pier height, resulting in a transverse reinforcement ratio of  
104 1%.

105 Specimen PRC-1 was a standard specimen with prestressing strands. This specimen was designed  
106 to be the same as specimen RC-1 except that prestressing strands were included. Four 12.7  
107 mm-diameter unbonded strands (each strand with a nominal area of 98.7 mm<sup>2</sup>) were used with a  
108 total prestressing force ratio of 0.1 (the definition of prestressing force ratio  $\zeta$  can be found in  
109 Equation (3)). The strands were arranged in a square pattern with a side length of 135 mm. Fig.  
110 1(b)-2 shows the reinforcement layout of specimen PRC-1. Specimen PRC-2 was designed the  
111 same as specimen PRC-1 except for the longitudinal mild bars, where as shown in Fig. 1(b)-3, eight  
112 8 mm-diameter longitudinal mild bars were used in this specimen to evaluate the longitudinal mild  
113 bars on the seismic behavior of the piers with prestressing strands. Specimen PRC-3 (Fig. 1(b)-4)  
114 was design to evaluate the amount of prestressing strands on the behavior of the piers. Only two  
115 strands were used in this specimen, and other parameters were the same as specimen PRC-1.

116 Specimen PRC-4 and Specimen PRC-5 were designed to evaluate the initial prestressing stress on  
117 the behavior of the piers. In specimen PRC-4, the prestressing force ratio was reduced to 0.05, while  
118 in specimen PRC-5, it reached 0.15. For the reinforcement layouts of specimens PRC-4 and PRC-5,  
119 they were exactly the same as specimen PRC-1. Specimen PRC-6 was designed with four  
120 prestressing strands concentrated at the center of the section to evaluate the arrangement of the

121 strands on the behavior of the piers, as shown in Fig. 1(b)-5. Thus totally three different types of  
 122 prestressing strand layout are considered in the test and they are summarized in Fig. 1(c). It should  
 123 be noted that, the prestressing strands were arranged inside the mild longitudinal bars, and the  
 124 concrete cover depth of the prestressing strands was much larger than the mild longitudinal bars. As  
 125 a result, the strands would be safe enough against corrosion damage compared with mild  
 126 longitudinal bars.

127 Before the tests, all the important parameters related to the specimens were tested and measured.  
 128 For example, the average concrete compression strength was measured as 55.9 MPa by using  
 129 150×150×150 mm cubic specimens. The yielding strengths of the 8 mm-diameter and 12  
 130 mm-diameter mild bars were 517 and 453 MPa, respectively. And the ultimate strengths of the 8  
 131 mm-diameter and 12 mm-diameter mild bars were 611 and 634 MPa, respectively. The ultimate  
 132 strength of the 12.7 mm-diameter prestressing strand was 1939 MPa. All these parameters were  
 133 adopted in the numerical simulations in Section 4.

134 To facilitate further explanation, the following parameters are defined in the present study. They are:  
 135 the total axial force ratio  $n$ , axial load ratio  $\eta$ , prestressing force ratio  $\zeta$  and mechanical prestressing  
 136 ratio  $\lambda$ . The parameters are defined as follows:

$$137 \quad n = \frac{N + N_p}{f'_c A} \quad (1)$$

$$138 \quad \eta = \frac{N}{f'_c A} \quad (2)$$

$$139 \quad \zeta = \frac{N_p}{f'_c A} \quad (3)$$

$$140 \quad \lambda = \frac{f_{py} A_p}{f_{py} A_p + f_y A_s} \quad (4)$$

141 where  $N$  is the applied axial load,  $N_p$  is the total prestressing force before test,  $f_c'$  is the cylinder  
142 concrete compressive strength,  $A$  is area of the cross section,  $A_p$  and  $f_{py}$  are the area and yielding  
143 stress (defined by the 85% of its ultimate strength) of the prestressing strands in the cross section  
144 and  $A_s$  and  $f_y$  are the area and yielding stress of mild longitudinal bars. Obviously, the parameters  $\eta$   
145 and  $\zeta$  representing the axial loads induced by the weight of the bridge superstructure and the  
146 prestressing strands, respectively. The parameter  $\lambda$  accounts for the contribution of the prestressing  
147 strands to the overall cross-sectional capacity of the pier. Table 1 summarizes the corresponding  
148 values for different specimens.

## 149 2.2 Test setup and loading sequence

150 The specimens were tested under lateral cyclic loadings while simultaneously being subjected to a  
151 constant axial load. The test setup for each of the specimen is shown in Fig. 2, the specimen was  
152 vertically fixed to the laboratory floor and the top of the pier was held by a vertical hydraulic  
153 actuator to provide axial load, which was used to simulate the weight of the bridge superstructure.  
154 Under the vertical actuator, the specimen was loaded by two horizontal actuators (actuator A and  
155 actuator B) to provide the lateral cyclic loads. It should be noted that as the horizontal actuators  
156 could only provide compressive force, but not able to provide tensile force, two horizontal actuators  
157 were placed in a straight line to provide the lateral cyclic loads. During the tests, actuator A was  
158 first used to push the specimen to a predefined positive displacement, while actuator B was  
159 separated from the specimen. Then, actuator B was used to push the specimen to a predefined  
160 negative displacement, and actuator A was separated from the specimen. By using this method, the  
161 cyclic loadings were achieved. The lateral loading history was divided into two phases: the load  
162 control phase and the displacement control phase. The load control phase was used to determine the  
163 specimen's experimental concrete cracking strength  $F_{cr,e}$ . Then, the specimens were tested under  
164 displacement control mode to study the inelastic behavior of the specimens. During the load control  
165 phase, the theoretical concrete cracking strength  $F_{cr,t}$  was first calculated by using the software

166 Response-2000 (Bentz 2000), which is based on the Modified Compression Field Theory (Bentz et  
167 al. 2006). Then, lateral loads corresponding to 0.6, 0.8, 1.0, 1.2, and 1.4 times of  $F_{cr,t}$  were applied  
168 to the specimens, with each load repeated twice. During the displacement control phase, tests were  
169 conducted to drift levels of 0.32%, 0.5%, 1.0%, 1.5%, 2.0%, 2.5%, 3.0%....., each cycle was  
170 repeated three times, until the lateral strength of the pier declined to 85% of the peak load. Figure 3  
171 shows the lateral loading histories. It should be noted that drift ratio was used as a dimensionless  
172 measure of pier top displacement in the present study. It was defined for the test specimens as the  
173 lateral displacement at the loading point divided by the height of the specimen. The horizontal load  
174 was measured by two load cells on the horizontal actuators, and the horizontal top displacement was  
175 measured by a displacement transducer. This transducer was fixed to the laboratory floor to obtain  
176 the pier top displacement. For specimen with prestressing strands, force measuring transducers were  
177 used to measure the stress of the prestressing strands when the specimen was loaded to the  
178 maximum displacement during the first cycle at each load or displacement level. For specimen  
179 PRC-6, only one force measuring transducer was used to measure the total stress of all strands. For  
180 other specimens, each strand was equipped with a transducer to measure the stress separately.  
181 During the tests, the concrete crack width was measured using the DJCK-2 Crevice Width Finder  
182 (with an accuracy of 0.01 mm), which was manufactured by the Beijing Earth Long Science and  
183 Technology Co., Ltd. It should be noted that, both the maximum and residual concrete crack widths  
184 were measured in the present study. The maximum crack width was measured when the specimen  
185 reached a maximum top displacement (in the first cycle at each load or displacement level). And the  
186 residual crack width was measured when the specimen was unloaded (zero lateral load, in the first  
187 cycle at each load or displacement cycle). Both the maximum and residual crack width listed in the  
188 current study was the measured maximum value for each specimen.

189

### 190 **3 Experimental results**

### 191 3.1 Damage pattern and hysteretic response of the specimens

192 During the tests, no obvious difference is observed for the damage development and failure pattern  
193 between the specimens with and without prestressing strands. For illustration purpose, Fig. 4(a)  
194 shows the failure pattern of the pier without prestressing strands (specimen RC-1) and the failure  
195 pattern of specimen PRC-1 is plotted in Fig. 4(b) to represent the pier with prestressing strands. It  
196 can be seen that both the specimens show a flexural failure mode in regions close to the bottom of  
197 the specimens (the plastic hinge regions).

198 The damage developments of all the specimens are similar with each other as well. During the load  
199 control phase, horizontal flexural cracks develop first in the plastic hinge regions and the crack  
200 length and width increase with the top load. The measured maximum crack width reaches 0.09 mm  
201 in specimen RC-1, while in other specimens they are between 0.03-0.06 mm. Table 2 lists both the  
202 experimental and theoretical concrete cracking strengths of the specimens, it could be found that all  
203 the specimens with prestressing strands show a higher concrete cracking strength than specimen  
204 RC-1, indicating that the concrete cracking strength of the pier could be increased by using vertical  
205 prestressing strands. The experimental and theoretical concrete cracking strengths are close with  
206 each other, and the experimental concrete cracking strengths of the specimens are between 0.8 and  
207 1.2 times of the theoretical concrete cracking strengths. For the residual crack, the measured  
208 residual width is about 0.01 mm in specimen RC-1. While in other specimens (in which prestressing  
209 is applied), no obvious residual crack is observed when the specimens unloaded from the maximum  
210 lateral load during the load control phase.

211 During the displacement control phase, the residual cracks are observed in all the specimens and  
212 both the maximum and residual crack widths increase with the increment of drift ratio. At the drift  
213 level of 0.32% (3.5mm), the maximum crack width reaches 0.25 mm in specimen RC-1, while in  
214 other specimens they are not larger than 0.15 mm. The residual crack width is 0.02 mm in specimen  
215 RC-1 while it is 0.01 mm in other specimens. At the drift level of 1% (11 mm), the maximum crack

216 width is 0.9 mm in specimen RC-1 while the widths are between 0.5-0.7 mm in other specimens.  
217 For the 2% drift level (22 mm), the spalling of the concrete cover initiates in all the specimens, and  
218 the specimens reach the maximum lateral load capacity.

219 It should be noted that during the displacement control phase, some horizontal flexural cracks  
220 extend to the regions which are close to the neutral axial of the cross section. Within this region, the  
221 absolute value of the normal stress is much smaller than the shear stress, some flexural cracks  
222 change to be diagonal shear cracks, as shown in Fig. 4(c). However, generally speaking the  
223 performance of all the specimens is dominated by concrete spalling and longitudinal bar buckling  
224 damages, which could be classified as flexural failure mode.

225 At the later stages of loading (where drift levels are larger than 2%), the cover concrete peels off  
226 and the spiral and longitudinal bars are exposed (Fig. 4(d)), longitudinal bar buckling and concrete  
227 core crushing (Fig. 4(e)) follow progressively within the next displacement cycles. At the end of the  
228 test, the concrete spalling heights of all the specimens are measured and illustrated in Fig. 5, it can  
229 be seen that the concrete spalling damages of all the specimens are concentrated at the plastic hinge  
230 regions, the spalling heights are between 210 and 330 mm, corresponding to 0.7-1.1 times of the  
231 section depth. Except specimen PRC-4, all the specimens with prestressing strands show larger or  
232 similar spalling heights compared with specimen RC-1.

233 It should be mentioned that during the test of specimen PRC-2, one prestressing strand fails due to  
234 the damage of the anchorage and a snapping noise is heard when the drift level reaches 0.5%. For  
235 all the other specimens, the prestressing strands perform well and no rupture damage is observed  
236 during the tests.

237 Figure 6 shows the lateral load vs displacement (drift) hysteretic curves for all the specimens, in  
238 which the occurrences of concrete cover spalling, longitudinal bar buckling and prestressing strand  
239 failure damage are indicated. It can be seen from these figures that a fat hysteretic curve with no  
240 pinching effect is observed for specimen RC-1, in which no prestressing strand is used. For

241 specimens with prestressing strands, specimens PRC-3 and PRC-4 display a slight pinching effect  
242 while pinching is evident in other specimens, and specimen PRC-2 shows the most obvious  
243 pinching effect among all the specimens. Obviously, the pinching effect is attributed to the restoring  
244 force (prestressing force) provided by the prestressing strands. It should be noted, specimen PRC-2  
245 is designed with the maximum mechanical prestressing ratio ( $\lambda=0.76$ ) while the ratio in specimen  
246 PRC-3 is the minimum ( $\lambda=0.44$ ). Even after one prestressing strand is failed, the mechanical  
247 prestressing ratio ( $\lambda=0.70$ ) in specimen PRC-2 is the largest one among all the specimens, indicating  
248 that a high mechanical prestressing ratio will lead to significant pinching effect of the piers. The fat  
249 hysteretic curve of specimen PRC-4 would attribute to the low prestressing stress of the strands in  
250 larger lateral displacement, which would be illustrated in the following section of the work.

### 251 3.2 The strand stress

252 The strand stress is recorded at the maximum displacement during the first cycle at each  
253 displacement level. Figure 7 shows the measured strand stress under different drift ratios. It should  
254 be noted that as only one force measuring transducer is used, the values in specimen PRC-6  
255 representing the average ones of all the four strands. It could be found that the strand stress would  
256 be increased or decreased as a result of the lateral displacement. It also can be seen from the figure  
257 that the stress-drift relationship could almost be regarded as linear in both the positive or negative  
258 directions.

259 Table 3 tabulates the strand stress values in all the specimens. It includes the initial strand stress  
260  $\sigma_{PS,1}$  of all the strands in each specimen measured after the axial load is applied, the measured  
261 maximum strand stress  $\sigma_{PS,max}$  and the minimum strand stress  $\sigma_{PS,min}$  of the strands, and the stress  
262 change amplitude  $\sigma_{PS,var}$  of each strand during the tests. It could be found that except strand PS3 in  
263 specimen PRC-2 (failed due to damage of the anchorage), the measured maximum strand stress is  
264 1410 MPa (strand PS3 in specimen PRC-5), it is about 73% of the ultimate strength of the strand  
265 (1939 MPa as mentioned in Section 2.1), the strands would be elastic and no yielding or rupturing

266 damage would be observed. The measured minimum strand stress is only 8 MPa for strand PS1 in  
267 specimen PRC-4, and the minimum stress of other strands in specimen PRC-4 are less than 200  
268 MPa.

269 The relationship between the total prestressing force provided by the strands (recorded at the  
270 maximum displacement during the first cycle at each displacement level) and the top drift ratio of  
271 the specimens is shown in Fig. 8. Obviously, specimen PRC-5 has the largest prestressing force  
272 while the force in specimen PRC-4 is the minimum. Except specimen PRC-2, the total prestressing  
273 force in all the specimens increases gradually with the lateral drift. For specimen PRC-2, the total  
274 prestressing force decreases suddenly at a drift ratio of 0.5% as a result of the failed strand.

### 275 3.3 Residual drifts

276 Residual drift is an important measurement of post-earthquake functionality of a bridge, normally it  
277 is used to determine whether or not a bridge remains functional following an earthquake. During the  
278 tests, the residual drifts of the specimens are measured when the lateral loads reached zero during  
279 the first cycle at each displacement level. Figure 9(a) shows the relationship between the residual  
280 drift ratio and the applied drift ratio for each specimen, and they are compared in different groups  
281 from Figs. 9(b) to 9(f) to make them clearer.

282 It is obvious that the residual drift in specimen RC-1 is higher than all of the other specimens when  
283 the same drift level is considered, which indicates that employing prestressing strands is quite  
284 effective in reducing the residual drift of bridge piers. It also can be seen from the figure that among  
285 all the specimens with prestressing strands, specimen PRC-4 exhibits the largest residual drift,  
286 while specimen PRC-2 has the minimum residual drift. Except specimen PRC-4, the residual drift  
287 in specimen PRC-3 is much larger than other specimens with prestressing strands in the positive  
288 direction. While in the negative direction, the residual drift of specimen PRC-3 is larger than  
289 specimens PRC-2 and PRC-6. This is because, as can be seen from Table 1, the mechanical  
290 prestressing ratio  $\lambda$  in specimen PRC-2 is the largest (0.76 before the test and changed to 0.70 after

291 one prestressing strand failed) among all the tested specimens. While for specimen PRC-3, the  
292 mechanical prestressing ratio is the minimum (0.44), which indicates that larger mechanical  
293 prestressing ratio can result in lesser residual drift. The reason for the larger residual drift in  
294 specimen PRC-4 is attributed to the low prestressing stresses in the strands, as illustrated in the  
295 above section.

296 Specimen PRC-2 is designed with less longitudinal mild bars than specimen PRC-1, and the  
297 mechanical prestressing ratio of specimen PRC-2 ( $\lambda=0.76$  before the test and changes to 0.70 after  
298 one prestressing strand failed) is larger than specimen PRC-1 ( $\lambda=0.61$ ). As a result, there is a  
299 reduction in residual drift ratio, as shown in Fig. 9(b). The amount of prestressing strands in  
300 specimen PRC-3 is reduced compared with specimen PRC-1, which results in a low mechanical  
301 prestressing ratio ( $\lambda=0.44$  for specimen PRC-3). The reduction of the prestressing strands leads to  
302 higher residual drift ratios, as shown in Fig. 9(c). From the above analysis, it is clear that the  
303 mechanical prestressing ratio  $\lambda$  is an important parameter for controlling the residual drift of the pier,  
304 larger mechanical prestressing ratio can result in lesser residual drift in the piers.

305 The initial prestressing stresses are changed in specimens PRC-4 and PRC-5, and the effect of the  
306 initial prestressing stress on the residual drift is shown in Figs. 9(d) and 9(e). It can be found that  
307 specimen PRC-4 exhibits notable larger residual drift ratio than PRC-1. While the residual drift  
308 ratio in specimen PRC-5 is slightly larger than that in PRC-1. These results indicate that the  
309 influence of the initial prestressing stress on the residual drift is not clear. It should be noted that the  
310 prestressing stress for strand PS1 in specimen PRC-4 is reduced to 8 MPa in large lateral  
311 displacement, the restoring force (prestressing force) provided by this strand would be neglected,  
312 which would induce larger residual drift in specimen PRC-4. From the above analysis, it could be  
313 concluded that the initial prestressing stress should have little influence on residual drift of the pier  
314 if the strands are effective under seismic action.

315 The residual drift in specimen PRC-6 is almost identical to PRC-1, as shown in Fig. 9(f). This is  
316 because both the specimens are designed with the same mechanical prestressing ratio ( $\lambda=0.61$ ). Also,  
317 the total prestressing forces in specimens PRC-1 and PRC-6 are almost the same during the tests, as  
318 shown in Fig. 8. In that case, the location of the prestressing strands has little influence on the  
319 residual drift of the piers.

#### 320 3.4 Residual crack width

321 Residual concrete crack width is also important for the usability of the pier following an earthquake.  
322 Figure 10(a) shows the relationship between the measured maximum residual crack width and  
323 lateral load for all the specimens, and they are compared in different groups from Figs. 10(b) to 10(f)  
324 to make them clearer. It should be noted that as large residual crack width will lead to corrosion  
325 damage of the reinforcement and deterioration of the bridge piers. Normally it is required to limit  
326 the residual crack width within 0.2 mm, beyond this value, corrosion of the reinforcement and  
327 concrete cover spalling damage would occur. It is thus believed that the controlling of residual  
328 crack width becomes meaningless if it is larger than 0.2 mm. In Figs. 10(b) to 10(f), the y-axis is  
329 thus only up to 0.2 mm. The measured residual crack width beyond 0.2 mm can be found in Fig.  
330 10(a).

331 It can be seen from Fig. 10(a) that the residual crack widths in specimen without prestressing  
332 strands (RC-1) are much larger compared with the specimens with prestressing strands. The  
333 maximum residual crack width reaches as much as 1.0 mm in specimen RC-1, while they are not  
334 larger than 0.4 mm in all the other specimens.

335 In all the specimens with prestressing strands, the residual crack widths in specimen PRC-4 are  
336 much larger than the other specimens. And specimen PRC-5 has the minimum residual crack width  
337 compared with other specimens. This is because, as can be seen from Table 1, the prestressing force  
338 ratio in specimen PRC-5 is the largest ( $\zeta=0.15$ ) among all the tested specimens while for specimen  
339 PRC-4 it reaches the minimum ( $\zeta=0.05$ ), which indicates that the prestressing force ratio has a

340 significant influence on the residual crack width, larger prestressing force ratio can result in smaller  
341 residual crack width.

342 Specimen PRC-2 is designed the same as specimen PRC-1 except for longitudinal mild bars, and  
343 the mechanical prestressing ratio of specimen PRC-2 ( $\lambda=0.76$  or  $0.70$ ) is larger than specimen  
344 PRC-1 ( $\lambda=0.61$ ). As a result, the residual crack width in specimen PRC-2 is much smaller than  
345 specimen PRC-1, as shown in Fig. 10(b). Also, the residual crack width in specimen PRC-3 ( $\lambda=0.44$ )  
346 is larger than specimen PRC-1 ( $\lambda=0.61$ ), as shown in Fig. 10(c). Indicating that larger mechanical  
347 prestressing ratio will lead to smaller residual crack width.

348 As shown in Fig. 10(f), the residual crack widths in specimens PRC-1 and PRC-6 are almost similar  
349 with each other. These observations indicate that the arrangement of the strands has little influence  
350 on the residual crack width of the piers if both the prestressing force ratio and the mechanical  
351 prestressing ratio of the specimens are identical with each other.

352 As mentioned above, both the residual drift and residual crack width of specimen PRC-4 are larger  
353 than other specimens with prestressing strands, indicating that the strand stress has a significant  
354 influence on the residual drift and residual crack width. To minimize the residual drift and concrete  
355 crack width in bridge piers, the strand should be kept effective under seismic actions.

### 356 3.5 Strength and ductility of the specimens

357 The strength and ductility of the specimens are compared with each other in this section. The  
358 associated parameters, including the peak load  $F_{\max}$ , yield displacement  $\Delta_1$ , ultimate displacement  
359  $\Delta_{\mu}$ , displacement ductility factor  $\mu_{\Delta}$ , and ultimate drift ratio  $R$ , are obtained based on the skeleton  
360 curve of the specimens as described in Fig. 11. The parameters are defined by the following  
361 equations:

$$362 \quad F_{\max} = \frac{F_{\max}^+ + F_{\max}^-}{2} \quad (5)$$

363 
$$\Delta_1 = \frac{\Delta_1^+ + \Delta_1^-}{2} \quad (6)$$

364 
$$\Delta_\mu = \frac{\Delta_\mu^+ + \Delta_\mu^-}{2} \quad (7)$$

365 
$$\mu_\Delta = \frac{\Delta_\mu}{\Delta_1} \quad (8)$$

366 
$$R = \frac{\Delta_\mu}{L} \quad (9)$$

367 where  $L$  is the height of the specimen, the superscripts + and – denote the corresponding values  
368 obtained at the positive and negative phases respectively.

369 Table 4 lists the measured and calculated strength and ductility parameters of all the specimens. It is  
370 shown that the peak loads of all the specimens with prestressing strands are higher than specimen  
371 RC-1, indicating an increasing of the lateral strength of the pier specimens by using unbonded  
372 prestressing strands. As for the ductility parameters  $\Delta_\mu$ ,  $\mu_\Delta$  and  $R$ , it could be found that all the  
373 specimens exhibit good ductility. The displacement ductility factors of all the specimens are larger  
374 than 4.0, and the ultimate drifts of all the specimens are larger than 3.0%, except for specimen  
375 PRC-2. Also should be noted, the ductility of the specimens with prestressing strands are essentially  
376 the same with specimen RC-1, indicating no obvious change of ductility capacity by using  
377 prestressing strands. This is because, as shown in Table 1, the axial load ratio  $\eta$  of all the specimens  
378 is only 0.10, and the total axial force ratio of all the specimens is equal or less than 0.25, which is  
379 much lower than the axial loading capacity of the piers. With such a low axial load ratio, the using  
380 of the vertical prestressing strands will not have an obvious influence on the deformation capacity  
381 of the piers. In most cases, the axial load ratio of the commonly used bridge piers under dead load  
382 would be less than 0.1, so it is practical to reduce the seismic residual drift and residual concrete  
383 crack width of these piers by using vertical prestressing strands.

384

#### 385 **4 Numerical simulations of the tests**

386 Experimental studies are expensive, time consuming, labor extensive and sometimes may be limited  
387 by the capacities of the experimental facilities. In contrast, numerical simulations are more  
388 convenient and efficient for the analysis. A reliable finite element model is believed to be necessary  
389 for the readers to appreciate the results of the paper. In the present study, numerical simulations are  
390 also carried out by using the open-source finite element code OpenSees. The numerical results are  
391 compared with the experimental data.

##### 392 4.1 Description of the numerical model

393 The total lateral deformation of a column subjected to lateral loads is comprised of deformations  
394 due to three response mechanisms: flexure, longitudinal bar slip at the column footing, and shear. In  
395 the numerical simulation, each deformation component can be conveniently modeled (Yavari et al.  
396 2009; Shoraka et al. 2013). However, as all the specimens failed in flexural mode in the present  
397 study, the shear deformation of the specimen is neglected in the numerical model.

398 The specimens are modeled by using the open-source finite element code OpenSees (Mazzoni et al.  
399 2007) and the finite element scheme is illustrated in Fig. 12. Owing to the large size of the RC  
400 footing, it is not modeled and only the specimen above the footing top is considered. Also should be  
401 noted, as the prestressing strands are anchored at the bottom of the footing, the strand length is  
402 larger than the specimen height in the numerical model.

403 The total lateral response of the specimen are modeled by coupling flexure and longitudinal bar slip  
404 responses by two elements in series, where the force in each element is the same and the total  
405 deformation is the sum of individual element deformations. Flexural deformation is modeled by the  
406 nonlinear beam-column element, while the longitudinal bar slip deformation is modeled by the  
407 zero-length fiber section element. As shown in Fig. 12, each specimen consists of a single nonlinear  
408 beam-column element and a zero length fiber section element located at the bottom of the

409 beam-column element. The length of the beam-column element (distance between Node 2 and Node  
410 3) is the same as the height the specimen between footing top surface to the point where lateral  
411 loading is applied. The fiber section element is defined by two nodes (Node 1 and Node 2) at the  
412 same location.

#### 413 4.1.1 Flexural deformation

414 The force-based nonlinear beam-column element, implemented in OpenSees, accounts for the  
415 nonlinear flexural deformation by assuming plane sections remain plane and captures the spread of  
416 plasticity along the element while the shear and longitudinal bar slip deformations are neglected  
417 (Spacone et al. 1996a, 1996b). The nonlinear hysteretic behavior of the element derives from the  
418 constitutive relations of concrete and reinforcing steel fibers into which each section is divided. All  
419 concrete fibers are modeled by using the “Concrete01” uniaxial material model in OpenSees, which  
420 is based on the modified Kent and Park concrete model (1971). Longitudinal mild bars are modeled  
421 using “Steel02”, based on the Giuffre-Menegotto-Pinto model.

422 The prestressing strands are modeled separately from the beam-column fiber section by using truss  
423 elements fixed at the bottom and connected rigidly to the fiber section at the top. As no yielding of  
424 the strands occurred during the tests, the stress-strain relationship of the truss element is assumed to  
425 be linear. Rigid element connects the specimen fiber section to the anchorage of the prestressing  
426 strands, which are modeled by beam-column element with much higher strength and stiffness.

#### 427 4.1.2 Longitudinal bar slip deformation

428 Longitudinal bar slip deformation results from the extension of the mild longitudinal bar from the  
429 specimen footing, this deformation generates rigid body rotation of the specimen that can  
430 substantially increase member flexibility (Ghannoum and Moehle 2012). To model bar slip  
431 deformation, a zero length fiber section element is used. The section of the element has the same  
432 geometry as the fiber section of the beam-column element it is attached to but with different

433 material properties for its steel and concrete fibers (Ghannoum 2007; Melo et al. 2011; Ghannoum  
434 and Moehle 2012; Zhang et al. 2013).

435 For steel fiber in the fiber section element, the constitutive law of the steel reinforcement is  
436 modified from a stress-strain relation to a stress-slip relation. A hysteretic model for the bar stress  
437 versus loaded-end slip response developed by Zhao and Sritharan (2007) is adopted, and the bar  
438 stress  $\sigma$  versus loaded-end slip  $s$  relationship is shown in Fig. 13. The slip values corresponding to  
439 bar yielding ( $s_y$ ) and ultimate strength ( $s_u$ ) are calculated using Eqs. (10) and (11), respectively.

$$440 \quad s_y \text{ (mm)} = 2.54 \left( \frac{d_b \text{ (mm)}}{8437} \frac{f_y \text{ (MPa)}}{\sqrt{f'_c \text{ (MPa)}}} (2\alpha + 1) \right)^{1/\alpha} + 0.34 \quad (10)$$

$$441 \quad s_u \text{ (mm)} = (30 \sim 40)s_y \quad (11)$$

442 where,  $d_b$  is the bar diameter,  $\alpha$  is the parameter used in the local bond-slip relation and is taken as  
443 0.4.

444 For parameters shown in Fig. 13,  $f_u$  is the ultimate strength of the mild reinforcing bar.  $K$  is the  
445 slope of the straight line for bar stress  $\sigma$  versus loaded-end slip  $s$  relationship, and  $b$  is stiffness  
446 reduction factor ( $b=0.3 \sim 0.5$ ).  $R$  is power index of unloading/reloading curve ( $R=0.5 \sim 1.0$ ).

447 For concrete fiber in the fiber section element, the “Concrete01” uniaxial material model is also  
448 used as in the beam-column element. While the concrete strain at maximum stress is multiplied by a  
449 scale factor  $F_{conc}$  ( $F_{conc}=10 \sim 20$ ) to maintain compatibility between the beam-column element and  
450 the bar slip section element (Ghannoum, 2007), as shown in Fig. 14.

#### 451 4.2 Comparison between numerical and experimental results

452 It is very difficult to model the residual concrete crack width for reinforced concrete structures.  
453 Only the hysteretic curves, residual drifts and prestressing strand stress are compared with the test  
454 results in this study.

455 In Fig. 15, a comparison between experimental and numerical hysteretic curves of the specimens is  
456 illustrated. It can be seen that the calculated curves of all the specimens coincide well with  
457 experimental results in terms of strength, stiffness, residual displacement and overall performance.  
458 These results indicate that the proposed numerical model is adequate to evaluate the hysteretic  
459 behavior of the pier specimens with unbonded prestressing strands.

460 Figure 16 shows the residual drifts of the specimens from experimental results and numerical  
461 analyses. In general, a good agreement is observed between the numerical and experimental results.  
462 For specimens PRC-1, PRC-3, and PRC-6, the simulated residual drifts are slightly larger than the  
463 corresponding experimental results in the negative direction. But more accurate numerical results  
464 are observed in the positive direction. The differences between the experimental and numerical  
465 results are very likely caused by the asymmetry of the specimen response during the tests.

466 Taken strand PS-2 (for specimen PRC-6, PS is taken since the stress was measured together as  
467 mentioned above) as an example, Figure 17 shows the strand stress of the specimens from  
468 experimental results and numerical analysis. It could be found that the simulated strand stress agree  
469 well with experimental results, which indicates that the proposed numerical model can accurately  
470 simulate the unbonded strand stress under cyclic loading.

471

## 472 **5 Conclusions**

473 Longitudinal unbonded prestressing strands are used to minimize the residual drift and residual  
474 concrete crack width in RC bridge piers. A series of experimental studies were carried out to  
475 examine the influences of various parameters including the prestressing force ratio, the mechanical  
476 prestressing ratio and the location of the prestressing strands on the bridge pier residual drift and  
477 residual concrete crack width. A FE model was developed and calibrated by using the open-source  
478 finite element code OpenSees. Following conclusions are drawn:

479 1. During the tests, no obvious difference is observed for the damage development and failure  
480 pattern between the specimens with and without prestressing strands. Flexural failure occurs in all  
481 the specimens under lateral cyclic loading, and these failures include concrete cracking, concrete  
482 cover spalling and longitudinal bar buckling.

483 2. The residual drift of bridge piers can be reduced by using the vertical unbonded prestressing  
484 strands, and the mechanical prestressing ratio is an important parameter for controlling the residual  
485 drift of the piers. Larger mechanical prestressing ratio would lead to smaller residual drift. The  
486 initial prestressing stress and the arrangement of the strands have little influence on residual drift of  
487 the piers.

488 3. The residual concrete crack width of the piers can be reduced significantly by using vertical  
489 unbonded prestressing strands. Both the prestressing force ratio and the mechanical prestressing  
490 ratio have a significant influence on the residual crack width, larger prestressing force ratio and  
491 mechanical prestressing ratio would lead to smaller residual crack width. The arrangement of the  
492 strands has little influence on the residual crack width.

493 4. During the tests, the strand stress increases or decreases almost linearly with the pier drift. Except  
494 for one strand fails due to damage of the anchorage, all the other strands are elastic and no yielding  
495 or rupturing damage is observed. To minimize the residual drift and concrete crack width in bridge  
496 piers, the strand should be kept effective under seismic actions.

497 5. The lateral strength of the pier specimens can be increased by using unbonded prestressing  
498 strands, while the ductility capacity of the piers with prestressing strands is not obviously changed.  
499 It is practical to reduce the seismic residual drift and residual concrete crack width of bridge piers  
500 by using prestressing strands for commonly used bridge piers with an axial load ratio less than 0.1.

501 6. The proposed numerical model is adequate to evaluate the hysteretic behavior of the pier  
502 specimens with prestressing strands.

503

504 **Acknowledgements**

505 The authors gratefully acknowledge the support for this research by the National Natural Science  
506 Foundation of China under Grant Nos. 51008041 and 51178071, China Postdoctoral Science  
507 Foundation under Grant Nos. 2013M540226 and 2014T70250. The third author acknowledges the  
508 partial support from Australian Research Council Discovery Early Career Research Award  
509 (DECRA).

510

511 **References**

- 512 Bentz E C (2000) Sectional analysis of reinforced concrete members. Ph.D. Thesis, University of Toronto,  
513 Toronto, Canada
- 514 Bentz E C, Vecchio F J, Collins M P (2006) Simplified modified compression field theory for calculating shear  
515 strength of reinforced concrete elements. *ACI Structural Journal* 103(4): 614-624
- 516 Fujino Y, Hashimoto S, Abe M (2005) Damage analysis of Hanshin expressway viaducts during 1995 Kobe  
517 earthquake. I: Residual inclination of reinforced concrete piers. *Journal of Bridge Engineering, ASCE* 10(1):  
518 45-53
- 519 Ghannoum W M (2007) Experimental and analytical dynamic collapse study of a reinforced concrete frame with  
520 light transverse reinforced. Ph.D. Thesis, University of California, Berkeley, Berkeley, USA
- 521 Ghannoum W M, Moehle J P (2012) Dynamic collapse analysis of a concrete frame sustaining column axial  
522 failures. *ACI Structural Journal* 109(3): 403-412
- 523 Guo A X, Yuan W, Lan C M, Guan X C, Li H (2015) Time-dependent seismic demand and fragility of  
524 deteriorating bridges for their residual service life. *Bulletin of Earthquake Engineering* 13(8): 2389-2409.
- 525 Hashimoto S, Fujino Y, Abe M (2005) Damage analysis of Hanshin expressway viaducts during 1995 Kobe  
526 earthquake. II: Damage mode of single reinforced concrete piers. *Journal of Bridge Engineering, ASCE* 10(1):  
527 54-60
- 528 Iemura H, Takahashi Y, Sogabe N (2004) Development of unbonded bar reinforced concrete structures.  
529 Proceeding of the 13th World Conference on Earthquake Engineering, Vancouver, B.C., Canada, Paper  
530 Number: 1537
- 531 Kawashima K, Macrae G A, Hoshikuma J I, Nagaya K (1998) Residual displacement response spectrum. *Journal*  
532 *of Structural Engineering, ASCE* 124(5): 523-530
- 533 Kent D C, Park R (1971) Flexural members with confined concrete. *Journal of the Structural Division* 97(7):  
534 1969-1990

535 Mahin S, Sakai J, Jeong H (2006) Use of partially prestressed reinforced concrete columns to reduce  
536 post-earthquake residual displacements of bridges. Proceeding of the 5th National Seismic Conference on  
537 Bridge & Highways, San Francisco, America

538 Mazzoni S, McKenna F, Scott M H, Fenves G L (2007) Opensees command language manual. Pacific Earthquake  
539 Engineering Research Center, University of California, Berkeley

540 Melo J, Fernandes C, Varum H, Rodrigues H, Costa A, Arêde A (2011) Numerical modeling of the cyclic  
541 behavior of RC elements built with plain reinforcing bars. *Engineering Structures* 33: 273-286

542 Moshref A, Tehranizadeh M, Khanmohammadi M (2015) Investigation of the reliability of nonlinear modeling  
543 approaches to capture the residual displacements of RC columns under seismic loading. *Bulletin of*  
544 *Earthquake Engineering* 13(8): 2327-2345.

545 Ou Y C, Wang P H, Tsai M S, Chang K C, Lee G C (2010) Large-scale experimental study of precast segmental  
546 unbonded posttensioned concrete bridge columns for seismic regions. *Journal of Structural Engineering,*  
547 *ASCE* 136(3): 255-264

548 Sakai J, Mahin S A (2004a) Analytical investigations of new methods for reducing residual displacements of  
549 reinforced concrete bridge columns. Report No. PEER-2004/02, Pacific Earthquake Engineering Research  
550 Center, College of Engineering, University of California, Berkeley, California, USA.

551 Sakai J, Mahin S A (2004b) Mitigation of residual displacements of circular reinforced concrete bridge columns.  
552 Proceeding of the 13th World Conference on Earthquake Engineering, Vancouver, B.C., Canada, Paper  
553 Number: 1622

554 Shim C S, Chung C H, Kim H H (2008) Experimental evaluation of seismic performance of precast segmental  
555 bridge piers with a circular solid section. *Engineering Structures* 30: 3782-3792

556 Shoraka M B, Elwood K J (2013) Mechanical model for non ductile reinforced concrete columns. *Journal of*  
557 *Earthquake Engineering* 17(7): 937-957

558 Spacone E, Filippou F C, Taucer F F (1996a) Fiber beam-column model for non-linear analysis of R/C frames:  
559 Part I. Formulation. *Earthquake Engineering and Structural Dynamics* 25(7): 711-725

560 Spacone E, Filippou F C, Taucer F F (1996b) Fiber beam-column model for non-linear analysis of R/C frames:  
561 Part II. Applications. *Earthquake Engineering and Structural Dynamics* 25(7): 727-742

562 Sun Z, Wang D, Guo X, Si B, Huo Y (2012) Lessons learned from the damaged Huilan interchange in the 2008  
563 Wenchuan earthquake. *Journal of Bridge Engineering, ASCE* 17(1): 15-24

564 Wang J C, Ou Y C, Chang K C, Lee G C (2008) Large-scale seismic tests of tall concrete bridge columns with  
565 precast segmental construction. *Earthquake Engineering and Structural Dynamics* 37(12): 1449-1465

566 Yamashita R, Sanders D H (2009) Seismic performance of precast unbonded prestressed concrete columns. *ACI*  
567 *Structural Journal* 106(6): 821-830

568 Yavari S, Elwood K J, Wu C L (2009) Collapse of a nonductile concrete frame: Evaluation of analytical models.  
569 *Earthquake Engineering and Structural Dynamics* 38(2): 225-241

570 Zatar W A, Mutsuyoshi H (2002) Residual displacements of concrete bridge piers subjected to near field  
571 earthquakes. *ACI Structural Journal* 99(6): 740-749

572 Zhang Y Y, Harries K A, Yuan W C (2013) Experimental and numerical investigation of the seismic performance  
573 of hollow rectangular bridge piers constructed with and without steel fiber reinforced concrete. *Engineering*  
574 *Structures* 48: 255-265

575 Zhao J, Sritharan S (2007) Modeling of strain penetration effects in fiber-based analysis of reinforced concrete  
576 structures. *ACI Structural Journal* 104(2): 133-141

577 Zhuang W L, Liu Z Y, Jiang J S (2009) Earthquake-induced damage analysis of highway bridges in Wenchuan  
578 earthquake and countermeasures. *Chinese Journal of Rock Mechanics and Engineering* 28(7): 1377-1387. [in  
579 Chinese]

580

581

582

583

584

### **List of table captions**

585 **Table 1** Test parameters of the pier specimens

586 **Table 2** The experimental and theoretical concrete cracking strengths of the specimens

587 **Table 3** The strand stress of the specimens

588 **Table 4** Strength and ductility parameters of the specimens

589

590

591

592

593

594

595

596

597

598

599

**Table 1 Test parameters of the pier specimens**

Specimen	Longitudinal bars	Prestressing strands	$n$	$\eta$	$\zeta$	$\lambda$	Description of the specimen
RC-1	Eight 12 mm-dia. bars	Without	0.1	0.1	0	0	Specimen without prestressing strands
PRC-1	Eight 12 mm-dia. bars	Four 12.7 mm-dia. strands	0.2	0.1	0.1	0.61	Standard specimen with prestressing strands
PRC-2	Eight 8 mm-dia. bars	Four 12.7 mm-dia. strands	0.2	0.1	0.1	0.76	Longitudinal bars were reduced compared with specimen PRC-1
PRC-3	Eight 12 mm-dia. bars	Two 12.7 mm-dia. strands	0.15	0.1	0.05	0.44	Prestressing strands were reduced compared with specimen PRC-1
PRC-4	Eight 12 mm-dia. bars	Four 12.7 mm-dia. strands	0.15	0.1	0.05	0.61	Initial prestressing stress was reduced compared with specimen PRC-1
PRC-5	Eight 12 mm-Dia. bars	Four 12.7 mm-dia. strands	0.25	0.1	0.15	0.61	Initial prestressing stress increased compared with specimen PRC-1
PRC-6	Eight 12 mm-dia. bars	Four 12.7 mm-dia. strands	0.2	0.1	0.1	0.61	Concentrated prestressing strands was used

601

602

603

604

605

606

607

608

609

610

611

612

613

614

615

616

**Table 2 The experimental and theoretical concrete cracking strengths of the specimens**

Specimen	$F_{cr,e}$ (kN)	$F_{cr,t}$ (kN)	$F_{cr,e}/F_{cr,t}$
RC-1	20	17	1.2
PRC-1	34	34	1.0
PRC-2	26	33	0.8
PRC-3	24	30	0.8
PRC-4	29	24	1.2
PRC-5	31	39	0.8
PRC-6	24	30	0.8

617

618

619

620

621

622

623

624

625

626

627

628

629

630

631

632

633

634

**Table 3 The strand stress of the specimens**

Specimen	Strand	$\sigma_{PS,1}$ (MPa)	$\sigma_{PS,max}$ (MPa)	$\sigma_{PS,min}$ (MPa)	$\sigma_{PS,var}$ (MPa)	
					$\sigma_{PS,max}-\sigma_{PS,1}$	$\sigma_{PS,1}-\sigma_{PS,min}$
PRC-1	PS1	686	1020	573	334	113
	PS2	662	1057	464	395	198
	PS3	660	1061	502	401	158
	PS4	656	998	520	342	136
PRC-2	PS1	714	998	605	284	109
	PS2	766	1031	640	265	126
	PS3*	743	786	700	43	43
	PS4	694	1098	500	404	194
PRC-3	PS1	773	1173	427	400	346
	PS2	816	1246	619	430	197
PRC-4	PS1	310	521	8	211	302
	PS2	342	644	197	302	145
	PS3	326	606	42	280	284
	PS4	320	673	128	353	192
PRC-5	PS1	925	1212	732	287	193
	PS2	1037	1289	857	252	180
	PS3	1097	1410	931	313	166
	PS4	1036	1342	845	306	191
PRC-6	PS	701	855	694	154	7

636 \* Strand failed as a result of damage of the anchorage at 0.5% drift.

637

638

639

**Table 4 Strength and ductility parameters of the specimens**

Specimens	$F_{\max}$ (kN)	$\Delta_1$ (mm)	$\Delta_{\mu}$ (mm)	$\mu_{\Delta}$	$R$ (%)
RC-1	70.9	7.0	35.3	5.0	3.2
PRC-1	95.3	8.0	37.2	4.7	3.4
PRC-2	81.5	6.0	31.7	5.3	2.9
PRC-3	83.8	7.6	38.7	5.1	3.5
PRC-4	84.7	8.0	38.3	4.8	3.5
PRC-5	102.3	7.7	32.6	4.2	3.0
PRC-6	93.5	7.5	36.8	4.9	3.3

640

641

642

643

644

645

646

647

648

649

650

651

652

653

654

655

656

## List of Figure Captions

657 **Fig. 1** Design details of the pier specimens: **a** elevation view; **b** reinforcement layout; **c** prestressing  
658 strand layout (unit: mm)

659 **Fig. 2** Test setup

660 **Fig. 3** Lateral loading histories

661 **Fig. 4** Failure patterns of the specimens: **a** failure pattern of the specimen without prestressing  
662 strands at the end of the test (RC-1); **b** failure pattern of a specimen with prestressing strands at the  
663 end of the test (PRC-1); **c** flexural and shear concrete cracks; **d** concrete cover spalling and  
664 exposing of the transverse bars; **e** longitudinal bar buckling and concrete core crushing damage

665 **Fig. 5** Sketches of concrete spalling heights of specimens: **a** RC-1; **b** PRC-1; **c** PRC-2; **d** PRC-3; **e**  
666 PRC-4; **f** PRC-5; **g** PRC-6

667 **Fig. 6** Hysteretic curves of the specimens: **a** RC-1; **b** PRC-1; **c** PRC-2; **d** PRC-3; **e** PRC-4; **f** PRC-5;  
668 **g** PRC-6

669 **Fig. 7** Strand stress-drift relationship of the specimens: **a** PRC-1; **b** PRC-2; **c** PRC-3; **d** PRC-4; **e**  
670 PRC-5; **f** PRC-6

671 **Fig. 8** Prestressing force-drift relationship of the specimens

672 **Fig. 9** Residual drifts: **a** all the specimens; **b** RC-1, PRC-1 and PRC-2; **c** RC-1, PRC-1 and PRC-3;  
673 **d** RC-1, PRC-1 and PRC-4; **e** RC-1, PRC-1 and PRC-5; **f** RC-1, PRC-1 and PRC-6

674 **Fig. 10** Residual concrete crack widths: **a** all the specimens; **b** RC-1, PRC-1 and PRC-2; **c** RC-1,  
675 PRC-1 and PRC-3; **d** RC-1, PRC-1 and PRC-4; **e** RC-1, PRC-1 and PRC-5; **f** RC-1, PRC-1 and  
676 PRC-6

677 **Fig. 11** Definition of the strength and ductility parameters

678 **Fig. 12** Numerical model of the specimens

679 **Fig. 13** Bar stress versus loaded-end slip response model proposed by Zhao and Sritharan [20]: **a**  
680 under monotonic loading; **b** hysteretic response

681 **Fig. 14** Stress strain relations for beam-column element and bar slip element concrete fibers

682 **Fig. 15** Experimental and numerical hysteretic curves: **a** RC-1; **b** PRC-1; **c** PRC-2; **d** PRC-3; **e**

683 PRC-4; **f** PRC-5; **g** PRC-6

684 **Fig. 16** Experimental and numerical residual drifts: **a** RC-1; **b** PRC-1; **c** PRC-2; **d** PRC-3; **e** PRC-4;

685 **f** PRC-5; **g** PRC-6

686 **Fig. 17** Experimental and numerical strand stress: **a** PRC-1; **b** PRC-2; **c** PRC-3; **d** PRC-4; **e** PRC-5;

687 **f** PRC-6

688

689

690

691

692

693

694

695

696

697

698

699

700

701

702

703

704

705

706

707

708

709

710

711

712

713

714

715

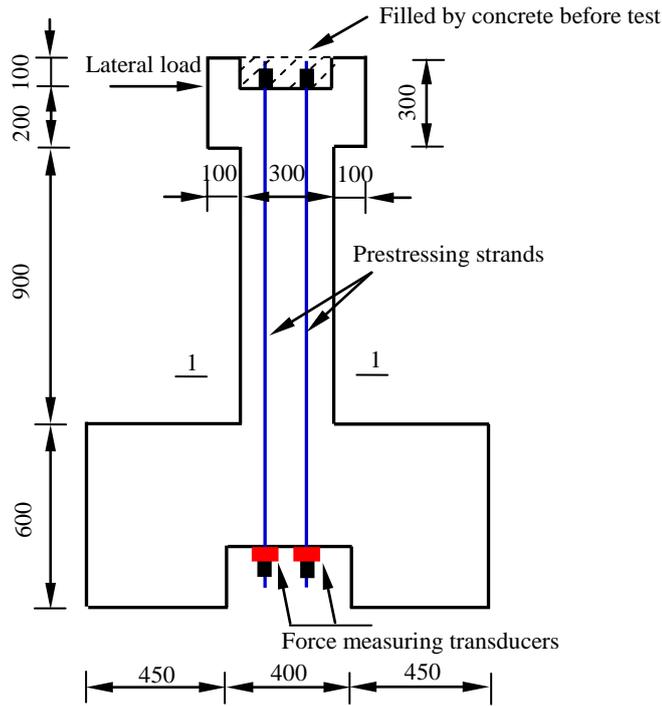
716

717

718

719

720



(a)

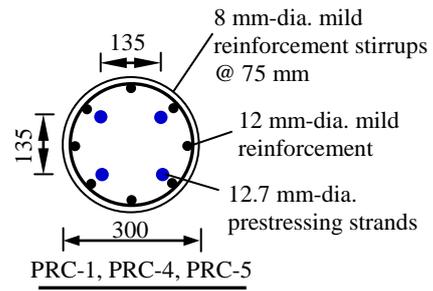
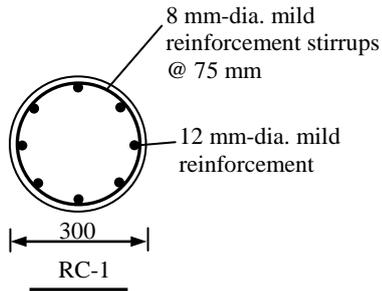
721

722

723

724

725

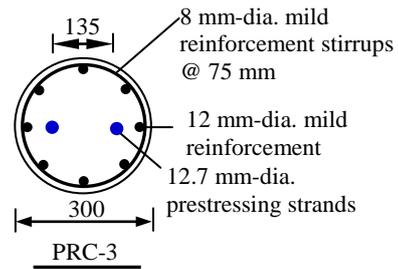
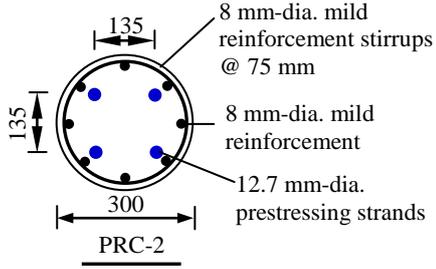


726

727

728

729



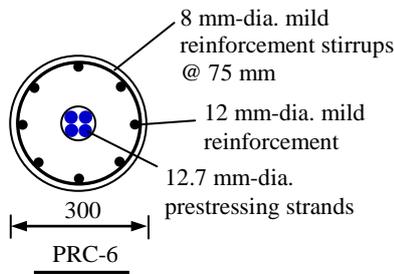
730

731

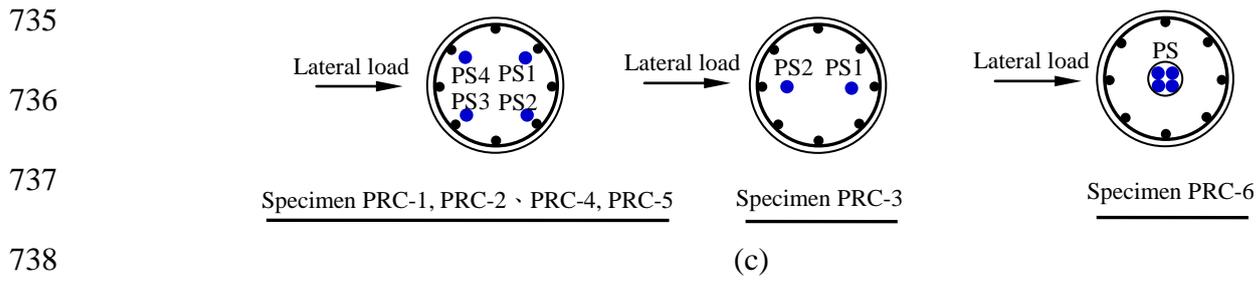
732

733

734



(b)



739 **Fig. 1** Design details of the pier specimens: **a** elevation view; **b** reinforcement layout; **c** prestressing  
 740 strand layout (unit: mm)

741

742

743

744

745

746

747

748

749

750

751

752

753

754

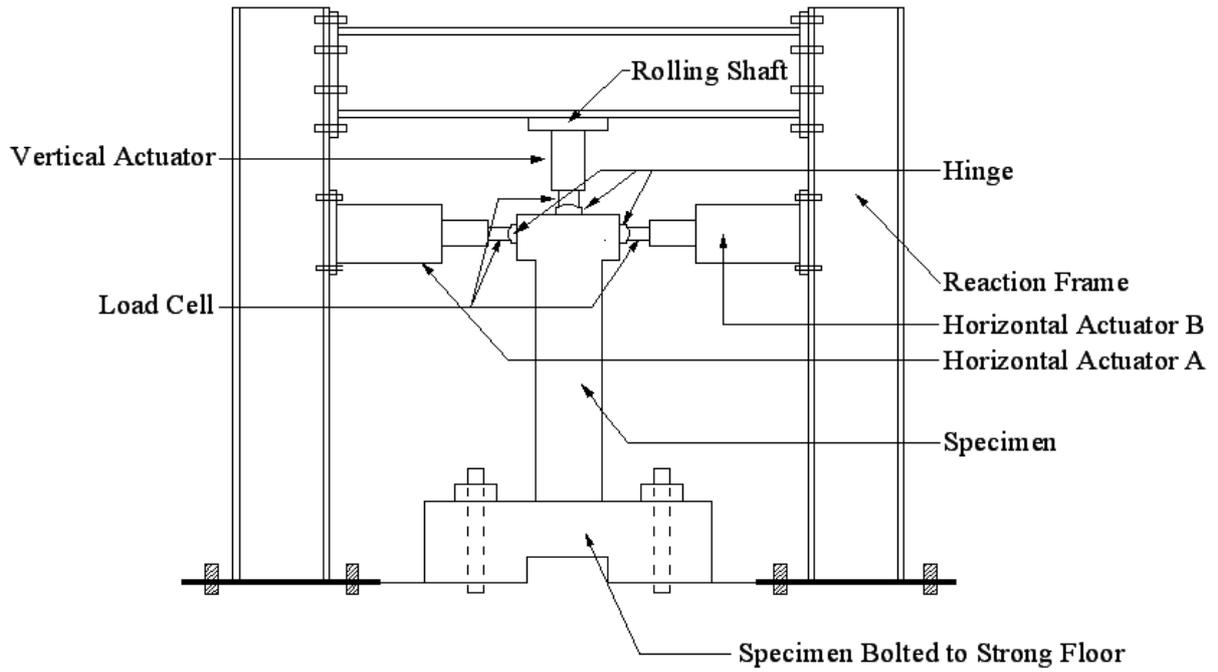
755

756

757

758

759



760

761 **Fig. 2** Test setup

762

763

764

765

766

767

768

769

770

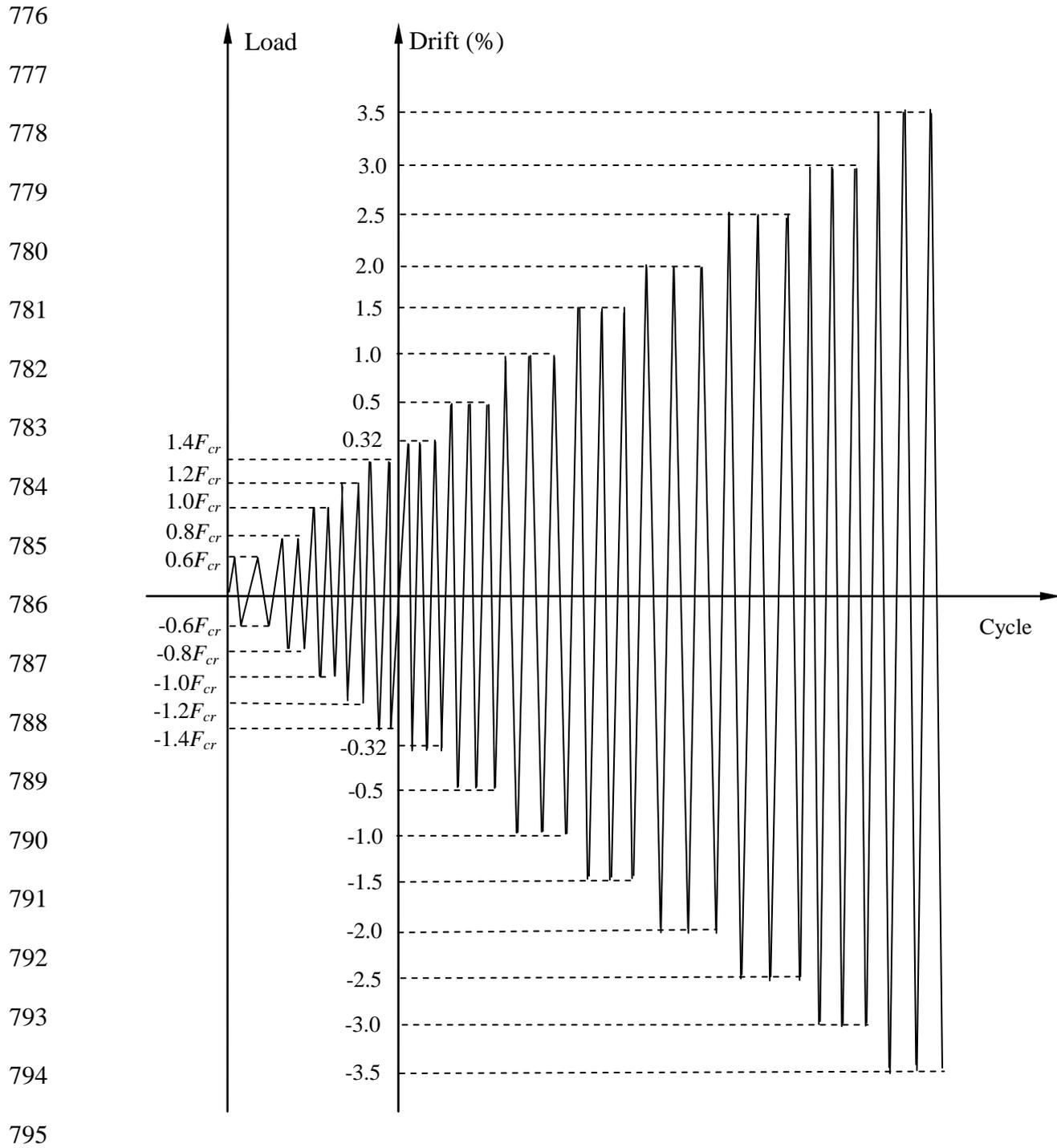
771

772

773

774

775



**Fig. 3** Lateral loading histories



(a)



(b)



(c)



(d)



(e)

798  
799

800

801

802 **Fig. 4** Failure patterns of the specimens: **a** failure pattern of the specimen without prestressing  
803 strands at the end of the test (RC-1); **b** failure pattern of a specimen with prestressing strands at the  
804 end of the test (PRC-1); **c** flexural and shear concrete cracks; **d** concrete cover spalling and  
805 exposing of the transverse bars; **e** longitudinal bar buckling and concrete core crushing damage

806

807

808

809

810

811

812

813

814

815

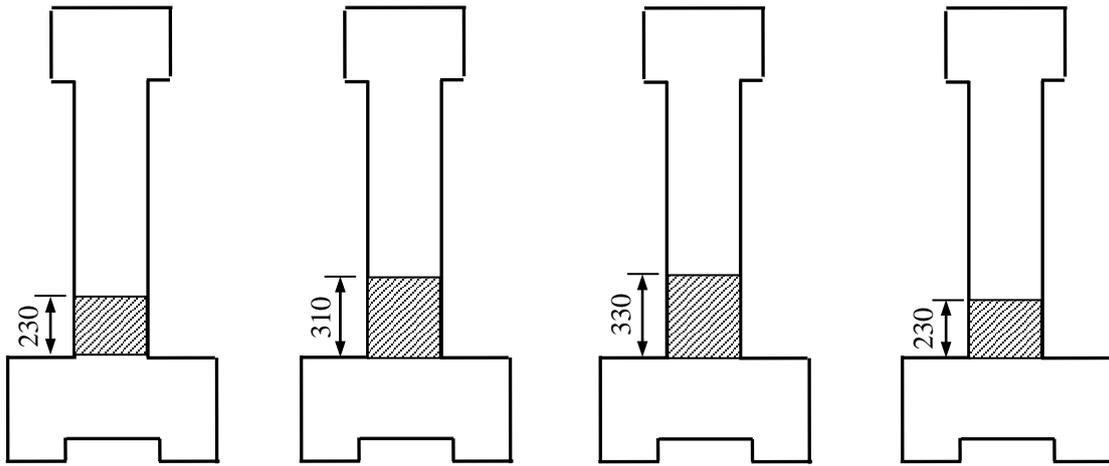
816

817

818

819

820



821

(a)

(b)

(c)

(d)

822

823

824

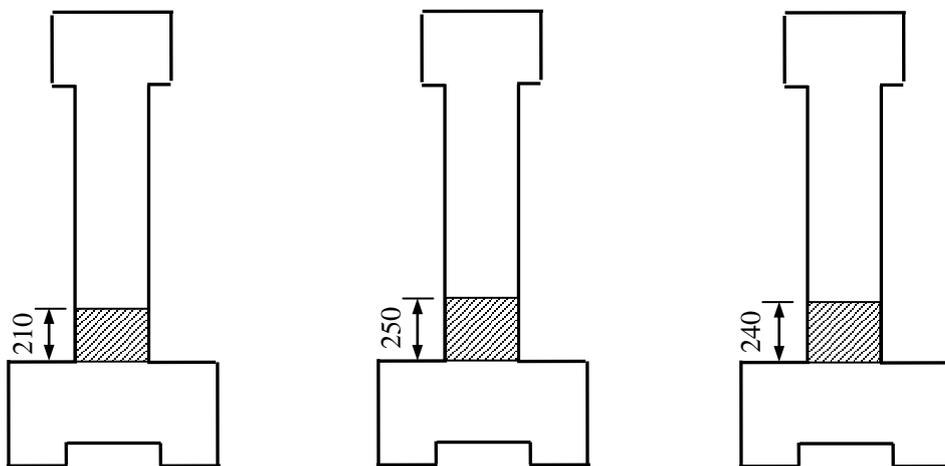
825

826

827

828

829



830

(e)

(f)

(g)

831 **Fig. 5** Sketches of concrete spalling heights of specimens: **a** RC-1; **b** PRC-1; **c** PRC-2; **d** PRC-3; **e**

832 PRC-4; **f** PRC-5; **g** PRC-6

833

834

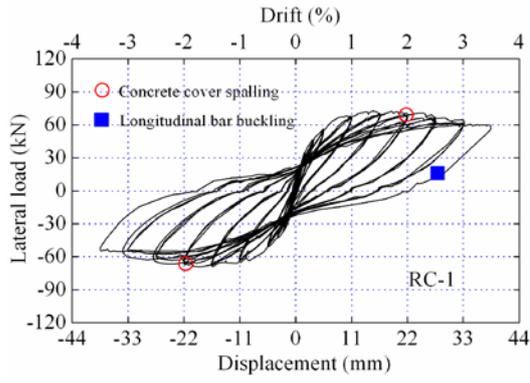
835

836

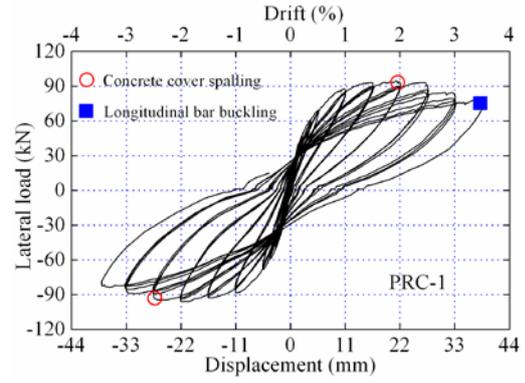
837

838

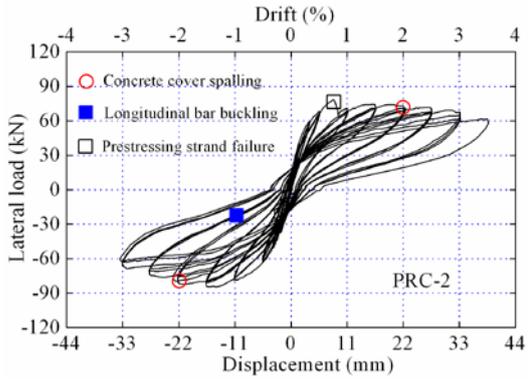
839  
840



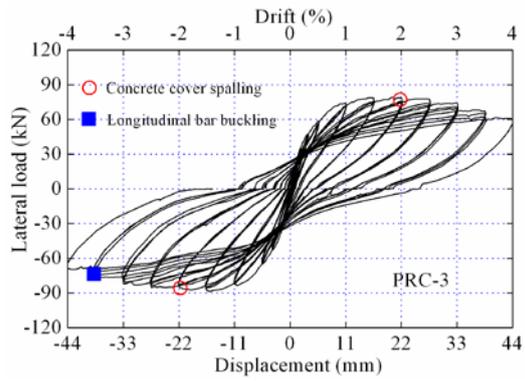
(a)



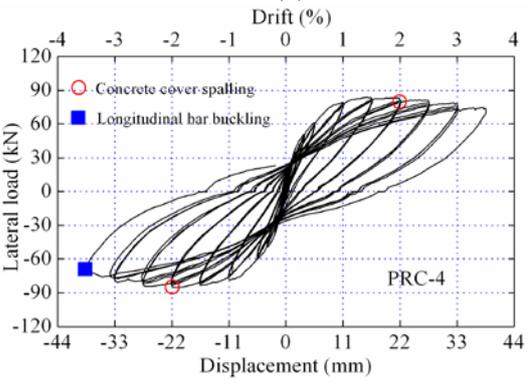
(b)



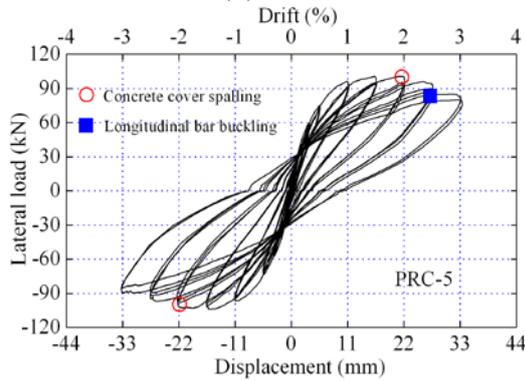
(c)



(d)

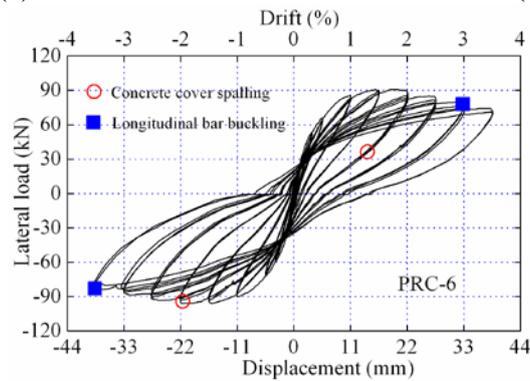


(e)



(f)

843  
844



(g)

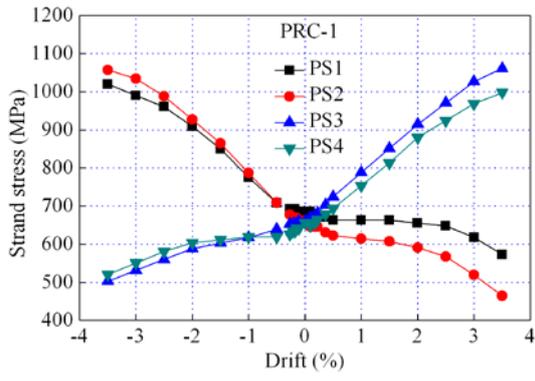
845  
846

847 **Fig. 6** Hysteretic curves of the specimens: **a** RC-1; **b** PRC-1; **c** PRC-2; **d** PRC-3; **e** PRC-4; **f** PRC-5;

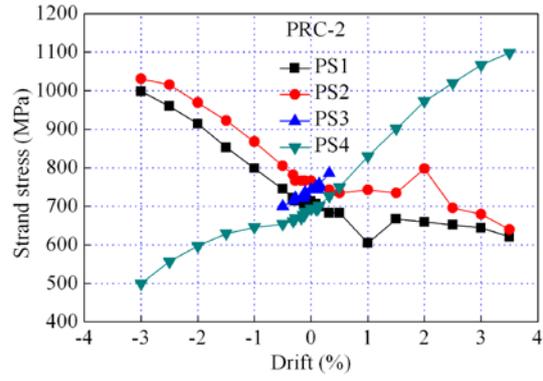
848

**g** PRC-6

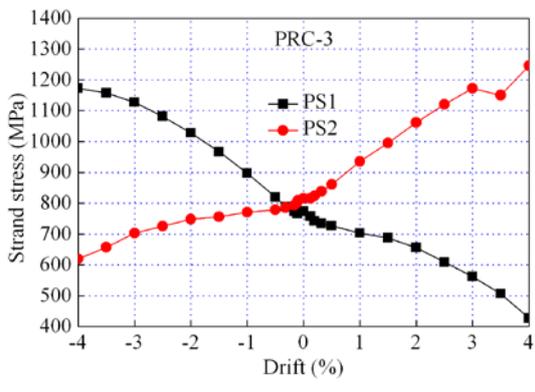
849



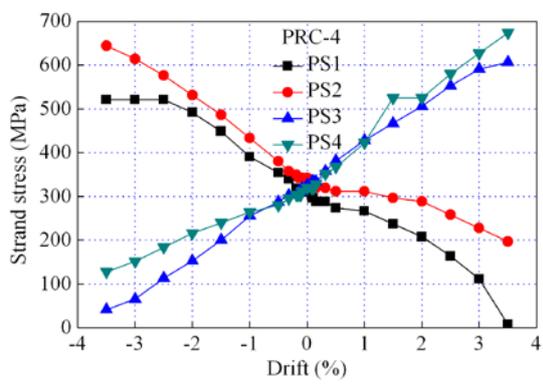
(a)



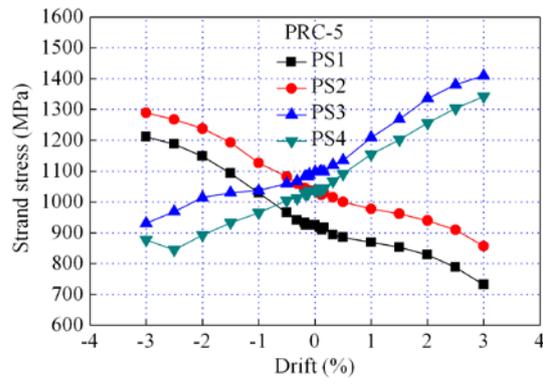
(b)



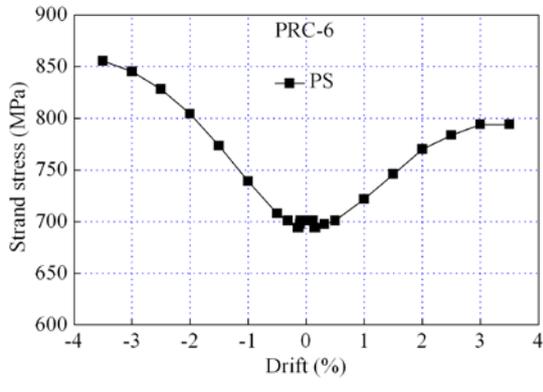
(c)



(d)



(e)



(f)

850

851

852

853

854

855

856

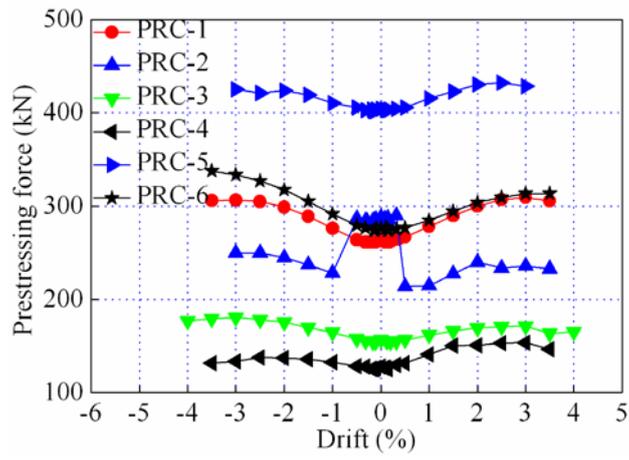
857

858

859

860

**Fig. 7** Strand stress-drift relationship of the specimens: **a** PRC-1; **b** PRC-2; **c** PRC-3; **d** PRC-4; **e** PRC-5; **f** PRC-6



861

862 **Fig. 8** Prestressing force-drift relationship of the specimens

863

864

865

866

867

868

869

870

871

872

873

874

875

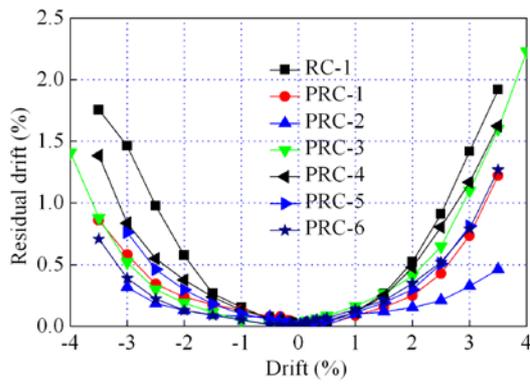
876

877

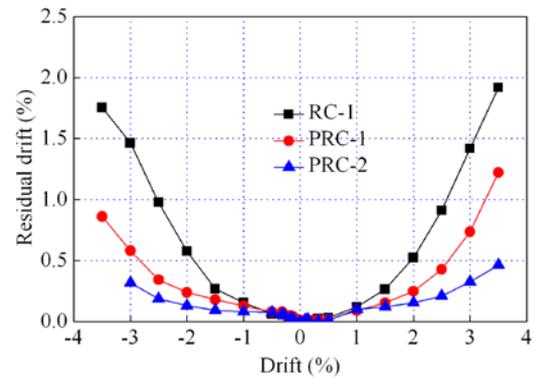
878

879

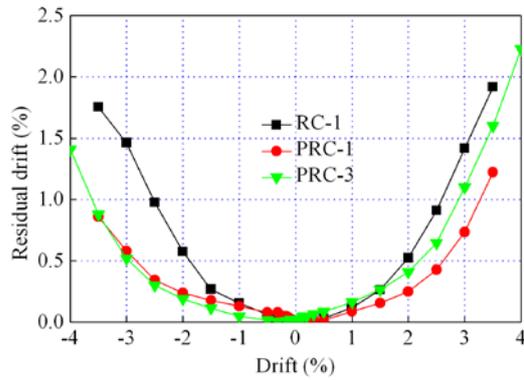
880



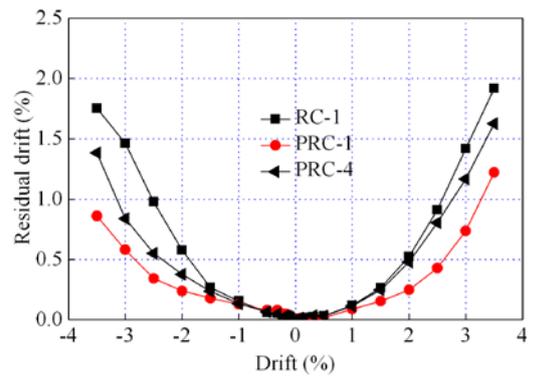
(a)



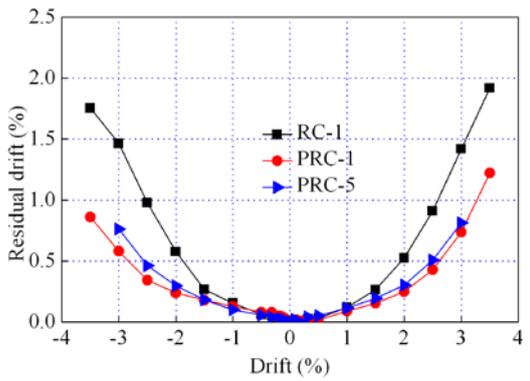
(b)



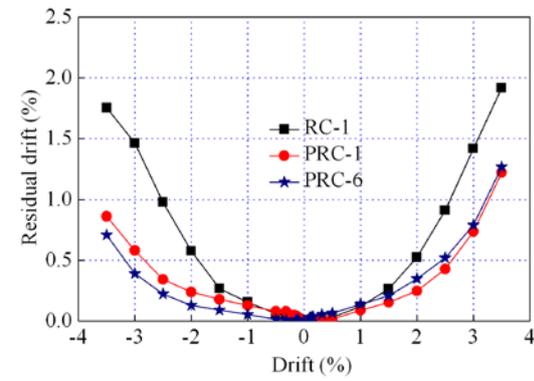
(c)



(d)



(e)



(f)

881

882

883

884

885

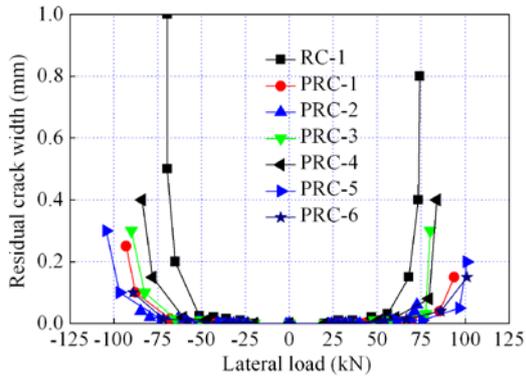
886

887 **Fig. 9** Residual drifts: **a** all the specimens; **b** RC-1, PRC-1 and PRC-2; **c** RC-1, PRC-1 and PRC-3;

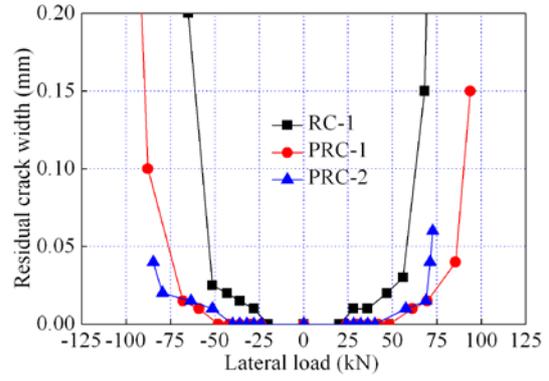
888 **d** RC-1, PRC-1 and PRC-4; **e** RC-1, PRC-1 and PRC-5; **f** RC-1, PRC-1 and PRC-6

889

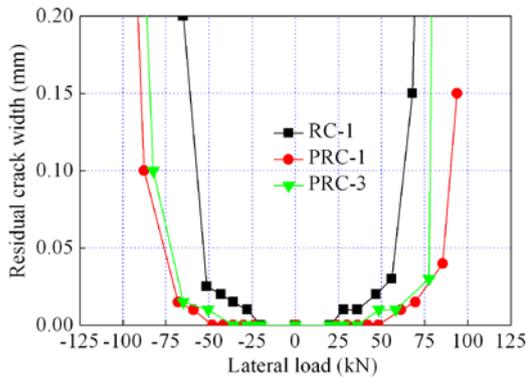
890



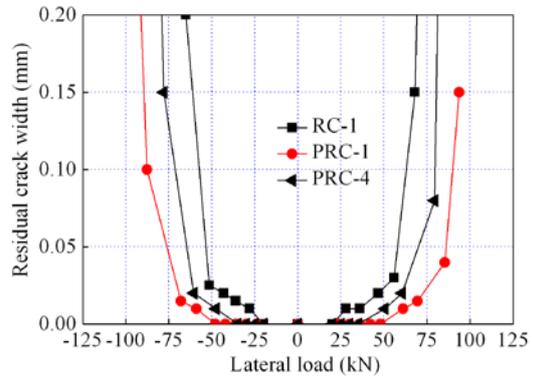
(a)



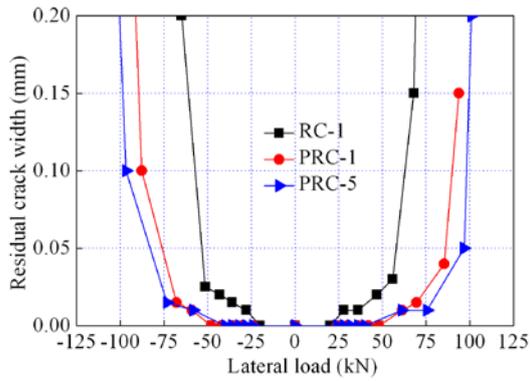
(b)



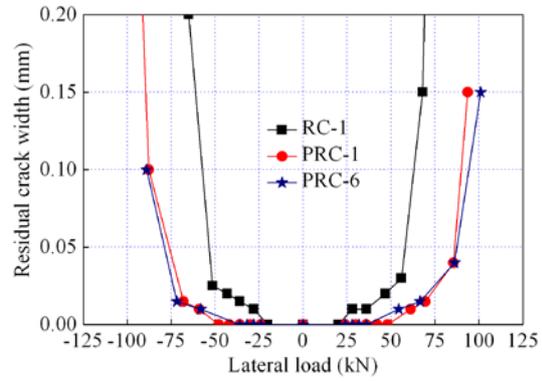
(c)



(d)



(e)



(f)

891

892

893

894

895

896

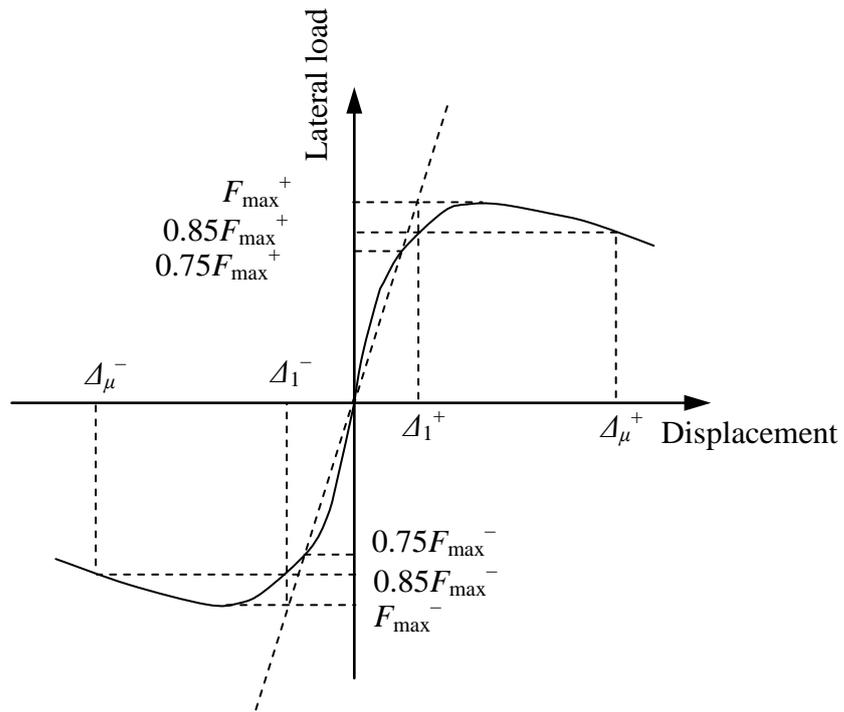
897 **Fig. 10** Residual concrete crack widths: **a** all the specimens; **b** RC-1, PRC-1 and PRC-2; **c** RC-1,

898 PRC-1 and PRC-3; **d** RC-1, PRC-1 and PRC-4; **e** RC-1, PRC-1 and PRC-5; **f** RC-1, PRC-1 and

899 PRC-6

900

901



**Fig. 11** Definition of the strength and ductility parameters

927

928

929

930

931

932

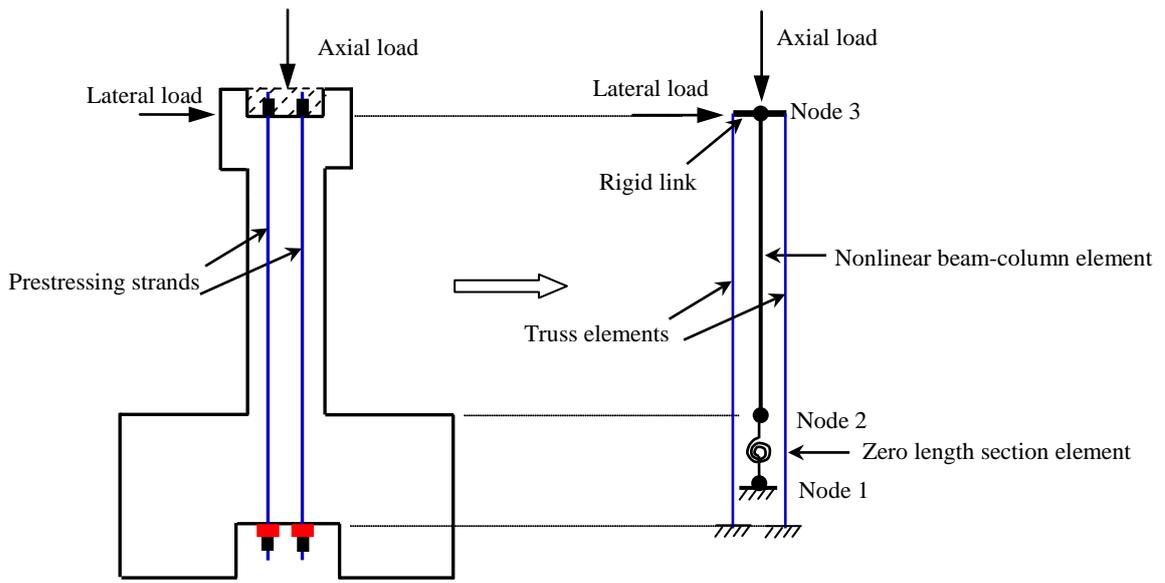
933

934

935

936

937



938 **Fig. 12** Numerical model of the specimens

939

940

941

942

943

944

945

946

947

948

949

950

951

952

953

954

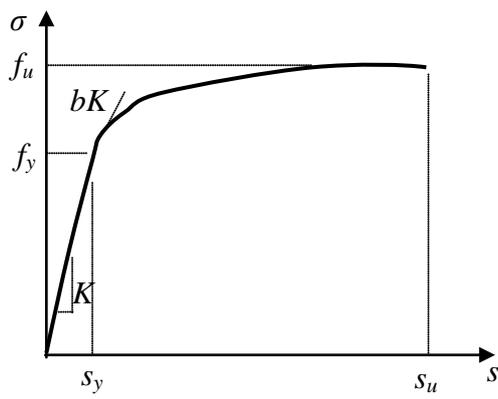
955

956

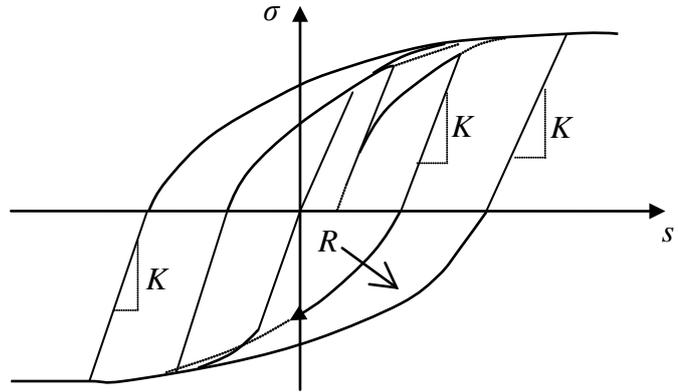
957

958

959



(a)



(b)

960

961 **Fig. 13** Bar stress versus loaded-end slip response model proposed by Zhao and Sritharan [20]: **a**  
962 under monotonic loading; **b** hysteretic response

963

964

965

966

967

968

969

970

971

972

973

974

975

976

977

978

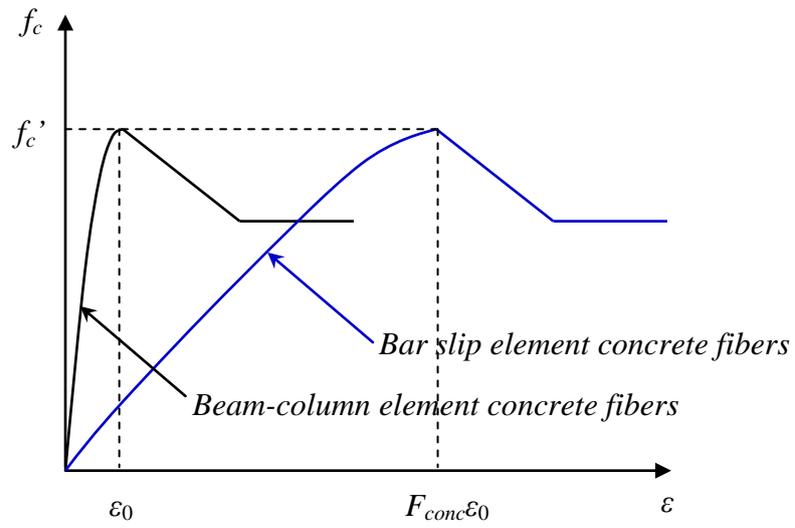
979

980

981

982

983



984 **Fig. 14** Stress strain relations for beam-column element and bar slip element concrete fibers

985

986

987

988

989

990

991

992

993

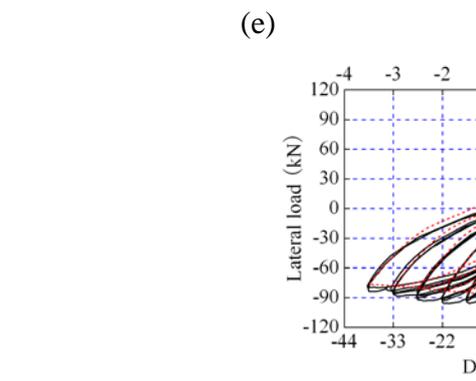
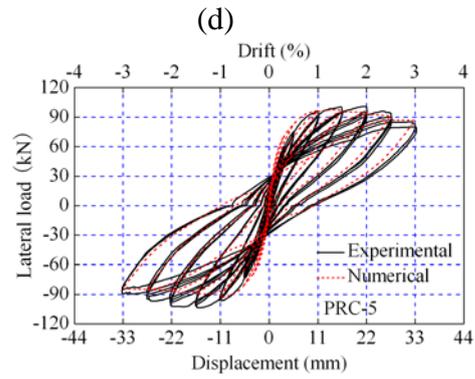
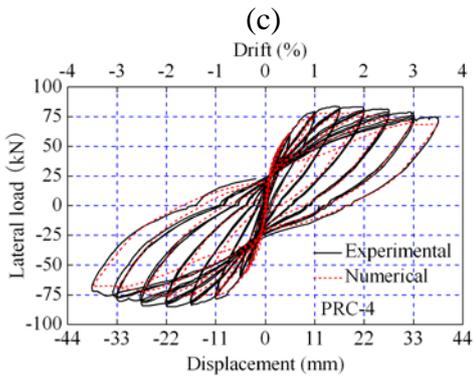
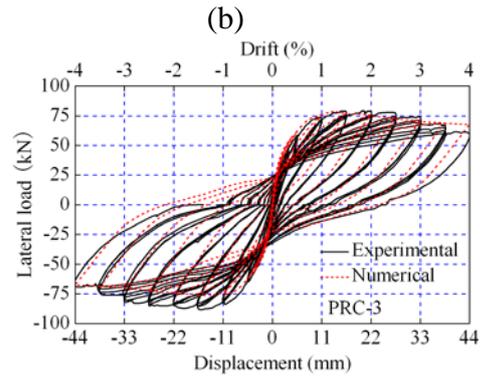
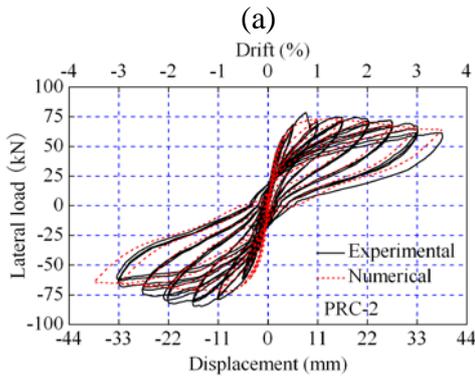
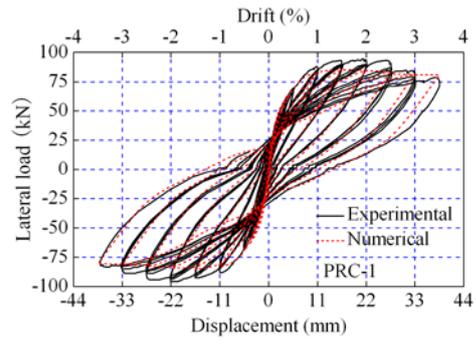
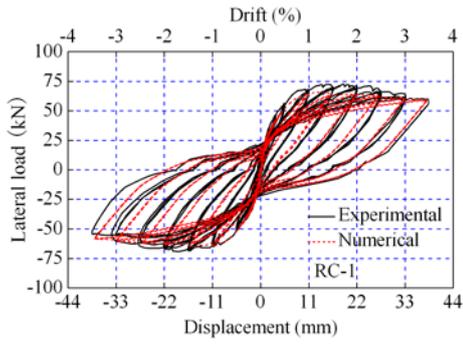
994

995

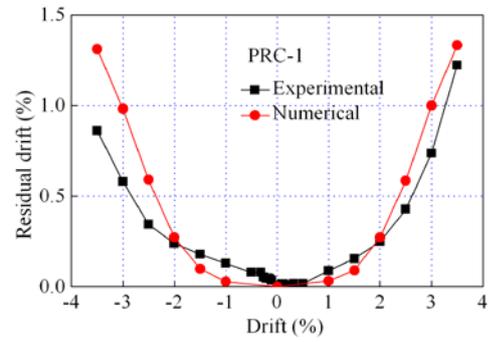
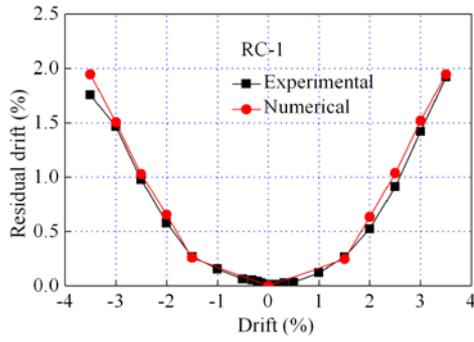
996

997

998

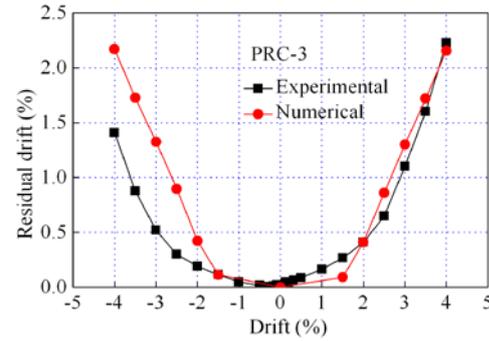
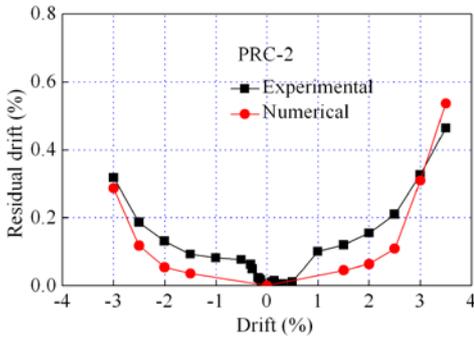


**Fig. 15** Experimental and numerical hysteretic curves: **a** RC-1; **b** PRC-1; **c** PRC-2; **d** PRC-3; **e** PRC-4; **f** PRC-5; **g** PRC-6



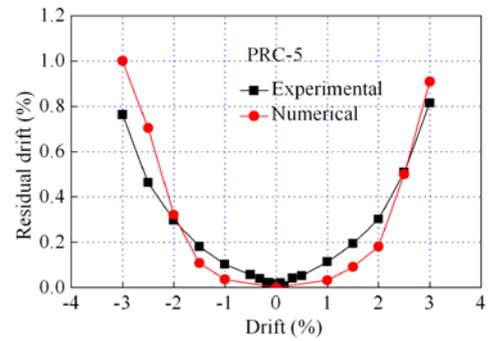
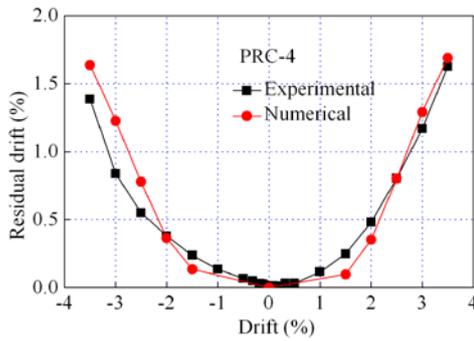
(a)

(b)



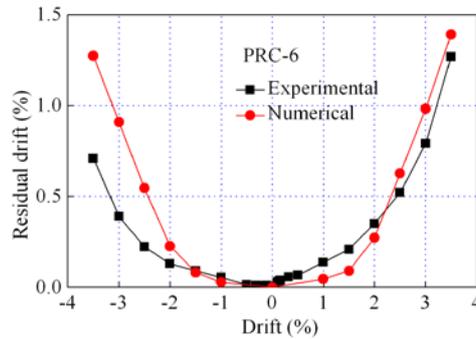
(c)

(d)



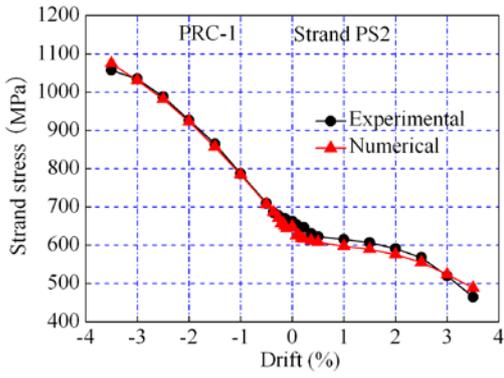
(e)

(f)

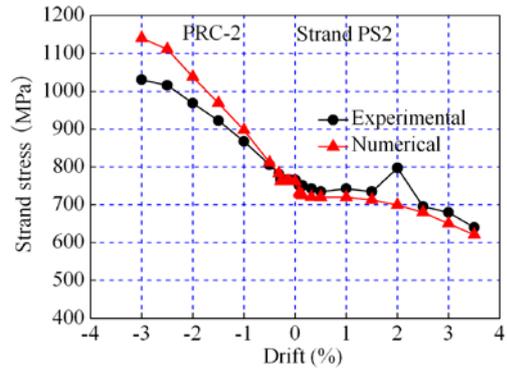


(g)

**Fig. 16** Experimental and numerical residual drifts: **a** RC-1; **b** PRC-1; **c** PRC-2; **d** PRC-3; **e** PRC-4; **f** PRC-5; **g** PRC-6



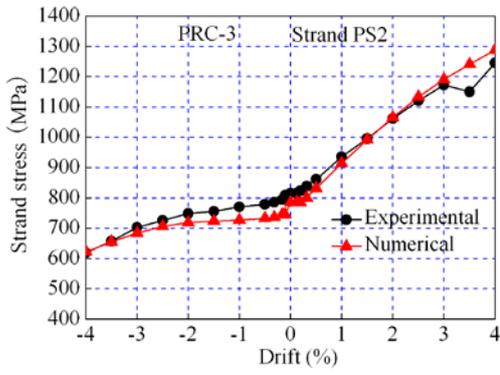
1021



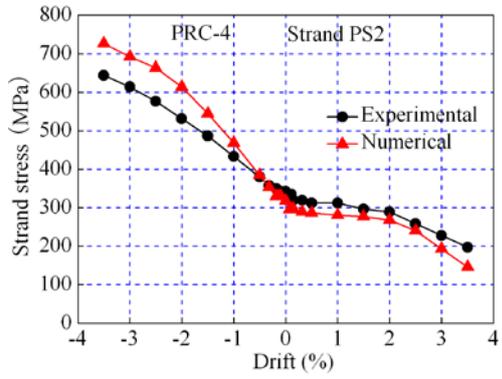
1022

(a)

(b)



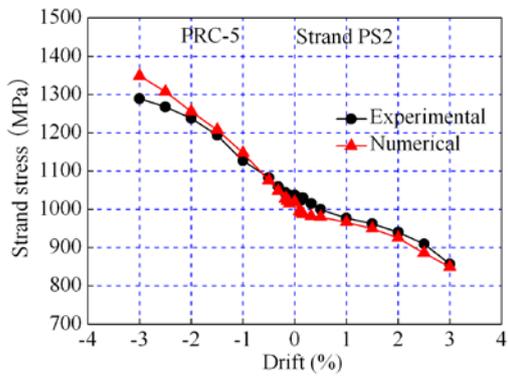
1023



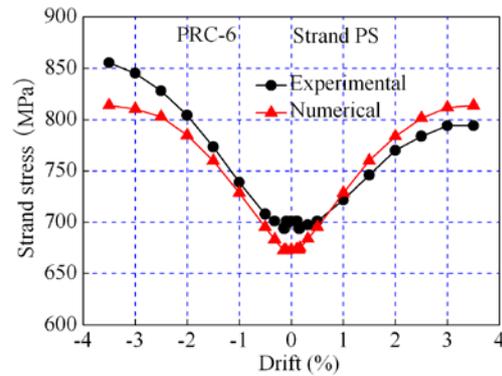
1024

(c)

(d)



1025



1026

(e)

(f)

1027 **Fig. 17** Experimental and numerical strand stress: **a** PRC-1; **b** PRC-2; **c** PRC-3; **d** PRC-4; **e** PRC-5;

1028 **f** PRC-6

1029

1030

1031

1032