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Impacts of Hysteresis and Magnetic Couplings on the Stability Domain of Ferroresonance in Asymmetric Three-Phase Three-Leg Transformers

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Abstract—This paper investigates the stability domain of ferroresonance in asymmetric three-phase three-leg transformers considering magnetic couplings and hysteresis effects of the core. A newly developed and accurate time-domain transformer model capable of simulating dynamic and transient operating conditions is implemented in this study. The model is based on electromagnetic circuit theory and considers dynamic hysteresis effects (major and minor loops) as well as core topology, asymmetry, and magnetic flux cross-coupling interactions of the core legs. Unbalanced switching with series and shunt capacitances, which is known to increase the risk of ferroresonance, is studied with the developed model. The validity of the model under ferroresonant conditions is confirmed by comparisons with extensive experimental data. The main contribution is a new analysis of (a)symmetric three-phase transformer ferroresonance behavior with an accurate core model capable of predicting ferroresonance modes.

Index Terms—Ferroresonance, hysteresis, nonlinear and three-phase transformer model.

I. INTRODUCTION

MANY investigations of ferroresonance phenomena in power and instrument transformers have been performed, spanning nearly a century of accumulated research [1], [2]. Much progress has been made in the modeling and understanding of single-phase transformer ferroresonance. However, one of the weakest areas in ferroresonance research remains in the modeling of (a)symmetric three-phase transformers.

A. Description of Ferroresonance Problem

Ferroresonance is a complex oscillatory interaction of energy exchanged between nonlinear magnetizing inductances of ferromagnetic cores and system capacitances (e.g., series compensated lines) [1], [3]. These oscillations manifest as large distorted voltages and currents potentially leading to excessive heating and insulation failure in transformers as well as significant disruptions to power networks [4]–[11].

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Unlike ordinary *RLC* circuit resonance, oscillations involving nonlinear magnetizing inductances can exhibit multiple modes with no definite resonant frequency. These modes typically come in four types. The fundamental mode oscillates at the system frequency f and usually contains harmonics. The subharmonic mode is periodic and oscillates at $1/n$ multiples of the system frequency (f/n). Quasi-periodic modes exhibit irregular patterns of periodicity due to incommensurable frequencies $nf_1 + mf_2$, where f_1/f_2 is irrational with integer n and m . These modes are strictly nonperiodic and produce a discontinuous frequency spectrum. Chaotic modes exhibit no periodicity and produce a continuous frequency spectrum resembling broadband noise. Sudden jumps (bifurcations) to different modes are also possible due to gradual system variations and perturbations (e.g., switching transients) [3].

B. Historical Review of Ferroresonance Research

Ferroresonance research has its origins in ordinary transformer resonance studies performed as early as 1907 [12]. It was not until 1920 that the vernacular “ferroresonance” was first documented by Boucherot [13] describing the unusual co-existing operating points in a series resistor, nonlinear inductor and capacitor circuit. Much early experience in ferroresonance was gained through extensive field observations when digital computer models and analytical methods were in their infancy. Notable examples are the studies conducted in [14]–[17] on distribution systems exhibiting ferroresonance with voltage regulation capacitors, and the triggering of ferroresonance in three-phase systems from single-pole switching.

Analytical approaches based on simple graphical solutions were proposed early on [18], [19] to predict particular bifurcations in single-phase ferroresonant circuits. It was not until the late 1980s that significant breakthroughs were made in nonlinear transformer models and analytical techniques. This was largely driven by advancements in computing power and the foundation of nonlinear dynamics and chaos theory, which Kiény [20] and Mork and Stuehm [21] first proposed as a suitable framework for ferroresonance study. Henceforth, new useful analytical approaches have emerged (e.g., bifurcation, phase-plane and Poincaré techniques [22]–[24]) which are now the benchmark for modern ferroresonance analyses.

Toward the end of the 20th century, the study area has branched into four main directions: 1) practical system level case studies [6], [25], [26]; 2) ferroresonance identification methods [27], [28]; 3) development of ferroresonance mitigation

approaches [29]–[33]; and most prominently, 4) the improvement of analytical techniques and the modeling of electromagnetic transients in transformers, which is the main contribution of this paper.

C. Modeling of Three-Phase Ferroresonance Phenomena

There have been very few attempts at studying three-phase transformers under ferroresonance conditions. The work given in [34]–[36] implement models considering core topology and employ single-value nonlinear functions for core effects. Analytical and numerical approaches are developed in [37]–[39] to calculate ferroresonance modes. However, these approaches do not consider dynamic hysteresis effects with core asymmetry and associated magnetic leg couplings. Furthermore, these models lack experimental validation.

D. New Ferroresonance Studies With Hysteretic Core Models

A new class of transformer models is emerging with the inclusion of hysteresis nonlinearities into core representations. Recent studies have shown that accurate representation of ferromagnetic iron-core nonlinearities (e.g., saturation, hysteresis, and eddy currents) is important in ferroresonance. Hysteresis formation significantly impacts the stability domain of ferroresonance, especially for subharmonic and chaotic modes in single-phase transformer core models [40], [41]. The common approach of approximating core nonlinearities with nonhysteretic single-value functions (e.g., piece-wise, exponential and polynomials) has proven to be inadequate for ferroresonance studies in single-phase transformers. The impacts of dynamic hysteresis nonlinearities (e.g., major and minor loops) and magnetically coupled asymmetric legs on three-phase transformer ferroresonance have not been explored.

For the first time, this paper studies ferroresonance in asymmetric three-phase transformers using a newly developed and detailed nonlinear electromagnetic circuit model for multi-leg transformer cores. The model is implemented in time domain and considers core asymmetry and topology, magnetic couplings of the legs, as well as nonlinearities in the iron-core structure. Accurate dynamic hysteresis nonlinearities including major and minor loop effects are implemented for each magnetically coupled core-leg. Experimental validation tests have been performed to demonstrate the models high accuracy in duplicating ferroresonance behavior in three-phase transformers.

II. THREE-PHASE TRANSFORMER MODELING APPROACH

There has been significant progress in the understanding and modeling of single-phase transformer ferroresonance [23], [42]–[45]. However, exact behavior of three-phase transformers under ferroresonance conditions is largely unexplored due to the lack of adequate core models. These models present significant challenges due to the magnetic circuits of different core topologies (e.g., three-leg, five-leg) and associated magnetic couplings in the iron-core structure. Moreover, a three-phase transformer core model cannot be simplified to three single-phase transformers. Each branch of the three-phase core structure has unique

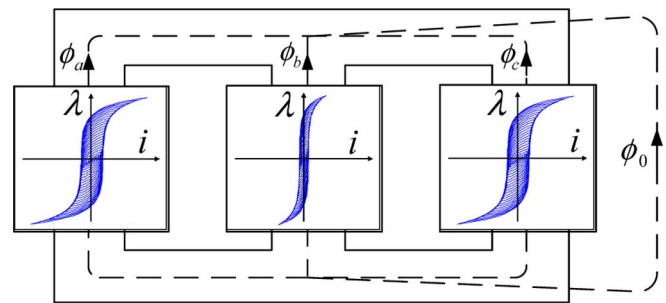


Fig. 1. Asymmetric three-phase three-leg transformer core.

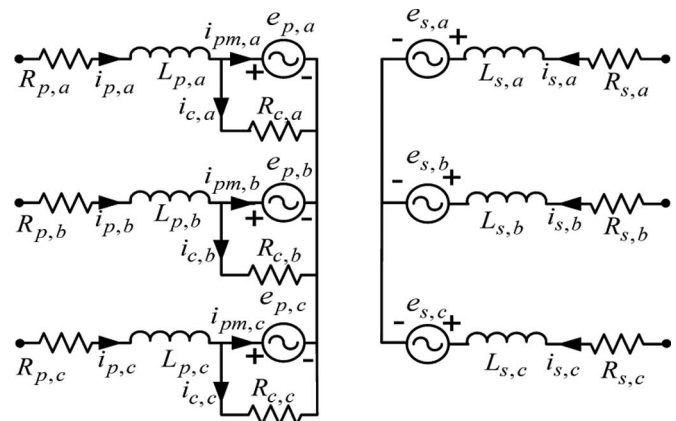


Fig. 2. Three-phase transformer electric equivalent circuit (wye/wye).

nonlinear leg and yoke reluctance characteristics due to varying core geometries and flux path lengths. This is referred to as an asymmetric three-phase transformer which has not been studied under ferroresonance conditions.

In this paper, a newly developed three-phase transformer model [46] is implemented and its performance under ferroresonance conditions is examined. The most significant feature of the developed model is the inclusion of detailed hysteresis core models considering major and minor loop effects combined with an asymmetric three-leg electromagnetic structure (see Fig. 1).

A. Transformer Electromagnetic Circuits

The duality principle is applied in the development of coupled electric and magnetic equivalent circuit models where fluxes are computed as currents, magnetomotive forces (MMFs) as voltages and reluctances as resistances [2], [47]–[49]. The electric circuit represents the ohmic losses in the windings as well as leakage flux inductances and eddy-current core losses. The electric couplings in the phases due to winding connections (e.g., wye, delta) are accounted for in the electric circuit (see Fig. 2).

The magnetic circuit is necessary for modeling the different core topologies, multiple flux paths and corresponding couplings in the magnetic legs (see Fig. 3). Each magnetic leg uses an expanded nonlinear core model to represent dynamic hysteresis nonlinearities in each leg. In this way, the hysteresis functions in each core leg can be individually adjusted to represent core asymmetry in the magnetic circuit. The governing electric and magnetic circuit relationships based on Kirchoff's

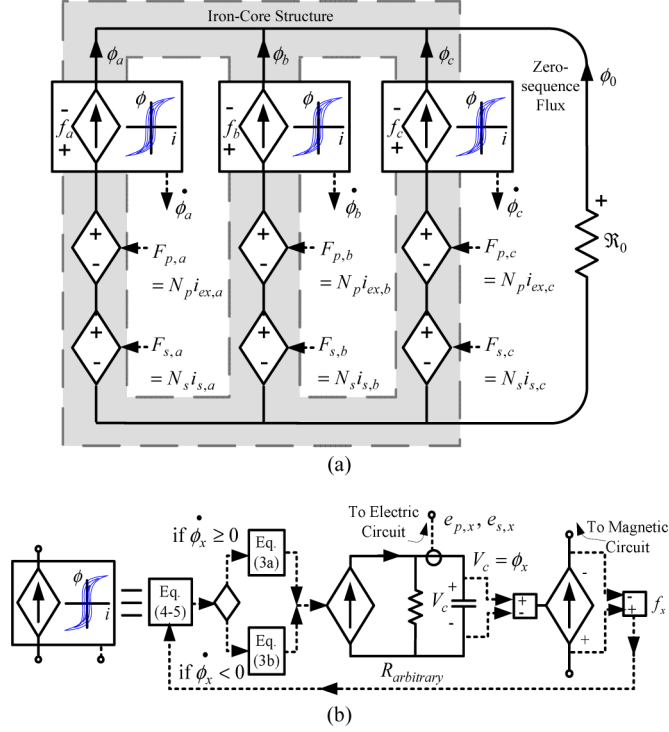


Fig. 3 (a) Three-phase three-leg transformer magnetic equivalent circuit and (b) expanded view of hysteresis subcircuit for modeling each core leg.

voltage and current laws are

$$\begin{aligned} v_{p,x}(t) &= R_{p,x} i_{p,x}(t) + L_{p,x} \frac{di_{p,x}(t)}{dt} + \frac{d\lambda_{p,x}(t)}{dt} \\ v_{s,x}(t) &= R_{s,x} i_{s,x}(t) + L_{s,x} \frac{di_{s,x}(t)}{dt} + \frac{d\lambda_{s,x}(t)}{dt} \end{aligned} \quad (1)$$

$$\phi_a + \phi_b + \phi_c + \phi_0 = 0 \quad (2)$$

where the respective primary/secondary terminal voltages, winding currents, and flux linkages for each phase x are $v_{p,x}$, $v_{s,x}$, $i_{p,x}$, $i_{s,x}$, $\lambda_{p,x}$, and $\lambda_{s,x}$. The primary/secondary phase winding resistances and inductances are $R_{p,x}$, $R_{s,x}$, $L_{p,x}$, and $L_{s,x}$, respectively. The magnetic circuit fluxes in each leg are ϕ_a , ϕ_b , and ϕ_c with zero-sequence leakage flux ϕ_0 .

B. Magnetic Hysteresis Core Models

The ferroresonance phenomenon is very much dependent on the complex magnetization processes of ferromagnetic iron-core structures. Therefore, accurate core models for true hysteresis behavior including major and minor loop effects are crucial for reliable ferroresonance predictions. The approach adopted in this paper is to modify the scalar hysteresis model of [50] and integrate it into the three-leg magnetic circuit.

In order to integrate the model into the electromagnetic circuit, the original hysteresis functions [50] have been modified to compute magnetic flux and MMFs instead of B and H

(e.g., $B \rightarrow \phi$ and $H \rightarrow f$)

$$\frac{d\phi_x}{dt} = \frac{df_x}{dt} \left[\rho_x + \frac{\phi_x^-(f_x) - \phi_x}{\phi_x^-(f_x) - \phi_x^+(f_x)} \left(\frac{d\phi_x^+(f_x)}{df_x} - \rho_x \right) \right] \quad \text{if } \frac{d\phi_x}{dt} \geq 0 \quad (3a)$$

$$\frac{d\phi_x}{dt} = \frac{df_x}{dt} \left[\rho_x + \frac{\phi_x - \phi_x^+(f_x)}{\phi_x^-(f_x) - \phi_x^+(f_x)} \left(\frac{d\phi_x^-(f_x)}{df_x} - \rho_x \right) \right] \quad \text{if } \frac{d\phi_x}{dt} < 0 \quad (x = a, b, c). \quad (3b)$$

The major hysteresis loop limiting ascending and descending curve functions, and instantaneous leg fluxes for each phase x are $\phi_x^+(f_x)$, $\phi_x^-(f_x)$, and ϕ_x , respectively, where the leg MMF potential is f_x . The slope of the fully saturated region along the limiting hysteresis curves is approximated by ρ_x .

In order to compute the hysteresis response through (3), the ascending and descending limiting curves ($\phi_x^+(f_x)$, $\phi_x^-(f_x)$) must be determined for the major hysteresis loops in each core leg. The following nonlinear function is used for this purpose:

$$\phi(f) = \text{sgn}(f) \cdot \alpha \log_e(\beta |f| + 1) \quad (4)$$

where α_x and β_x influence the vertical and horizontal scaling of $\phi(f)$, respectively. If (4) is transposed to the right (or left) by σ_x , the limiting ascending (or descending) curve functions defined for the major hysteresis loop are as follows:

$$\begin{aligned} \phi_x^+(f_x) &= \text{sgn}(f_x - \sigma_x) \cdot \alpha_x \log_e(\beta_x |f_x - \sigma_x| + 1) \\ \phi_x^-(f_x) &= \text{sgn}(f_x + \sigma_x) \cdot \alpha_x \log_e(\beta_x |f_x + \sigma_x| + 1) \end{aligned} \quad (x = a, b, c) \quad (5)$$

Therefore, σ_x allows the width of the major hysteresis loop to be specified. Furthermore, by separately defining $\phi_x^+(f_x)$ and $\phi_x^-(f_x)$, nonsymmetrical hysteresis loops can be defined. The advantage of these functions is that only two parameters (α_x, β_x) are required to fit the curve to measured data. However, the curve fitting process must be carefully performed for individual core legs because the strong magnetic leg couplings can increase sensitivity to fitting errors.

The required slope functions for (3) are obtained through differentiation of (5) with respect to MMF (f_x)

$$\frac{d\phi_x^\pm(f_x)}{df_x} = \frac{\alpha_x \beta_x}{\beta_x |f_x \mp \sigma_x| + 1} \quad (x = a, b, c). \quad (6)$$

In this paper, the limiting functions $\phi_x^+(f_x)$ and $\phi_x^-(f_x)$ were curve fitted to measured major hysteresis loops for each core leg obtained from the test procedures of [51] (see the Appendix for function parameters).

The modified hysteresis equations (3)–(6) estimate minor hysteresis loops based on domain wall motion theory of ferromagnetic material. The model assumes domain wall motion densities (Barkhausen jumps) vary proportionally to the growth or recession of domain regions corresponding to changes in field strength [50]. It is therefore important to note that even though the major hysteresis loop curve functions are estimated from sinusoidal excitation measurements, the model is capable of accurately estimating the magnetic response for arbitrary

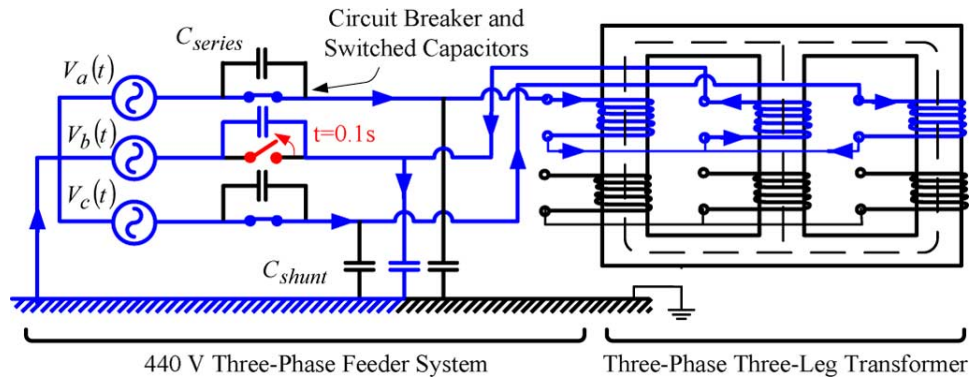


Fig. 4. Ferroresonance in an unloaded transformer fed through series and shunt capacitors (e.g., cable capacitance). The blue lines indicate the ferroresonance path when phase b circuit breaker is opened (red).

nonsinusoidal excitations (e.g., ferroresonance) provided they fall within the domain of the major hysteresis loop. This is because the hysteresis equations (3) are based on the variation of excitation to compute the variation of flux for estimating minor loop formations.

Finally, the formulated hysteresis functions are realized with current sources in the electromagnetic circuit controlled by (3) and solved in time domain in PSPICE using the Newton–Raphson numerical approach (see Fig. 3). At every time step, an “IF statement” selects one of the equations (3) based on the sign of the induced voltage or flux derivative, e.g., whether magnetization is increasing or decreasing. The model parameters and transformer data are included in the Appendix.

III. FERRORESONANCE SYSTEM CASE STUDY

The ferroresonance study for this paper is performed for an unloaded wye/wye three-phase three-leg transformer supplied by a three-phase source (see Fig. 4). The transformer primary and secondary windings are rated at 440 and 55 V (10 A), respectively, and operate at a nominal frequency of 50 Hz. The ferroresonance circuit consists of series and shunt capacitances interacting with the magnetizing inductances of the wound transformer core legs. The origin of C_{shunt} and C_{series} can typically be from circuit breakers equipped with grading capacitors, shunt and series transmission line capacitances (overhead and underground cables), reactive power compensation capacitor banks, and lumped stray capacitances in transformer windings, bushings, bus bars, and feeders.

In order for ferroresonance to occur, a system perturbation (e.g., switching transient) with initial conditions conducive to ferroresonance is usually necessary. For the studied system, phase b circuit breaker is used to impose switching transients to initiate ferroresonance. There have been many such practical occurrences where unsynchronized three-phase switching or single-phase circuit breaker operations resulted in one or two phases suddenly lost while the transformer is unloaded or lightly loaded, giving rise to ferroresonance [3]. For example, feeders employing single-phase circuit breakers or fuses can suddenly develop faults causing one of the phases to deenergize. The switching transient and resulting unbalanced excitation of the transformer can lead to a ferroresonance path involving magne-

tizing inductances in series with capacitances. Furthermore, in unloaded or lightly loaded systems (e.g., rural distribution feeders), there may be insufficient damping for ferroresonance. The resulting large distorted currents and over-voltages can cause severe damage to networks.

IV. SIMULATION RESULTS

Detailed time-domain simulation analysis based on the developed three-phase three-leg transformer model is carried out for the system described in Section III. Simulations are performed in PSPICE using the Newton–Raphson numerical algorithm with a variable time step limited to 50 μ s.

At the start of each simulation run, the voltage is ramped linearly to its rated value to reach steady-state conditions and to avoid transformer inrush effects. Ferroresonance considering different combinations of C_{series} and C_{shunt} parameters (see Fig. 4) with single-phase switching actions are tested. The initial conditions of the system must be considered as they highly influence ferroresonance behavior. Unless otherwise stated, the reported simulation results maintain the same initial values (e.g., point-on-wave of ac voltage when the circuit breaker is opened, residual fluxes and capacitance charge). At $t = 0$ s, the simulated core is assumed to have zero residual flux and all capacitors have no initial charge. The initial phase angle between the switch opening instant with respect to the phase a voltage peak is stated in degrees as ψ .

For selected cases, time-domain waveforms of primary voltages and currents including core leg fluxes are computed. Furthermore, bifurcation diagrams, Poincaré maps, phase-plane trajectories, and hysteresis formations are plotted to better analyze the complicated stability domain of ferroresonance modes. In Section V, experimental tests are performed to verify simulated results and model accuracy.

A. Bifurcation Analysis

A useful and effective approach for identifying system parameters conducive to ferroresonance is carried out through bifurcation analysis. The shunt capacitance is chosen as the bifurcation parameter and the primary phase voltages are studied. Tests are repeated for C_{shunt} ranging from 0.1 to 10 μ F under

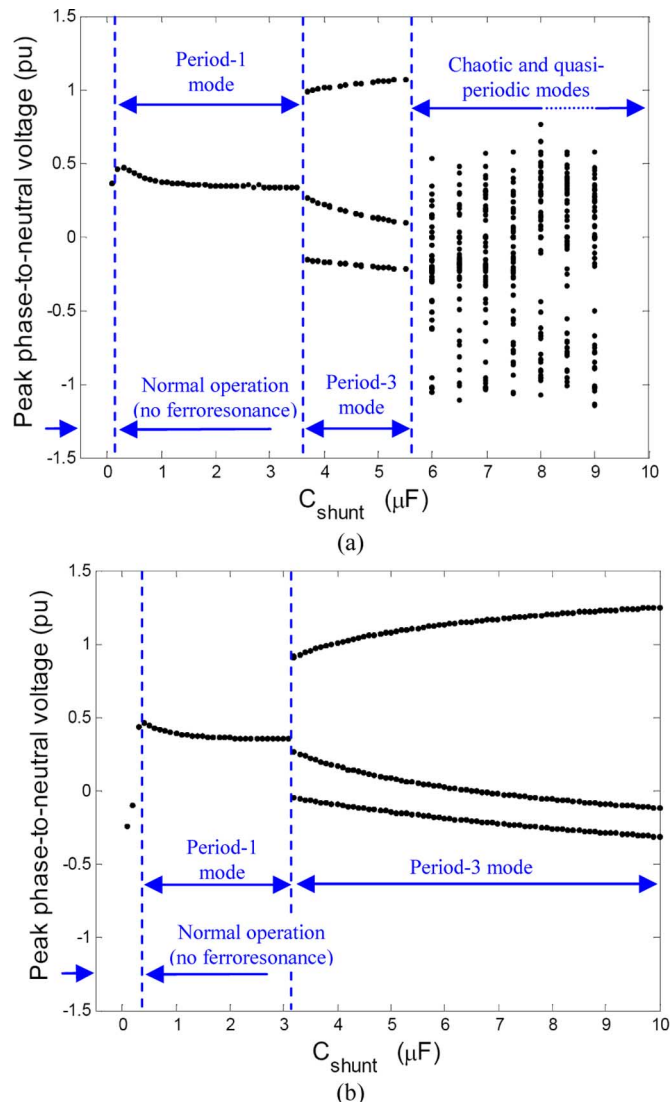


Fig. 5. Bifurcation diagram of ferroresonance modes (phase b voltage) for fixed C_{series} ($= 30$ pF) and different C_{shunt} values. (a) Considering hysteresis using the proposed three-phase three-leg transformer model and (b) without hysteresis using single-value magnetizing curves. Note the absence of chaotic ferroresonance modes and the generation of false period-3 modes in the lower diagram when using single-value (nonhysteretic) core models.

the same single-phase fault clearing condition. The bifurcation diagram is constructed from each C_{shunt} parameter change by sampling at the power system frequency (50 Hz) the primary voltage for the open phase b . The transient period is ignored in the sampling process to only analyze the subsequent stable ferroresonance oscillations. Poincaré maps are constructed in a similar way by sampling the phase-plane trajectory orbits. The resulting patterns can be interpreted for visual classification of ferroresonance modes [22].

Fig. 5 illustrates the existence of multiple ferroresonance modes in the bifurcation diagram based on the developed hysteresis core model. For $C_{\text{shunt}} = 0.1$ to 0.5 μF , there is a small jump (bifurcation) in the operating point from normal conditions to fundamental ferroresonance mode. Fundamental ferroresonance mode is shown in Fig. 6 for $C_{\text{shunt}} = 200$ pF. The

circuit breaker transient is indicated by the large orbit excursions which eventually settle to a stable attracting limit cycle. The distorted noncircular orbit indicates the presence of harmonics in the voltage waveforms.

For $C_{\text{shunt}} = 3.6$ μF , another bifurcation occurs where the transformer enters period-3 type ferroresonance mode as indicated by the branching into a three line trajectory (see Fig. 5). This mode is stable up to $C_{\text{shunt}} = 5.5$ μF . Simulated time-domain waveforms and hysteresis formation for this mode are shown for $C_{\text{shunt}} = 4$ μF in Fig. 7. The voltages, fluxes and currents exhibit highly distorted waveforms reaching in excess of 1.2, 2, and 0.4 pu of rated peak values, respectively. The phase-plane trajectory of this mode indicates multiple competing solutions (known as attractors) which influence the trajectory orbits to form subharmonic oscillations.

Beyond $C_{\text{shunt}} = 5.5$ μF , a bifurcation from period-3 into chaotic ferroresonance modes is detected. This is indicated by the nonrepeating structure of the bifurcation diagram corresponding to the sampling of chaotic voltage waveforms. This behavior is due to the existence of a strange attractor in the stability domain.

B. Sensitivity of Ferroresonance to Initial Conditions

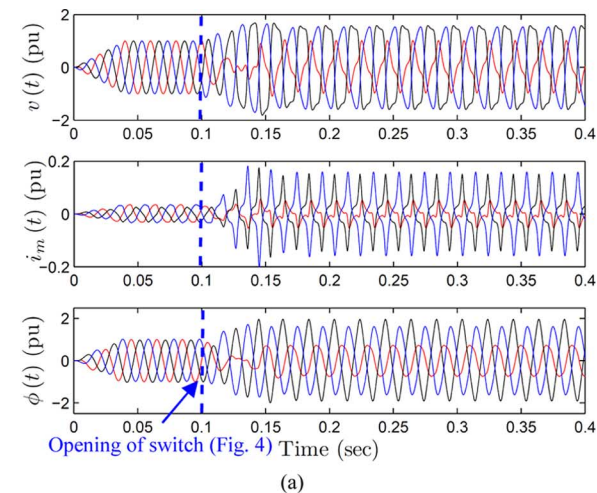
The previous simulation studies have assumed fixed circuit parameters for a varying C_{shunt} . To illustrate the sensitivity of ferroresonance to initial conditions, the circuit breaker opening instant for the previous case (see Fig. 7) is now changed to $\psi = 60^\circ$. The resulting waveforms and phase-plane trajectories in Fig. 8 now indicate a momentary ferroresonant oscillation which loses its stability and dampens out.

C. Impact of Hysteresis on Three-Phase Three-Leg Transformer Ferroresonance

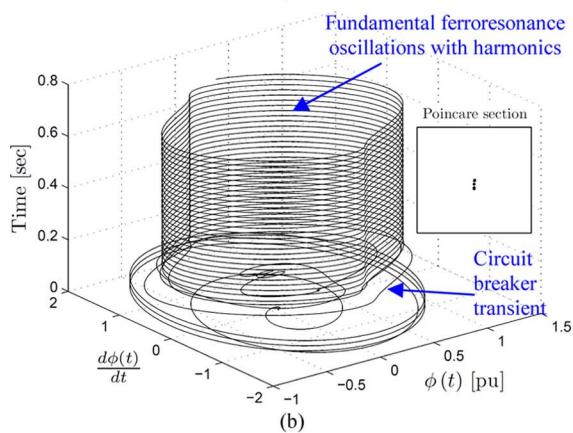
The bifurcation diagram of Fig. 5(b) demonstrates the estimated ferroresonance modes based on a nonhysteretic core model. A single-value nonlinear saturation curve based on (4) with zero hysteresis width in each core leg is implemented for the previous case study. The predicted stability domain of ferroresonance is significantly different when compared to Fig. 5(a). The bifurcation transition into period-3 ferroresonance occurs at a lower C_{shunt} value (3.1 μF) without hysteresis compared to $C_{\text{shunt}} = 3.6$ μF with hysteresis, and extends for a wider range of capacitance. More importantly, when hysteresis is neglected, the model does not detect the chaotic modes and falsely replaces them with extended period-3 subharmonic modes. These findings are consistent with the single-phase transformer study performed in [41] in which chaotic modes were also misrepresented in nonhysteretic core models. The bifurcation diagram of Fig. 5(a) has been confirmed through extensive measurements.

D. Impact of Magnetic Couplings on Three-Phase Three-Leg Transformer Ferroresonance

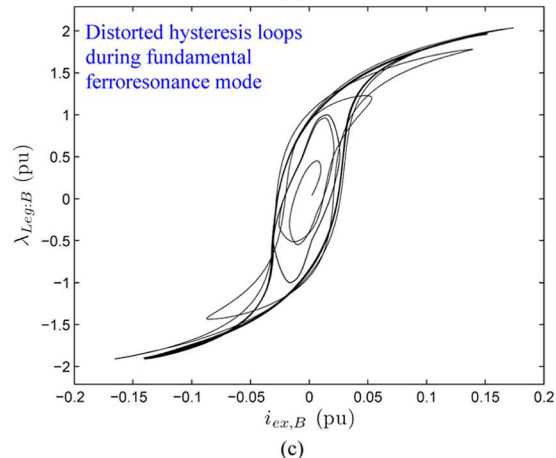
In order to assess the impact of magnetic leg couplings on three-phase transformer ferroresonance, a transformer bank (i.e., three single-phase transformers) was simulated under the



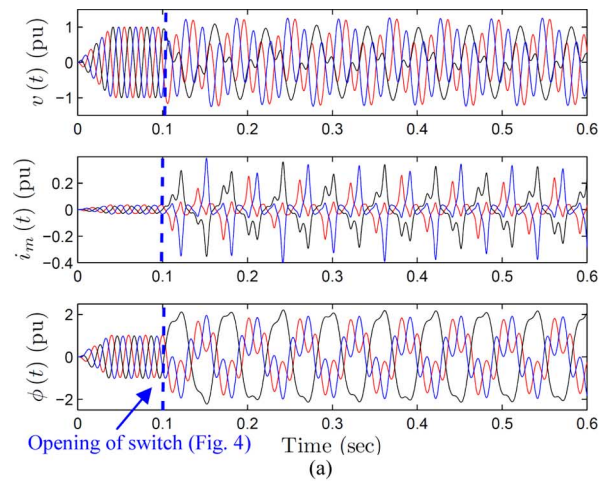
(a)



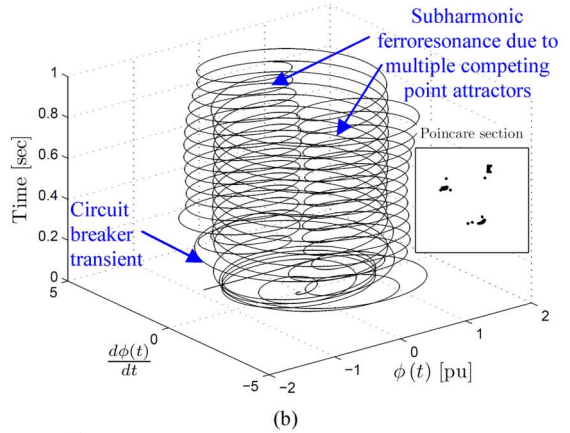
(b)



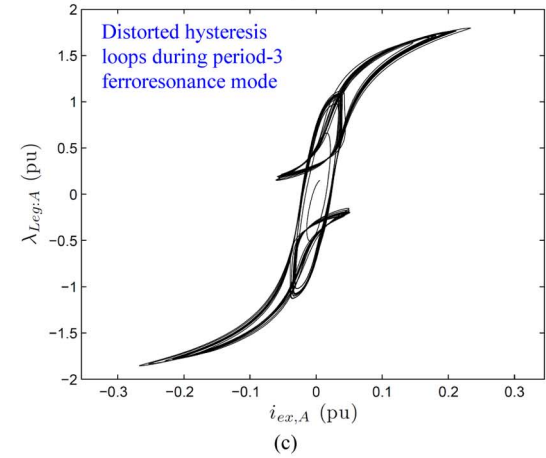
(c)



(a)



(b)



(c)

Fig. 6. Time-domain waveforms of transformer primary voltages, winding currents and core fluxes for *fundamental ferroresonance mode* ($C_{\text{series}} = 200 \text{ nF}$, $C_{\text{shunt}} = 200 \text{ pF}$). (b) Phase-plane trajectory and (c) hysteresis loop (phase *b*) shows the circuit breaker transient perturbing the system oscillations which then settle to a stable attracting limit cycle. The circuit breaker is opened at an initial phase angle of $\psi = 90^\circ$ w.r.t. peak phase *a* voltage.

Fig. 7. (a) Time-domain waveforms of transformer primary voltages, winding currents and core fluxes for *period-3 subharmonic ferroresonance mode* ($C_{\text{shunt}} = 4 \mu\text{F}$). (b) Phase-plane trajectory and (c) hysteresis loop (phase *a*) clearly indicates the transient caused by circuit breaker operation and the existence of competing attractors in the system orbits. The circuit breaker is opened at an initial phase angle of $\psi = 90^\circ$ w.r.t. peak phase *a* voltage.

same conditions described in Section III (see Fig. 4). This type of transformer has no magnetic core leg couplings because the magnetic cores of each phase are physically isolated. The developed model can approximate this behavior by setting the zero-sequence reluctance to a very small value, effectively elim-

inating magnetic leg couplings. The corresponding bifurcation diagram is very similar to Fig. 5 (not shown) and similar ferroresonance modes are predicted. However, on closer examination of time-domain waveforms (e.g., $C_{\text{shunt}} = 5 \mu\text{F}$), ignoring inter-phase magnetic couplings results in significant differences

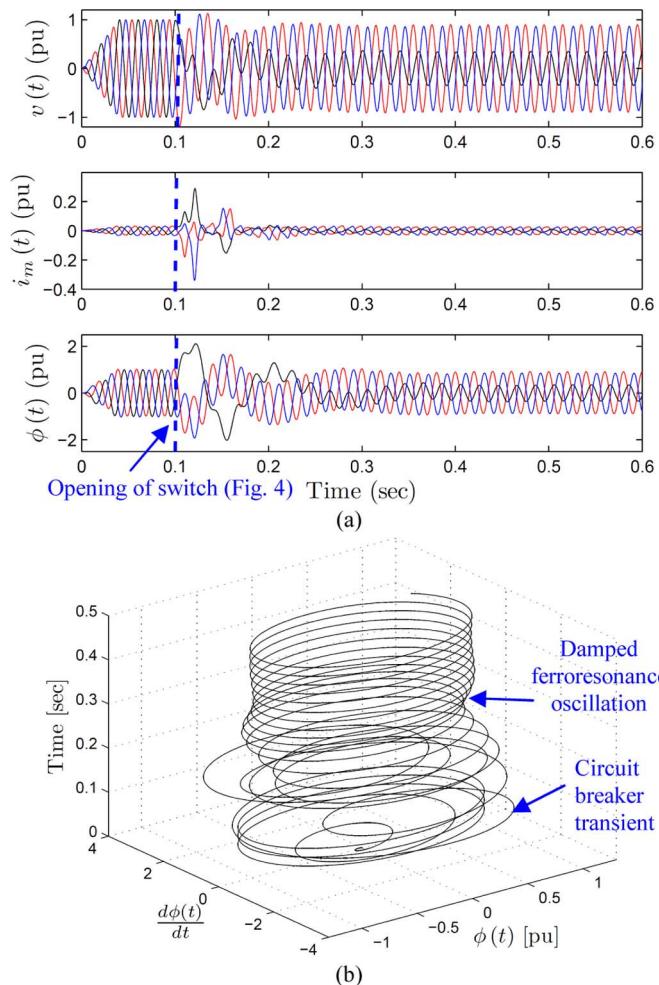


Fig. 8. (a) Time-domain waveforms of transformer voltages, winding currents, and fluxes for *unstable ferroresonance*. (b) Phase-plane trajectory indicates the transitory period and damping of ferroresonance in the steady state. The circuit breaker is opened at an initial phase angle of $\psi = 60^\circ$ w.r.t. peak phase a voltage.

in the predicted waveforms when compared to the proposed model (see Fig. 9). Furthermore, the computed phase-plane trajectories (drawn in 2 dimensions to highlight incongruities) assume different orbit trajectories.

V. EXPERIMENTAL RESULTS AND MODEL VALIDATION

Further investigations of three-phase transformer ferroresonance were carried out through experimental tests for the system of Fig. 4. The validity of the developed transformer model under ferroresonance conditions is examined by comparing simulations of ferroresonance with real measurements obtained from a dry-type three-leg 440/55-V laboratory test transformer (see Fig. 15 in the Appendix). The transformer electrical parameters have been determined from three-phase open and short circuit tests. The nonlinear asymmetric core magnetizing characteristics were measured by single-phase sinusoidal excitations of each leg. Based on the parameters given in the Appendix, the core models for each magnetic leg closely agree with mea-

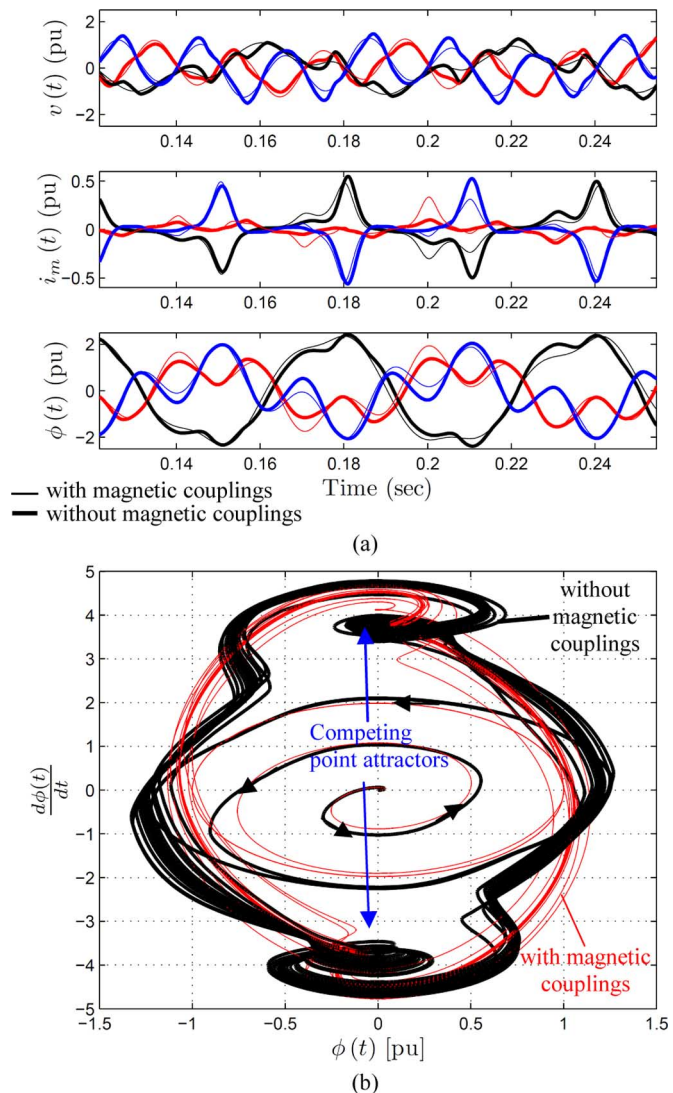


Fig. 9. Comparisons of simulated ferroresonance oscillations for $C_{\text{shunt}} = 5 \mu\text{F}$ considering core leg magnetic couplings (thin lines) versus three single-phase transformer bank with no magnetic couplings (thick lines). Time-domain waveforms (a) for voltages, currents, and fluxes are shown (see Fig. 11 for model comparison to measurements) and (b) phase-plane trajectories (drawn in two dimensions to highlight differences). Both models indicate *period-3 subharmonic modes*, however, wave shapes are incongruent and phase-plane trajectories diverge to different orbits.

sured hysteresis loops for a wide range of excitations (see Fig. 10).

A. Measurement Apparatus and Method

The three-phase experimental setup (see the Appendix) consists of an autotransformer source, isolation transformers, three single-phase circuit breakers for imposing unbalanced switching transients, capacitor banks, and a 440/55-V three-phase three-leg transformer. Each circuit breaker has a fixed measured open-circuit capacitance of approximately 30 pF. The switchable capacitor banks operate in the microfarad range and are connected in shunt arrangement, as shown in Fig. 4. Two synchronized oscilloscopes were setup to capture the transformer primary phase-to-neutral voltages and phase winding currents.

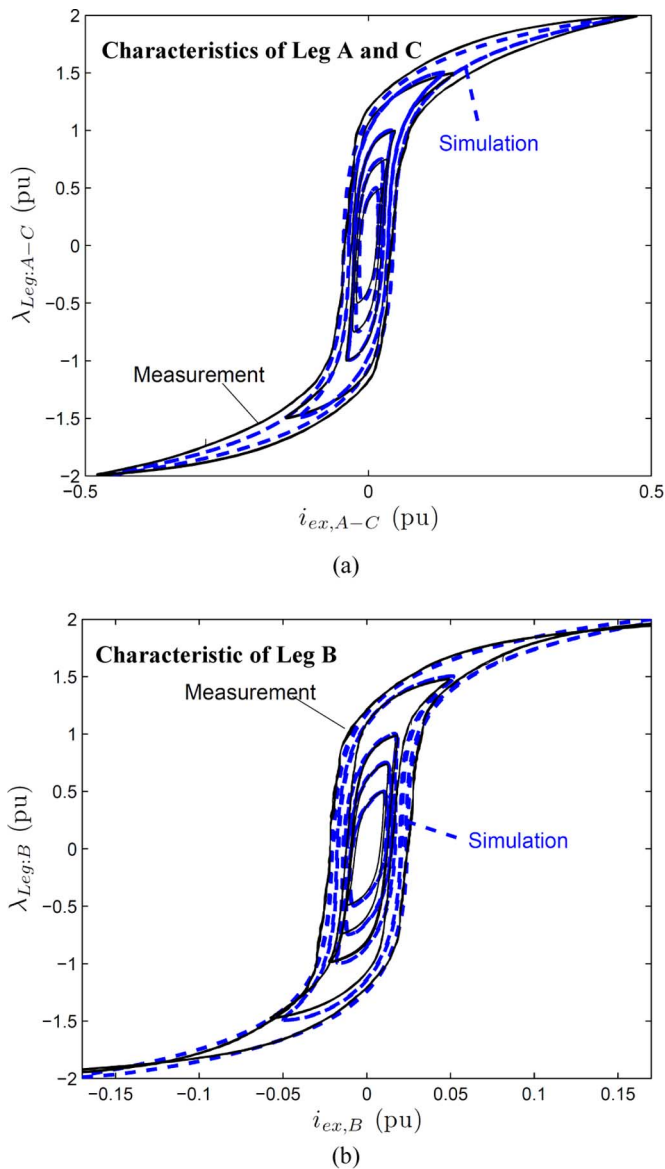


Fig. 10. Measured (solid line) versus modeled (dashed line) core magnetization hysteresis loops (major and minor) for (a) outer and (b) center legs at different excitation levels.

In order to obtain good comparisons of measured and simulated waveforms, the initial conditions (i.e., the instant of voltage phase angle the circuit breaker operates) at the onset of ferroresonance must be determined precisely. The slightest phase mismatch can lead to large discrepancies. The two oscilloscopes were triggered simultaneously at the moment of circuit breaker operation to capture initial conditions and subsequent ferroresonance oscillations. Measurements of ferroresonance were obtained with different shunt capacitance values and switching of phase *b* circuit breaker.

B. Experimental Results

Fig. 11 displays the measured and model computed period-3 subharmonic ferroresonance modes in the primary voltage waveforms ($C_{\text{shunt}} = 5 \mu\text{F}$). Close agreement is shown for the transition (bifurcation) from normal conditions to fer-

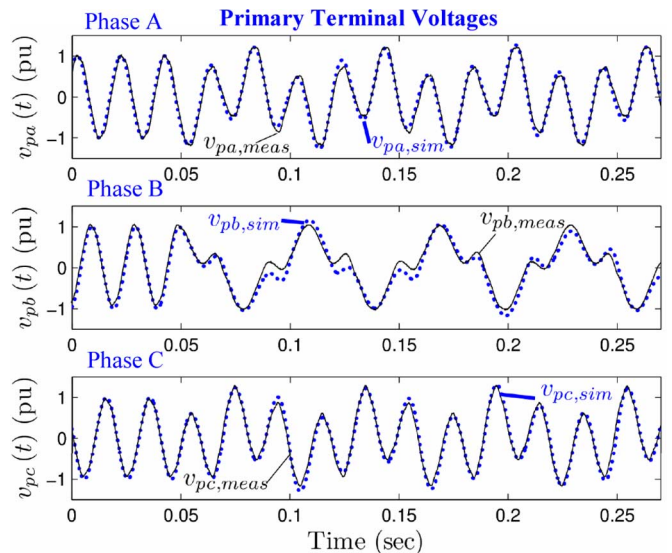


Fig. 11. Comparison of measured (solid line) versus simulated (dashed line) ferroresonance oscillations in transformer primary voltage (v_p) waveforms ($C_{\text{shunt}} = 5 \mu\text{F}$). Transition (bifurcation) from normal operation to stable period-3 subharmonic ferroresonance (bifurcation) is shown. The circuit breaker is opened at an initial phase angle of $\psi = -137^\circ$ w.r.t. peak phase *a* voltage.

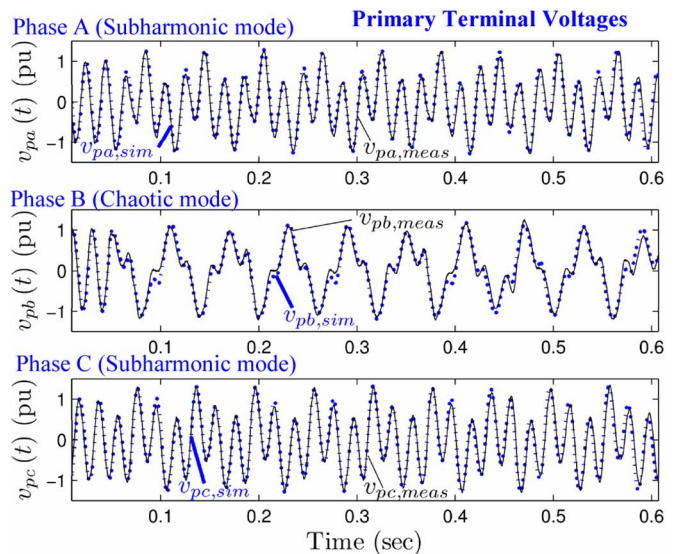


Fig. 12. Comparison of measured (solid line) versus simulated (dashed line) chaotic ferroresonance oscillations in transformer primary voltage (v_p) waveforms ($C_{\text{shunt}} = 7 \mu\text{F}$). Stable subharmonic period-3 (phases *a* and *c*) and chaotic ferroresonance oscillations (phase *b*) are shown. The circuit breaker is opened at an initial phase angle of $\psi = -74^\circ$ w.r.t. peak phase *a* voltage.

roresonance as well as the subsequent steady-state oscillations in all three phases. Note that the wave shapes are not identical amongst all phases. The wave shape of the faulted phase *b* is markedly different to phases *a* and *c*, but is still period-3 mode. This is because the ferroresonance path of the center leg is not identical to the other legs due to the open phase *b* condition. The center phase magnetizing inductance has a direct path to the shunt capacitance compared to the other two phases (see Fig. 4). Furthermore, the core is asymmetric because the center leg (phase *b*) has a shorter flux path length. Since phase *b* is open, the voltage is not being supplied by the source, but

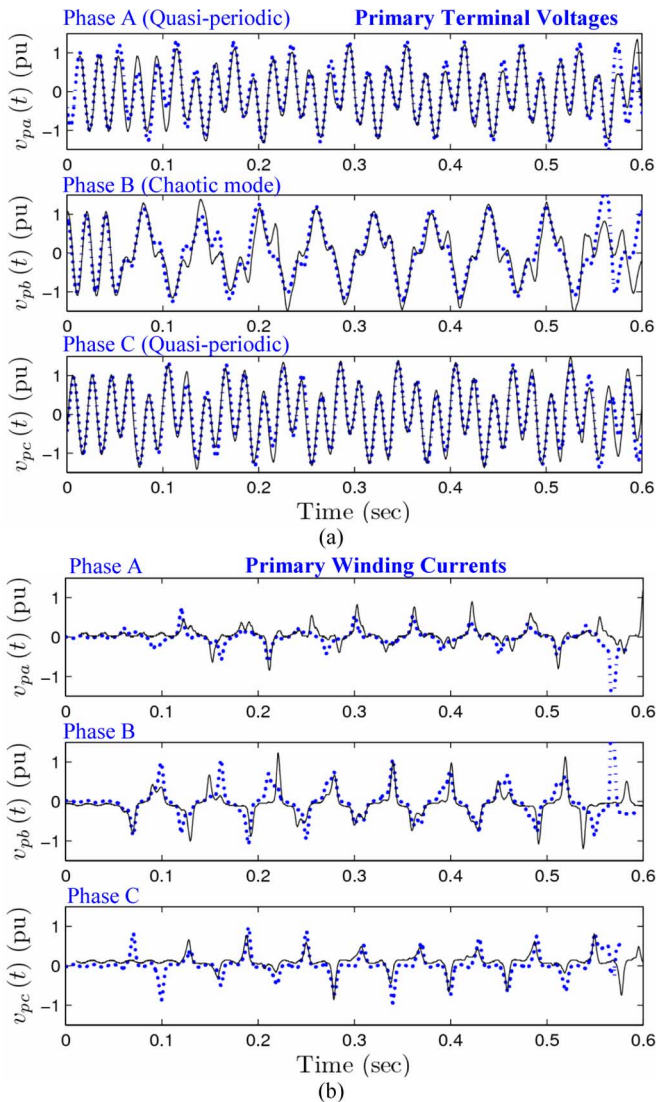


Fig. 13. Comparison of measured (solid line) versus simulated (dashed line) chaotic ferroresonance oscillations for primary (a) terminal voltages (v_p) and (b) winding currents (i_p) for $C_{\text{shunt}} = 9 \mu\text{F}$. The waveforms exhibit chaotic behavior in phase b and quasi-periodic mode resembling subharmonic (period-3) ferroresonance in phases a and c . The circuit breaker is opened at an initial phase angle of $\psi = 60^\circ$ w.r.t. peak phase a voltage. The errors are due to the sensitivity of chaos to mismatching of initial conditions.

is developed by induction from magnetic flux couplings of the core.

Comparisons of measured and simulated waveforms for $C_{\text{shunt}} = 7 \mu\text{F}$ are shown in Fig. 12. It is interesting to note that phases a and c exhibit subharmonic ferroresonance oscillations while phase b waveforms are chaotic. This has not been documented in prior studies. This behavior is due to the complicated electromagnetic phase couplings in the core. The developed transformer model accurately duplicates this behavior under the same conditions. Further experimental tests determined more chaotic modes for larger C_{shunt} values.

Fig. 13 depicts the measured and simulated phase voltages and winding currents for $C_{\text{shunt}} = 9 \mu\text{F}$. Chaotic ferroresonance modes are observed in phase b ; however, phases a and c waveforms resemble period-3 mode but are strictly

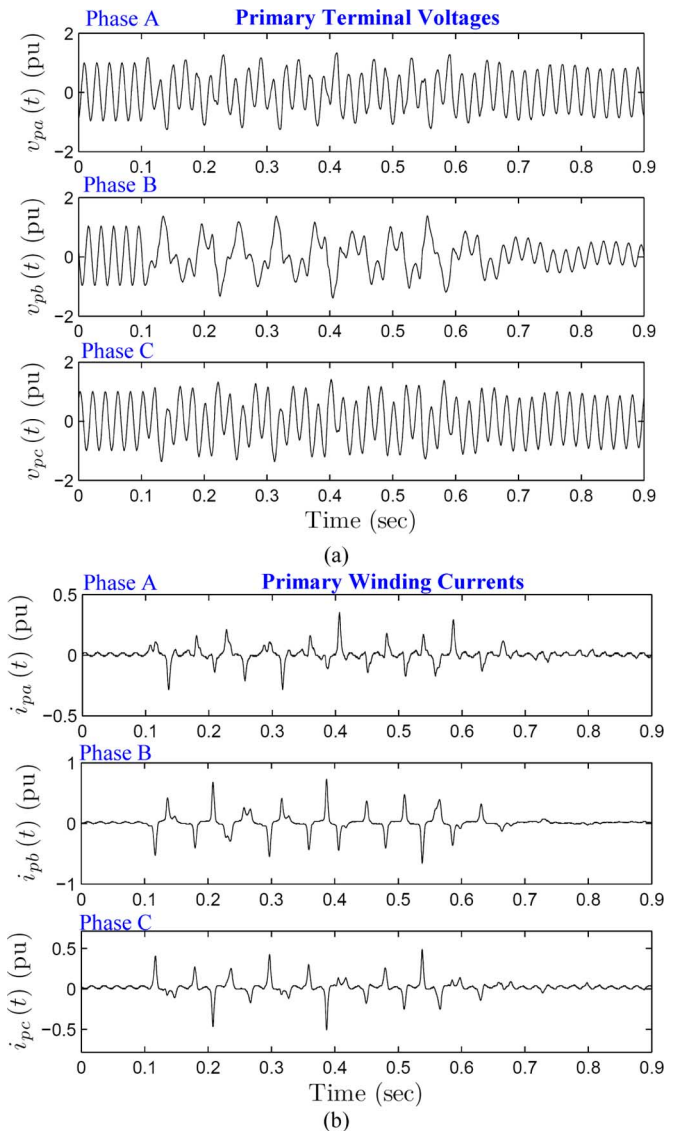


Fig. 14. Measured transformer waveforms for primary (a) terminal voltages (v_p) and (b) winding currents (i_p). The previous case (see Fig. 13) is repeated for the same C_{shunt} ($9 \mu\text{F}$) but at a different circuit breaker opening time which results in momentary unstable chaotic ferroresonance. The circuit breaker is opened at an initial phase angle of $\psi = 66^\circ$ w.r.t. peak phase a voltage.

nonrepeating (quasi-periodic). The maximum peak voltage is approximately 1.5 pu for C_{shunt} between 8.0 and 9.5 μF . These high overvoltages can degrade winding insulation and cause excessive losses.

Note that after a few cycles, the simulated chaotic waveforms tend to diverge away from measurements due to sensitivity to small unaccounted for perturbations (e.g., supply harmonics) and differences in initial conditions (e.g., precise switching instant). A summary of the measured ferroresonance modes and peak phase voltages is shown in Table I.

Lastly, the influence of circuit breaker switching time on resulting ferroresonance behavior was examined experimentally (see Fig. 14). The case for $C_{\text{shunt}} = 9 \mu\text{F}$ (see Fig. 13) was repeated for a different switching angle with respect to phase a voltage peak. By changing the circuit breaker opening instant

TABLE I
OBSERVED FERRORESONANCE MODES AND PEAK PHASE VOLTAGE
VALUES: $C_{\text{series}} = 30 \mu\text{F}$ AND $C_{\text{shunt}} = 2 \text{ TO } 10 \mu\text{F}$

C_{shunt} (μF)	Ferroresonance Modes*			V_a^{peak} (pu)	V_b^{peak} (pu)	V_c^{peak} (pu)
	Phase a	Phase b	Phase c			
2.0	I	I	I	1.16	0.82	1.16
3.0	I	I	I	1.17	1.04	1.29
4.0	III	III	III	1.25	1.17	1.40
5.0	III	III	III	1.20	1.05	1.37
5.5	III	III	III	1.21	1.09	1.37
6.0	III	C	III	1.29	1.30	1.43
6.5	III	C	III	1.35	1.25	1.45
7.0	III	C	III	1.27	1.27	1.40
7.5	III	C	III	1.38	1.35	1.46
8.0	III	C	III	1.45	1.45	1.49
8.5	III	C	III	1.43	1.37	1.49
9.0	Q-III	C	Q-III	1.45	1.43	1.48
9.5	Q-III	C	Q-III	1.40	1.49	1.45
10.0	Q-III	C	Q-III	1.43	1.45	1.45

*) Ferroresonance modes- I: period-1 fundamental, III: period-3 subharmonic, Q: quasi-periodic, C: chaotic, Q-III: quasi-periodic modes resembling period-3 type ferroresonance.

from $\psi = 60^\circ$ to $\psi = 66^\circ$, the previously stable chaotic modes became unstable and dampened out.

VI. CONCLUSION

A new analysis of the stability domain of three-phase transformer ferroresonance in multi-leg core structures is presented in this paper. For the first time, a newly developed three-leg core model considering dynamic leg hysteresis nonlinearities, core topology and asymmetric leg couplings is applied to ferroresonance. Extensive experimental tests of transformer ferroresonance have been performed to confirm the accuracy of model predictions. The main conclusions are as follows.

- 1) The study results indicates that the stability domain of ferroresonance modes and amplitude oscillations (e.g., voltage, current and fluxes) are highly dependent on the correct modeling of magnetic couplings and nonlinearities of the iron-core structure.
- 2) Predicted ferroresonance modes (e.g., subharmonic and chaotic modes) are shown to be misrepresented in three-phase transformer models that neglect hysteresis nonlinearities (e.g., using single-value functions). False ferroresonance modes and the omission of more severe chaotic modes are shown for nonhysteretic core models.
- 3) Likewise, the magnetic couplings in the legs are shown to significantly impact the accuracy of predicted wave shapes and trajectories of ferroresonance oscillations.
- 4) For the first time, measured and modeled ferroresonance oscillations are shown to exhibit different behavior in each phase. For particular conditions, chaotic voltage waveforms were observed in the open circuited phase and subharmonic or quasi-periodic modes in the other phases. Therefore, extending per-phase modeling approaches and

analysis techniques to the study of three-phase transformer ferroresonance behavior can lead to incorrect results.

- 5) The developed three-leg core model correctly predicted ferroresonance modes observed in laboratory tests. Results show that the model duplicates the three-phase terminal voltage waveforms with high accuracy under transient and steady-state ferroresonance conditions.
- 6) Moreover, for stable periodic modes (e.g., subharmonics), the model accurately predicted their existence for the range of capacitance values observed experimentally. For nonperiodic modes (e.g., quasi-periodic and chaotic), the model can reproduce waveforms accurately for a few cycles after the bifurcation point if initial conditions are known precisely. However, due sensitivity of chaos to minute differences in initial conditions (e.g., switching transient) and small unaccountable perturbations (e.g., supply harmonics), incorrect predictions occur for long term behavior under chaotic conditions.
- 7) The proposed three-leg transformer modeling approach is general and expandable to the study of ferroresonance and other transient disturbances in different electrical machines, transformer types and configurations (e.g., five-leg transformers, induction machines, etc.). The modeling approach is useful for evaluating transformer stresses (e.g., insulation) and testing dynamics of three-leg core designs.

APPENDIX

MODEL PARAMETERS AND EXPERIMENTAL SETUP

TABLE II
HYSTERESIS AND MAGNETIC CORE MODEL DATA

Ascending function $\phi_x^+(f_x)$	Descending function $\phi_x^-(f_x)$
$\alpha_a = 0.73, \beta_a = 300, \sigma_a = 0.2$	$\alpha_a = 0.73, \beta_a = 300, \sigma_a = 0.1$
$\alpha_b = 0.65, \beta_b = 1400, \sigma_b = 0.1$	$\alpha_b = 0.68, \beta_b = 1400, \sigma_b = 0.01$
$\alpha_c = 0.73, \beta_c = 300, \sigma_c = 0.2$	$\alpha_c = 0.73, \beta_c = 300, \sigma_c = 0.1$
Magnetic parameters: $\Re_0 = 1500 \text{ A.t/Wb}$, $\rho_a = 0.1$, $\rho_b = 1.0$, $\rho_c = 0.1$	

TABLE III
TRANSFORMER DATA AND ELECTRIC EQUIVALENT CIRCUIT PARAMETERS

Description	Data
Rated primary winding voltage (v_p)	440 V
Rated secondary winding voltage (v_s)	55 V
Turns ratio (N)	8
Operating frequency (f)	50 Hz
Rated secondary current (i_s)	10 A
Primary winding resistance (R_{pa}, R_{pb}, R_{pc})	9.423 Ω (0.0268 pu)
Secondary winding resistance (R_{sa}, R_{sb}, R_{sc})	0.147 Ω (0.0268 pu)
Primary leakage inductance (L_{pa}, L_{pb}, L_{pc})	6.341 mH (0.00566 pu)
Secondary leakage inductance (L_{sa}, L_{sb}, L_{sc})	0.0991 mH (0.00566 pu)

$$Z_{p, \text{base}} = N^2 \cdot Z_{s, \text{base}} = N^2 \cdot v_{s, (\text{rated})} i_{s, (\text{rated})} \text{ (primary referred).}$$

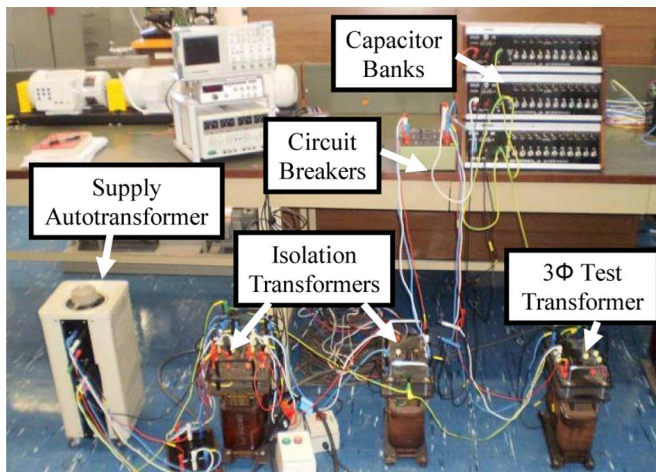


Fig. 15. Experimental setup for three-phase transformer ferroresonance tests.

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