

# Effect of Sintering Temperature on Microstructure and Strength Distribution of Alumina Coil Springs

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## Abstract

Ceramic coil springs are one of the most widely used components in mechanical systems under harsh chemical conditions and at high temperatures. In real applications of ceramic coil springs, knowing the effect of sintering temperature on their microstructure and strength distribution plays a crucial role. In this paper, the microstructure and strength distribution of alumina coil springs sintered at 1550°C, 1600°C and 1650°C are investigated. Strength data of alumina springs are fitted by the Weibull distribution and, according to the  $R^2$  value, the deviation from the Weibull distribution is discovered. It is shown that the Weibull distribution best fits the strength data of alumina springs sintered at 1600°C. The reasons for deviation from the Weibull distribution are discussed regarding the grain size, porosity, and  $R$ -curve behavior.

## Keywords

Alumina springs; Microstructure; Sintering temperature; Strength distribution

## Introduction

1 The advantageous characteristics of ceramics are often offset by concerns of their high  
2 manufacturing cost and brittleness or poor toughness. To overcome these barriers and develop  
3 advanced ceramics, major progress has been achieved over the past two decades, which results in an  
4 increase of ceramic structures in various industrial areas such as electronics, information and  
5 communication, energy and environment, and mechanical engineering<sup>1-3</sup>.

6 Many engineering components (e.g., bearing, wear plates, thermal plates, bushing, gears and  
7 springs) have benefited from advanced ceramics. Coil springs are nowadays produced in a wide  
8 range of materials such as chrome-silicon, high carbon steel, stainless steel, brass, zinc, and nickel  
9 alloy. However, these materials exhibit limited mechanical properties under severe service  
10 conditions. Therefore, ceramic springs are one of the most powerful candidates for applications in  
11 mechanical systems under harsh chemical and high temperature environments. In contrast to metals,  
12 ceramic springs are electrical insulators with high wear resistance, low density, good thermal  
13 resistance, and high temperature strength<sup>4,5</sup>. Moreover, an important advantage of using ceramics as  
14 springs is their lower energy dissipation in each loading-unloading cycle<sup>6,7</sup>. For example, ceramic  
15 springs can be used in magnetic resonance imaging scanners<sup>8</sup> and energy plants<sup>9</sup>.

16 There are three main methods for the production of ceramic springs: machining cylindrical  
17 compacts<sup>10</sup>, extrusion of sol-gel-derived pastes or polymer-ceramic mixtures<sup>11</sup> and low pressure  
18 injection molding (LPIM)<sup>4,5</sup>. Among these methods, LPIM provides ceramic springs with higher  
19 surface quality and lower cost. Krindges et al.<sup>4</sup> developed a simple LPIM method to mold helical  
20 springs. Barbieri et al.<sup>5</sup> produced alumina springs under three different sintering temperatures and  
21 investigated the effect of sintering temperatures on their mechanical properties such as porosity,  
22 spring constants and the Weibull parameters.

23 Compared to production of ceramic springs, there are only a few studies related to their reliability<sup>12-</sup>  
24 <sup>14</sup>. Nohut and Schneider<sup>12</sup> introduced a general formulation for the prediction of failure probability  
25 of ceramic springs with various mechanical properties and dimensions. Sato et al.<sup>13</sup> performed

1 compression tests with Si<sub>3</sub>N<sub>4</sub> coil springs and concluded that they obey Hooke's law and maintain  
2 the high strength until 1000°C. For a reliable use of ceramic coil springs, there is a need for the  
3 analysis of their microstructure and strength distribution in order to obtain the most suitable  
4 sintering temperature, at which springs can satisfy the required mechanical properties. The main  
5 aim of this study is to investigate the effect of sintering temperature on the strength distribution of  
6 alumina springs. The deviation of strength distributions from the Weibull distribution is explained  
7 regarding their microstructures and failure mechanisms (e.g., grain size, porosity, *R*-curve behavior  
8 etc.).  
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## 20 **Materials & Methods**

### 23 Sample and Experimental Procedure

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25 In the production of alumina springs, commercially available submicrometer-sized alumina (Al<sub>2</sub>O<sub>3</sub>)  
26 A-1000SG (Almatis Inc., Leetsdale, PA) was used as received. According to the supplier's data, this  
27 99.8% pure alumina has an average particle size of 0.4 μm. The mixture of alumina and binder for  
28 injection was prepared directly in the LPIM machine (Peltsman MIGL-33, Minneapolis, MN), with  
29 86 wt.% of alumina and 14 wt.% of wax based binder (~55 vol.%). The mixture was mixed for 20 h  
30 at 90°C before injection<sup>4, 5, 15, 16</sup>.  
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40 Ceramic springs were made by a brass mold lined with a fine polytetrafluoroethylene film. The  
41 brass mold was multi-parted to simplify the mechanical extraction of green ceramic springs after  
42 injection. The alumina/binder mixture was injected into the brass mold at 90°C and 400 kPa,  
43 keeping the pressure for 12 s. During injection, temperature of the mold was kept at 50°C<sup>4, 5</sup>.  
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50 The green ceramic parts were subjected to debinding immersed into an alumina powder bed (A-  
51 1000SG) up to 250°C<sup>4, 5</sup>. Then, the parts were fired to 1000°C in an electrical resistance furnace,  
52 and finally sintered at 1550°C, 1600°C or 1650°C for 2 hours in air (Lindberg/Blue M furnace -  
53 model BF51634PCOMC, Ashville, NC). To evaluate the maximum load that can be carried by  
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1 springs, compression tests were performed at room temperature in a mechanical testing machine  
2 (EMIC DL3000, PR, Brazil)<sup>5</sup>, as shown in Fig. 1.  
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### 6 **Figure 1**

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10 To avoid testing samples with macrovoids, only ceramic springs with green densities higher than  
11 2.64 g/cm<sup>3</sup> were sintered and used in compression tests. For helical springs subjected to a  
12 longitudinal, uniaxial compressive force  $F$ , torsional and transverse shear stresses occur. The  
13 maximum torsional shear stress occurring at the inner part of treads can be calculated as follows<sup>5</sup>  
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$$20 \tau_{\max} = \frac{2F(12D^2 - 19dD - d^2)}{3\pi d^3(D - 2d)} \quad (1)$$

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25 where  $D$  is the mean spring diameter and  $d$  is the coil diameter. The transverse shear stress due to  
26 bending the wire is given as<sup>6,12</sup>:  
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$$30 \tau_d = \frac{4F}{\pi d^2} \quad (2)$$

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34 In the limit of  $D/d \gg 1$ , the transverse shear stress can be neglected<sup>12,13</sup>. In this study, Eq. (1) was  
35 used to determine the strength of ceramic springs.  
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### 41 Microstructural Analysis

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44 The grain boundary was revealed by the thermal treatment of pre-polished sections of helical  
45 alumina springs at 1400°C for 30 min. Images were obtained using a SSX-550 scanning electron  
46 microscope (Shimadzu, Japan) with carbon coated samples. Measurements of grain sizes were  
47 carried out by using the lineal intercept procedure according to ASTM E112<sup>17</sup>.  
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### 56 Weibull Failure Statistics

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59 Failure of ceramics initiates from pre-existing flaws, and thus their strength depends on the size of  
60 the most critical flaw, which varies from one specimen to another. Therefore, the variation of  
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position, orientation and size of a critical flaw causes scattering of strength in advanced ceramics.

Therefore, a probability approach should be used in the design of ceramic springs.

The Weibull distribution<sup>18,19</sup> is most widely used in the statistical analysis of strength and design of ceramics. The failure probability of a ceramic component due to volume flaws  $P_{F,V}$  subjected to a multiaxial stress can be written as<sup>20,21</sup>

$$P_{F,V}(\sigma^*, V_{eff}) = 1 - \exp\left[-\frac{V_{eff}}{V_0} \left(\frac{\sigma^*}{\sigma_0}\right)^m\right] \quad (3)$$

where  $\sigma^*$  is the reference stress ( $\sigma^* = \tau_{max}$  for ceramic springs),  $V_{eff}$  can be described as the volume of a rod under tensile tests with the same stress distribution,  $V_0$  is the unit volume containing the average number of cracks,  $\sigma$  is the uniaxial applied stress,  $m$  is the Weibull modulus which describes the scatter of strength, and  $\sigma_0$  is the characteristic strength at which the failure probability is 63.2 % for a specimen with a volume of  $V_{eff} = V_0$ . The maximum likelihood estimators of  $\sigma_0$  and  $m$ , which are obtained by maximizing its log-likelihood function, are given as<sup>22</sup>

$$\sigma_0 = \left\{ \frac{1}{n} \sum_{i=1}^n \sigma_i^m \right\}^{1/m} \quad \text{and} \quad \frac{1}{m} = \frac{\sum_{i=1}^n [\sigma_i^m \ln(\sigma_i)]}{\sum_{i=1}^n \sigma_i^m} - \frac{1}{n} \sum_{i=1}^n \ln(\sigma_i) \quad (4)$$

## Results & Discussion

During the sintering stage, ceramic springs were internally supported by an alumina cylinder to avoid distortion during shrinkage<sup>5</sup>. Typical springs after sintering are shown in Fig. 2. No cracks were observed after debinding and sintering and three sets of ceramic springs with well-defined shapes were obtained.

### Figure 2

In Fig. 3, pictures of some broken alumina coil springs are shown. In Fig. 3(a), the crack plane is illustrated by using a dashed line and its angle is approximately equal to 45°. Nohut et al.<sup>21</sup>

1 investigated the angle of crack propagation in alumina ceramics by using tension-torsion tests. They  
2 reported that a normal stress criterion is in well agreement with experimental and numerical results  
3 and according to the normal stress criterion, the crack angle is equal to 45° when the specimen is  
4 loaded under pure torsion.  
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### 7 8 **Figure 3** 9

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12 During the loading of ceramic springs, the effect of bending stress can be neglected compared to  
13 torsional stress; therefore crack propagates along an angle of 45°, as shown in Fig. 3(a). This result  
14 shows that, under a multiaxial stress, alumina springs fail following the normal stress criterion.  
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18 In Table 1, the relevant parameters are given for springs sintered at 1550°C, 1600°C and 1650°C,  
19 including the number of samples  $N$ , the mean values of wire diameter  $d$  and spring diameter  $D$ , and  
20 the Weibull parameters calculated by the maximum likelihood method<sup>5</sup>.  
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### 30 **Table 1** 31

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34 As Barbieri et al.<sup>5</sup> reported, the Weibull modulus  $m$  and the characteristic strength  $\sigma_0$  increase as the  
35 increase of sintering temperature. In the calculation of fracture strength of ceramics springs by Eq.  
36 (1), the mean values of wire and spring diameters in Table 1 were used. In Fig. 4, the Weibull plot  
37 of strength of alumina springs sintered at different temperatures and the coefficient of determination  
38  $R^2$  values are given. Here,  $R^2$  provides information about the goodness of fit of a model, which is a  
39 statistical measure of how well the regression line approximates real data. An  $R^2$  of 1.0 indicates  
40 that the regression line perfectly fits the data. As  $R^2$  decreases, the fitting quality of the regression  
41 line decreases. Comparison of  $R^2$  values in Fig. 4 reveals that the Weibull distribution best fits the  
42 strength data of springs sintered at 1600°C. In Fig. 4(a-b), deviations (mostly at low strength  
43 values) from the Weibull line are observed for samples sintered at 1550°C and 1650°C.  
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#### Figure 4

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3 Scanning electron microscopy images in Fig. 5 reveal the microstructure of alumina springs, which  
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5 were obtained by secondary electrons.  
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#### Figure 5

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12 The porosity, measured by Barbieri et al.<sup>5</sup> on the basis of the Archimedes' method, and the average  
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14 grain size of alumina springs are given in Table 2. Measurements of the average grain size were  
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16 performed on scanning electron microscopy images by using the lineal intercept procedure<sup>17</sup>.  
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#### Table 2

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32 Alumina springs sintered at 1550°C have the highest porosity. As is well known, there are two main  
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34 prerequisites for a Weibull distribution: (i) structure fails if one single flaw becomes critical (i.e.,  
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36 the weakest link hypothesis) and (ii) flaws do not interact. Thus, in most cases, the Weibull  
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38 distribution can not be applied to porous materials<sup>23, 24</sup>. A group of pores as well as their interaction  
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40 would affect the final fracture rather than only the largest one as the weakest-link model  
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42 postulated<sup>25</sup>. The existence of a high ratio of pores (volume flaws) causes multiple flaw populations.  
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44 Each individual flaw population has its typical size distribution and leads to a distribution with  
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46 different Weibull parameters. As a result, the strength distribution resulting from different flaw  
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48 populations will overlap, which cannot be modeled by one single tail of flaw size distribution.  
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$$P=1-\exp\left[-\left(\frac{\sigma}{\sigma_{0,1}}\right)^{m_1}-\left(\frac{\sigma}{\sigma_{0,2}}\right)^{m_2}\right] \quad (5)$$

where  $\sigma_{0,1}$  and  $m_1$  are the Weibull parameters of flaw type I (e.g., volume flaws) and  $\sigma_{0,2}$  and  $m_2$  are the Weibull parameters of flaw type II (e.g., surface flaws). Fig. 6 shows the Weibull plot of strength data of alumina springs sintered at 1550°C.

### Figure 6

As shown in Fig. 6, the dashed line is the original Weibull plot and solid lines represent the Weibull plots with different flaw populations. It is evident that there are three types of Weibull distributions. Two kinks occur in the linear Weibull plot due to the multimodal flaw or the high porosity.

### Figure 7

In Fig. 7, the pictures of crack propagation planes of broken alumina springs, sintered at 1550°C, are shown. Type-I represents the volume flaw and type-II represents the surface flaw. It is seen that volume flaws, surface flaws or both may be the main reason of failure and strength determinant for alumina springs sintered at 1550°C. As a result, it is not reliable to characterize the strength of these springs by a single flaw size distribution. This is the main reason for the deviation of strength distribution of alumina springs sintered at 1550°C from the Weibull line.

In Fig. 4(c), deviation from the Weibull line at low strength values is observed. As seen in Table 2, the average grain size increases as the increase of sintering temperature. There are numerous investigations which show the effect of the average grain size on the *R*-curve behavior (i.e., an increase of fracture resistance with the crack propagation) of alumina<sup>27-31</sup>. Wieninger et al.<sup>32</sup> measured crack resistance curves of three pure alumina ceramics with different grain sizes, in which flat crack resistance curves were reported for fine-grained alumina and steeply rising crack



1 resistance curves for coarse grained alumina. This shows that as the grain size increases ( $> 2-3 \mu\text{m}$ ),  
2 the  $R$ -curve effect increases. As a result, the  $R$ -curve effect can be observed in alumina springs  
3 sintered at  $1650^\circ\text{C}$ .  
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5 According to linear elastic fracture mechanics, the stress intensity factor increases with increasing  
6 applied load until a critical value of stress intensity factor  $K_I$  is reached, at which a crack is still in  
7 equilibrium and above which the unstable crack propagation takes place. Such a critical value is  
8 referred to as fracture toughness  $K_{IC}$ . When there is an  $R$ -curve effect, the crack growth resistance  
9 increases with the crack extension and the crack propagation behavior is no more characterized by a  
10 single value  $K_{IC}$  but with  $K_{IR}$ , which increases from  $K_{I0}$ , an onset value of crack growth (crack-tip  
11 toughness).  
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13 Owing to the existence of short (small) cracks in a material with the  $R$ -curve behavior, the unstable  
14 crack propagation occurs since the condition  $K_I > K_{I0}$  is always fulfilled. As a result, there is no  
15 stable crack propagation. When a long crack exists in a material, as the condition  $K_I = K_{I0}$  is  
16 satisfied, the crack starts to propagate in a stable manner. The unstable crack propagation occurs at a  
17  $K_I$  value higher than  $K_{I0}$  after the stable crack growth. Therefore, it is obvious that the  $R$ -curve effect  
18 influences the strength of components with large cracks, but has no important effect on specimens  
19 with small defects<sup>26</sup>. The increasing crack growth resistance leads to an increase in the Weibull  
20 modulus  $m$ <sup>24,26</sup>. This explains the increase of the Weibull modulus with increasing sintering  
21 temperatures (see Table 1). It is concluded that, therefore, if a series of strength measurements are  
22 performed, specimens with large cracks (low strength) have a Weibull modulus higher than that  
23 with small cracks (high strength).  
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## 52 **Figure 8**

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57 In Fig. 8, the Weibull plot of measured strengths of alumina springs sintered at  $1650^\circ\text{C}$  is given. The  
58 dashed lines indicate the original population and the solid line shows the effect of  $R$ -curve behavior.  
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1 For low strength data (failure due to large cracks), the Weibull modulus is higher than that for high  
2 strength data (failure due to small cracks). This shows the effect of *R*-curve behavior on strength  
3 distribution. This is the main reason for deviation of strength data of alumina springs sintered at  
4 1650°C from the Weibull distribution.  
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## 10 **Conclusions**

11 In this paper, the effect of sintering temperature on the microstructure and strength distribution of  
12 alumina coil springs was investigated. It is shown that the average grain size increases with the  
13 increase of sintering temperature. For the measured strengths of alumina springs sintered at 1550°C  
14 and 1650 °C, deviations from the Weibull distribution were observed. Due to the high porosity in  
15 alumina springs sintered at 1550°C, there are multimodal flaw populations (volume and surface  
16 flaws), which result in deviations of the strength distribution from the Weibull plot. According to  
17 grain size measurements, alumina springs sintered at 1650°C have the largest average grain size. As  
18 the grain size increases, the *R*-curve effect appears which results in an increase of the Weibull  
19 modulus. As a conclusion, although the Weibull modulus is the highest (lowest scatter of strength)  
20 at the sintering temperature of 1650°C, the strength data for alumina springs sintered at 1600°C is  
21 best fitted by the Weibull distribution and the strength predicted by using the Weibull function is  
22 more reliable than that for springs sintered at 1550°C and 1650°C.  
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## Figure Captions

- 1 **Figure 1** Compression testing machine and alumina spring under testing.  
2  
3 **Figure 2** Alumina springs after the sintering stage.  
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5 **Figure 3** Typical morphology of broken alumina springs. (a) The spring was broken into two  
6 parts and (b) the spring was broken into three parts.  
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10 **Figure 4** Weibull plots of strength for alumina springs sintered at (a) 1550°C, (b) 1600°C, and  
11 (c) 1650°C.  
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15 **Figure 5** Scanning electron microscopy images showing the microstructures of alumina  
16 springs sintered at (a) 1550°C, (b) 1600°C and (c) 1650°C.  
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20 **Figure 6** The Weibull plot of measured strengths of alumina springs sintered at 1550°C. The  
21 dashed line indicates the original population and solid lines indicate different flaw  
22 populations.  
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27 **Figure 7** Pictures of alumina springs which fractured due to volume flaws (type-I), surface  
28 flaws (type-II) and mixed flaws (type-I and type-II).  
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32 **Figure 8** The Weibull strength plot of alumina springs sintered at 1650°C. The dashed line  
33 indicates the original population and solid lines indicate the flaw population with an  
34 *R*-curve.  
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## Tables

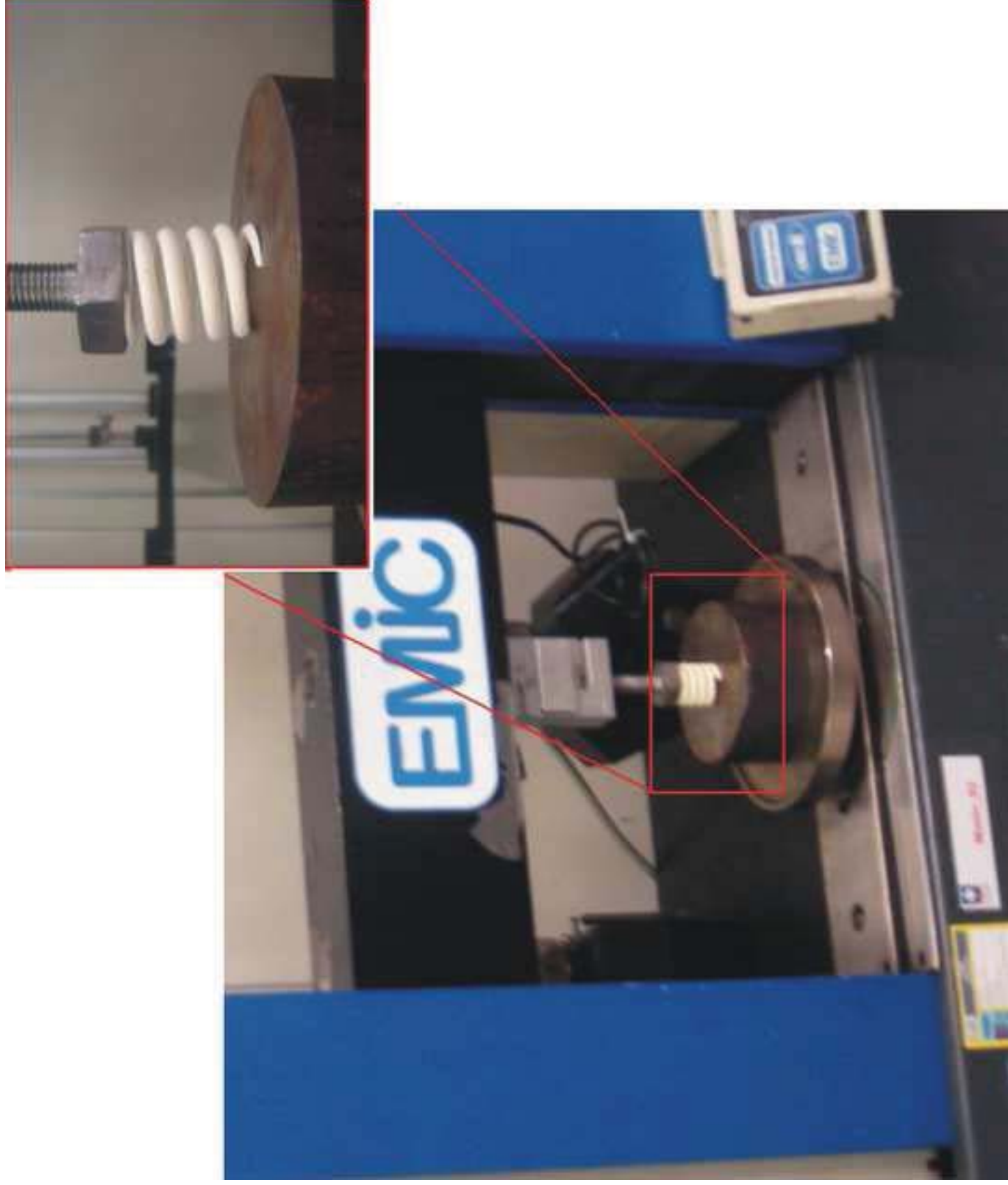
**Table 1.** Number and geometrical dimensions of spring samples at different sintering temperatures and parameters fitted by the Weibull distribution.

Sintering Temperature [°C]	$N$	$d$ [mm]	$D$ [mm]	$m$	$\sigma_0$ [MPa]
1550	41	4.06	23.15	1.88	39.03
1600	49	4.02	23.08	2.04	50.65
1650	47	4.04	22.91	2.35	52.08

**Table 2.** Porosity<sup>5</sup> and average grain size of alumina springs.

Sintering Temperature [°C]	Porosity, [vol. %]	Average Grain Size, [ $\mu\text{m}$ ]
1550	6	1.5
1600	3.4	2.1
1650	2.5	5.4

Figure 1  
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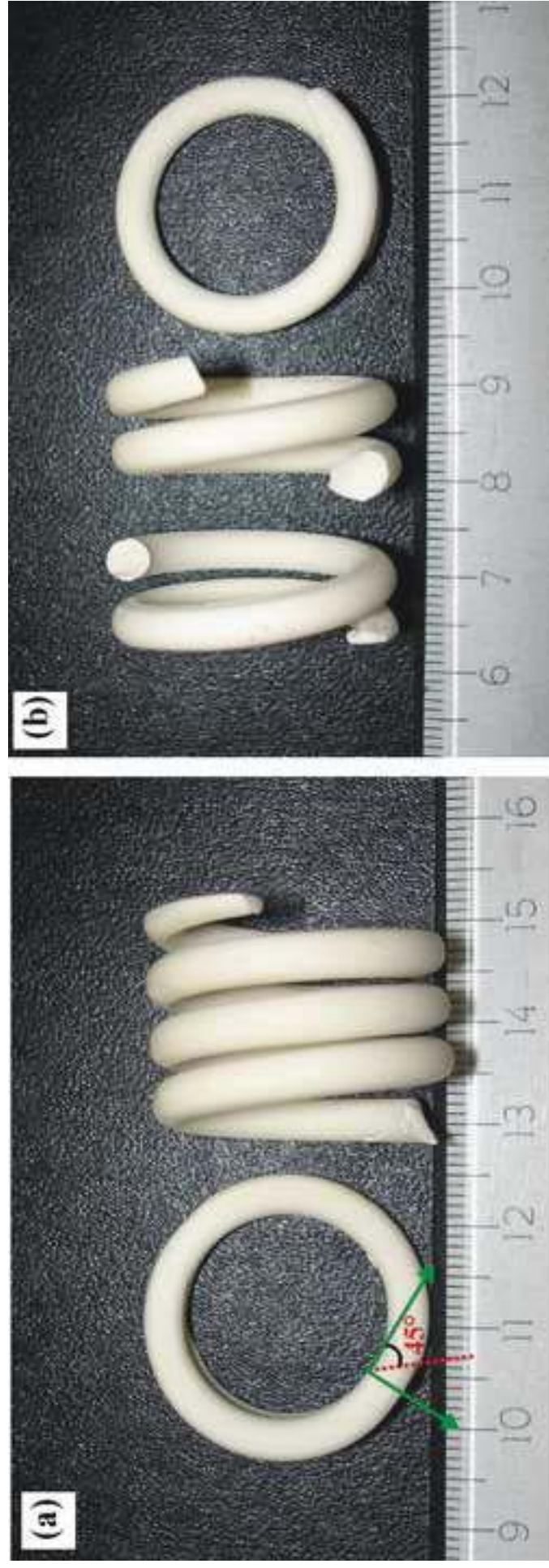
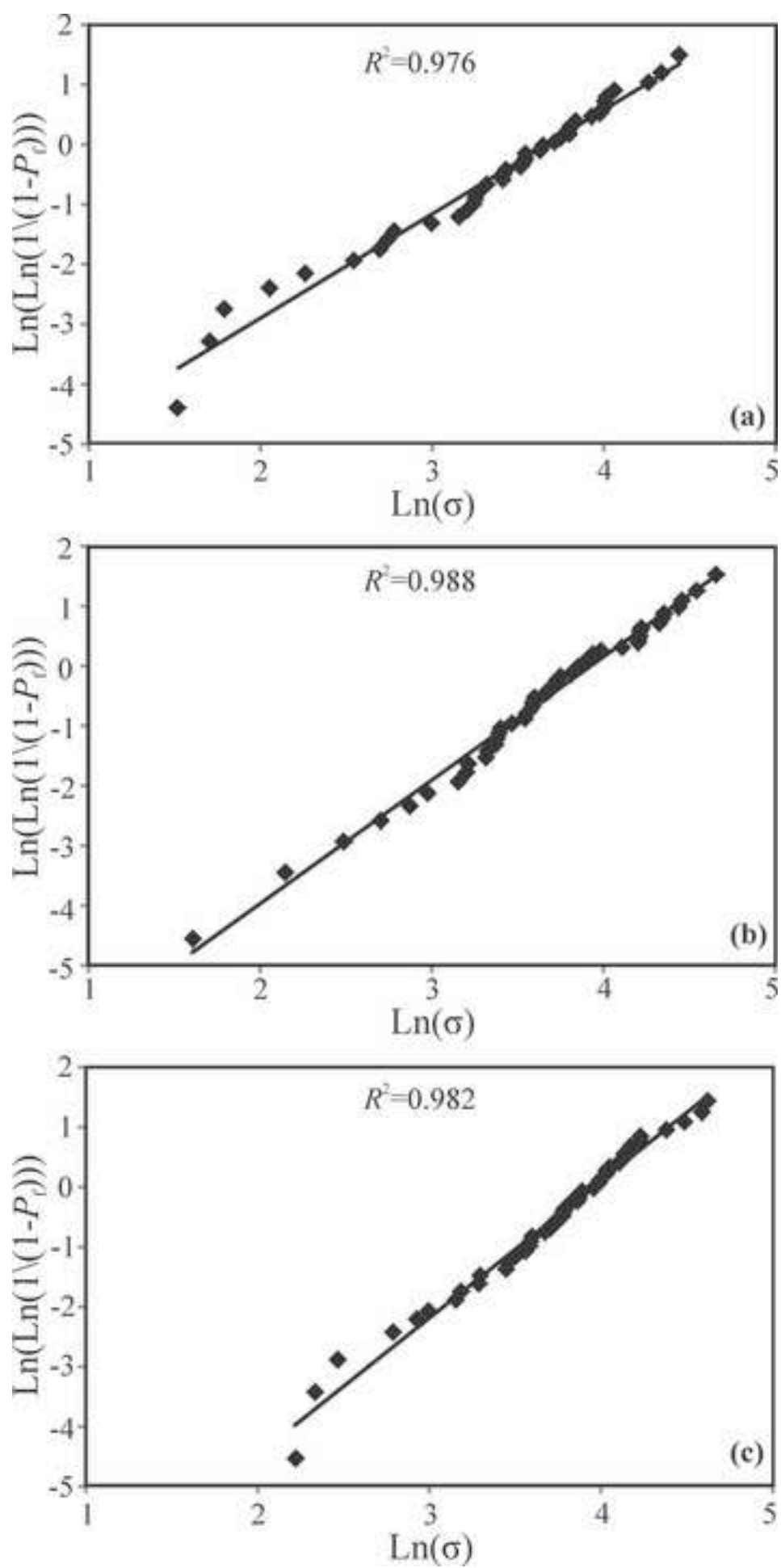
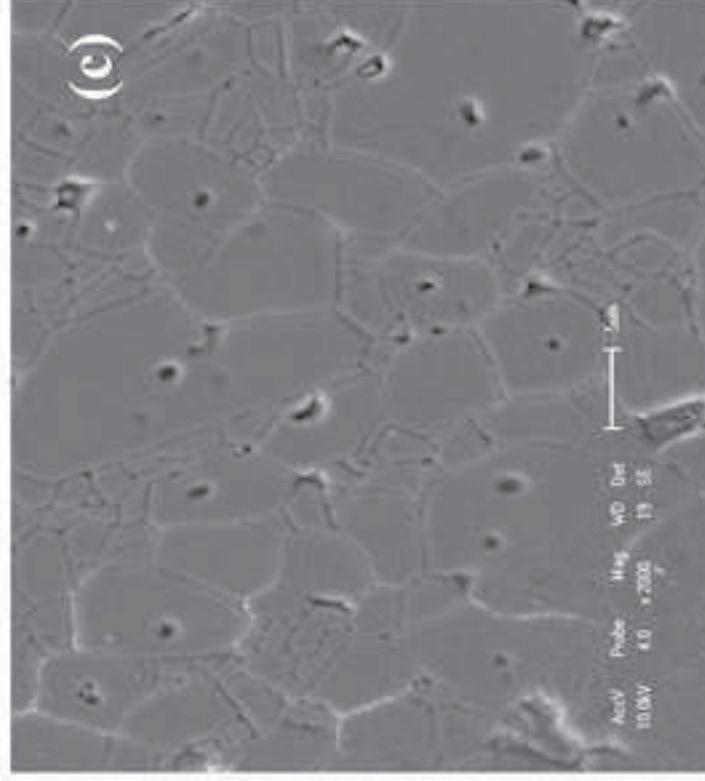
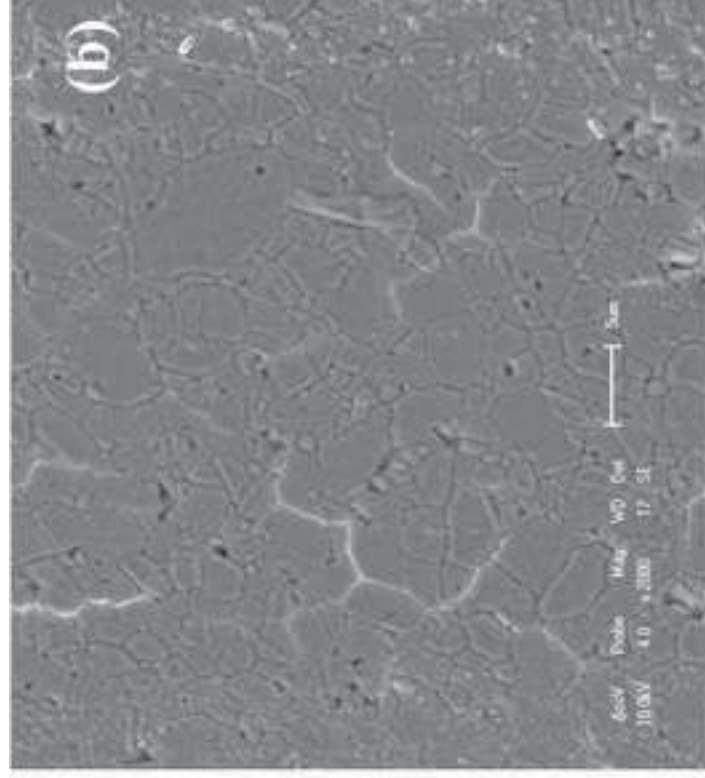
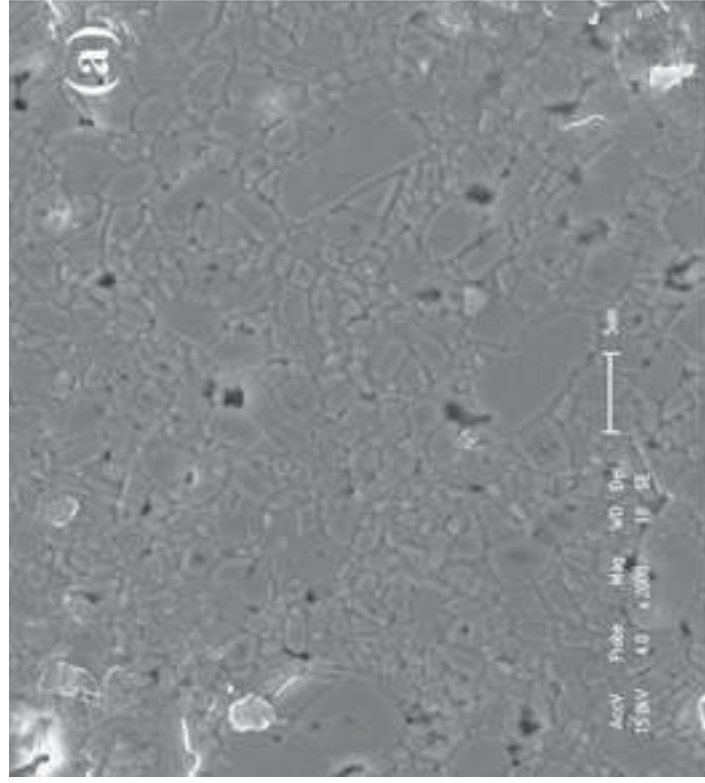


Figure 4

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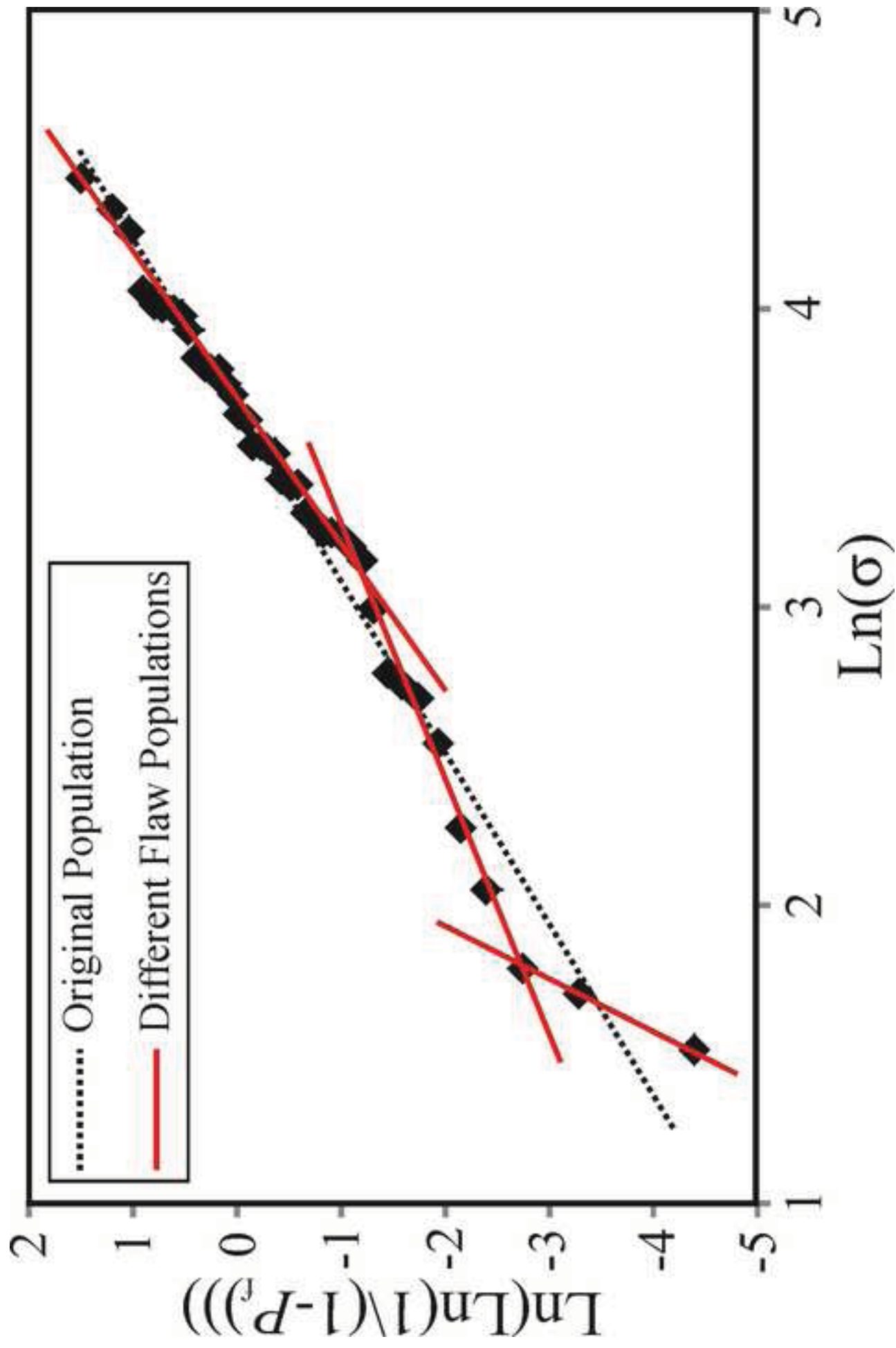


Figure 6  
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