A Dynamic Model of Mobile Telephony Subscription Incorporating a Network Effect

Running title: Mobile Telephony Subscription

Gary Madden*, Grant Coble-Neal, Brian Dalzell
Communication Economics and Electronic Markets Research Centre
School of Economics and Finance
Curtin University of Technology
GPO Box U1987, Perth, Australia 6845
Tel: +61-8-9266-4258, Fax: +61-8-9266-2391
CEEM Homepage: http://www.cbs.curtin.edu.au/research/ceem

*Corresponding author.
A Dynamic Model of Mobile Telephony Subscription Incorporating a Network Effect *

Abstract

This study examines the growth of global mobile telephony and the economic factors that affect this growth. Mobile telephony has exhibited substantial growth in the decade to 2000 and this growth is expected to continue with the introduction of technically advanced mobile cellular networks. A dynamic demand model is estimated using global telecommunications panel data comprised of 56 countries. Results from the estimation are provided along with elasticity estimates and impulse response functions for price and income.

* We thank Inho Chung, an anonymous referee and seminar participants at the Evolution of Mobile Services—National and International Session presentation at the 14th Biennial Conference of the International Telecommunications Society, Seoul, Korea, August 2002. The authors are also grateful to Yoel Finkel of the Central Bureau of Statistics Israel, Laszlo Kasa of the Communication Authority of Hungary, Elsa Neira De Uribe, Colombian Institute for the Development of Science and Technology, Bernadette Finn at Teligen, John Ure of the University of Hong Kong and the staff at ChinaNex.com for valuable assistance on data sources. The usual disclaimer applies.
1. INTRODUCTION

A mobile telephone network is comprised of the physical components required to connect users. The basic physical components are the handset, base station and mobile service switching station (MSC) (Gruber and Hoenicke, 1999). A call made from a handset is transmitted to a base station and then to an MSC. An area that is serviced by this network is divided geographically into cells. A cellular system can employ many small radio coverage areas to provide service (Foreman and Beauvais 1999). Since 1990 mobile telephone subscription has doubled globally every 20 months. From an 11 million subscriber base and an average penetration of 1% at 1990, the mobile telecommunications industry now supports a half billion subscribers (International Telecommunication Union (ITU), 1999). The average global penetration at June 1999 was 27% (Gruber and Valletti, 2003).

Several institutional developments have had an impact on mobile telephony growth.\(^1\) Introduction of digital technology substantially relaxed the radio spectrum constraint. Transmission rates increased from 0.33 bits/second/Hz to approximately 1.40 bits/second/Hz as TDMA allowed more efficient use of the radio spectrum (Gruber and Valletti, 2003). Digital technology brought features for commercial mobile telecommunications not available with analogue technology. In particular, digital technology permits data transmission, e.g., short message service, e-mail and increased sound quality. Digital networks require lower power levels for operation that results in lighter and smaller handsets (ITU,
Second-generation (2G) mobile systems operation have drawn on the experience of first-generation (FG) mobile systems in the realisation of network effects and economies of scale. This has resulted in the creation of fewer systems than for FG mobile.

The early mobile telephony industry was mostly monopoly-operator supplied. Existing fixed-line operators initially provided mobile telephony as an extension or value-added service. At 1990 three-quarters of the 29 Organisation for Economic Co-operation and Development (OECD) member countries with mobile telephony had a monopoly provider — by 2000 none had monopoly providers. Duopoly providers serviced four countries, eleven had three operators, and fourteen had more than three mobile operators (Gruber and Valletti, 2003). Regulatory innovation in mobile telephony markets concern the timing and number of licenses granted, the method by which licenses are granted and whether a technological standard is set (Gruber and Verboven, 2001). With technological advance the subscriber base a network can support is increased, as is the demand for mobile service. Ultimately the number of licenses granted also grew. Additional licenses allowed for intensified competition, which further fuelled diffusion. Gruber and Verboven suggest the timing of first and second licenses might explain why diffusion occurred more rapidly in certain countries. Reasons given for catch-up include economies of scale (infrastructure investment including the cost of mobile handsets decrease through time), whereby average network set up costs decline with network size. Late adoption externalities may also arise due to learning spillovers. Entry of mobile providers into former monopoly markets ensured the evolution of a more competitive environment.
Mobile operators developed tariff (pricing) packages in an attempt to differentiate themselves from their competitors, isolate market segments and target customer groups and geographic regions (ITU, 1999).²

The focus of this study is the analysis of economic drivers of market growth, viz., price, income and network effects (endogenous) within this evolving institutional context. In particular, the price of acquiring and using mobile telecommunications since its inception has declined. Further, Jha and Majumdar (1999) find that mobile telephony penetration has varied substantially among countries by their gross domestic product (GDP) per capita. They argue greater prosperity translates into an enhanced demand for mobile telecommunications service. Gruber and Verboven (2001) find no support for this case from within the OECD. Finally, Gruber and Valletti (2003) argue network effects in production are due to economies of scale equipment supply and operation of networks, and that consumption externalities arise from subscribers’ ability to roam.³ Network effects are larger in the presence of a common standard. Consumption effects lead to self-propelling or endogenous growth. Such endogenous growth is particularly important during the early adoption stage for new networks.

The literature concerning patterns of technology diffusion has mostly considered the dominant stylized fact that adoption typically follows an S-shaped curve, i.e., diffusion rates initially rise then fall over time ultimately leading to market satiation (Geroski, 2000). Many underlying motivations can generate S-shaped curves (see Parker, 1994). The estimation of such models typically requires long
time-series. This data requirement limits the potential to provide projects on market growth early in the diffusion process and also ignores the problem of parameter variation in new product diffusion models (see Meade and Islam; Putsis, 1998). The approach adopted here follows Madden and Coble-Neal (2001). Rather than modelling the diffusion process per se they consider optimising economic agent behaviour directly. They assume an individual’s instantaneous indirect utility of subscribing to mobile telephony depends on income, price and current network size, where network size is the number of current subscribers. An advantage of the approach is that it can be applied to developing country penetration issues by using short time-series employing a pooled sample. Pooled samples better enable the role of income in the diffusion process to be assessed in the absence of long time-series.

The paper is organized as follows. Section 2 provides a brief discussion of the economic factors that drive mobile subscription. In Section 3 a model to examine mobile telephony network growth that incorporates a network effect is specified. Data and variables used in the estimation are presented and described in Section 4. The empirical modelling strategy is explained in Section 5, and estimates are reported. Concluding remarks and policy implications are provided in Section 6.

2. ECONOMIC FACTORS AND MOBILE SUBSCRIPTION

Mobile Telephony Pricing

In the early stages of mobile telephony diffusion subscription was mostly
business related. Prior to digital cellular technology there was no incentive for providers to lower their prices as they faced excess demand. High service and access prices *de facto* rationed the limited spectrum. The introduction of digital technology allowed service provider entry into these monopoly markets. This entry led to competition among operators for subscribers and resulted in lower prices. Subsequent price reductions were used to expand an operator’s subscriber base — and were the first consumer-orientated tariff strategies. ITU (1999) *World Development Report* describes current mobile pricing strategy as based on extensive market research and analysis of usage. For instance, mobile telephone operators are now expanding market by targeting late-adopter groups.

*Gross Domestic Product*

Jha and Majumdar (1999) expect GDP per capita to enhance mobile telephony diffusion. They argue that greater GDP per capita signifies greater affordability and so leads to increased demand for mobile telecommunications service. Gruber and Verboven (2001) find no empirical support for this proposition however, their finding may arise because of the relative ‘narrow band’ of high-income countries they examine. Further, the role of GDP in mobile telephony diffusion may not be as clear as Jha and Majumdar (1999) propose, e.g., countries such as Cambodia have seen mobile telephony subscription outstrip that of fixed lines. Gruber (2001), however, finds no such relationship for Central and Eastern Europe.
Network Effects

New subscribers joining a network increase the utility of current subscribers. This process leads to self-propelling or endogenous network growth, and suggests that current subscription is positively influenced by previous subscription (Economides and Himmelberg, 1995). In particular, little if any utility is gained from an individual subscribing to the network unless there are sufficient subscribers already using the service. However, the viability of a new network relies on the spontaneous existence of an initial critical mass of subscribers. Intuitively, early adopters must derive a high level of value from the good, even though it has limited use.

3. THEORETICAL MODEL

The approach adopted here follows Madden and Coble-Neal (2001) who rather than modelling the diffusion process per se consider optimising economic agent behaviour directly. They let the instantaneous utility of subscribing to mobile telephony for an individual with income $Y$ and a network of size $N$ be given by $u(Y, N)$, where the size of a network is determined by the number of subscribers. Assuming network connection yields an infinite stream of future utility, given an expected future time path of network size $N^e(t)$, the present value of the benefits from network subscription for a consumer with income $Y$ is,
where \( \rho \) is the discount rate. Suppose subscription is offered at time \( t \) at price \( P(t) \). When subscribed at \( t \), the corresponding present value of access cost is

\[
q(t) = e^{-\rho t} P(t).
\]

Consumers choose to subscribe at \( t^* \) to maximize

\[
V(Y, t, N^e(t)) - q(t).
\]

Assuming (3) is concave over the relevant range, \( t^* \) is characterized by

\[
u(Y, N^e(t^*)) = \rho P(t^*) - \frac{\partial P(t^*)}{\partial t} = \lambda(t^*)
\]

where \( \lambda(t^*) \) is the opportunity cost of subscription. With utility specified Cobb-Douglas, (4) translates to

\[
u(Y_t, N_t^e) = A Y_t^e N_t^{ew} = \lambda_t
\]

and implies an equilibrium network size

\[
\ln N_t^e = \mu + \alpha \ln \lambda_t + \beta \ln Y_t
\]
where \( \mu = -\omega^{-1} \ln A \), \( \alpha \ln \lambda_i = \omega^{-1} \ln \lambda_i \), and \( \beta \ln Y_i = -\omega^{-1} \ln Y_i \). Further, assuming the market does not instantaneously adjust to its long-run equilibrium and the expected network size in equilibrium at \( t \) (\( N_e^t \)) is not observed. They follow Cabal and Leita (1992) by assuming the actual value of \( N_i \) results from a process of partial adjustment toward \( N_e^t \):

\[
\ln N_i - \ln N_{i-1} = \gamma (\ln N_e^t - \ln N_{i-1})
\]

(7)

where the partial adjustment coefficient is \( 0 < \gamma < 1 \). Substitution of (6) into (7) yields the network equilibrium correction model for estimation:

\[
\ln N_i - \ln N_{i-1} = \gamma (\mu + \alpha \ln \lambda_i + \beta \ln Y_i - \ln N_{i-1})
\]

(8)

which after rearrangement becomes

\[
\Delta \ln N_i = \alpha_0 + \alpha_1 \ln \lambda_i + \alpha_2 \ln Y_i - \alpha_3 \ln N_{i-1}
\]

(9)

where \( \Delta \ln N_i = \ln N_i - \ln N_{i-1} \), \( \alpha_0 = \gamma \mu \), \( \alpha_1 = \gamma \alpha \), \( \alpha_2 = \gamma \beta \), and \( \alpha_3 = \gamma \).

4. DATA AND VARIABLES

Annual data are required to estimate the model and are collected for 56 countries for 1995 to 2000 from the ITU (2002) World Telecommunications Indicators Database. These data are comprised of GDP, mobile telephone subscription,
monthly mobile telephone subscription charge and population. Countries represented include 8 Low, 11 Lower-Middle, 9 Upper-Middle and 28 High income nations from Africa, Asia, Europe, the Middle East and the Western Hemisphere.

GDP is denominated in Special Drawing Rights (SDR) to offset the rapid appreciation in the USD during the mid- to late-1990s and deflated by the consumer price index (CPI) \((1995=100)\). CPI is obtained from the World Bank (2002) World Development Indicators Database. Deflated GDP series are divided by population to provide per capita INCOME series. Cellular mobile telephone subscribers per 100 inhabitants (SUBSCRIBERS) comprise analogue and digital users (CDMA, DAMPS, GSM, PCS and PHS systems). PRICE is constructed using the cellular monthly subscription charge denominated in SDR and deflated by the CPI index. Missing data for OECD member countries is sourced from the OECD Communication Outlook (1997, 1999, 2001). The remaining missing observation for the US (1997) is obtained from the Cellular Telecommunications and Internet Association’s Semi Annual Mobile Telephone Survey (2000). Other data are detailed in the Appendix.

Figure 1 and Figure 2 illustrate the relationship between SUBSCRIBERS against INCOME and PRICE. Indicated pair-wise correlations reveal expected relationships between SUBSCRIBERS and the explanatory variables INCOME and PRICE. Also evident is the high degree of variation by country, particularly for PRICE. Capello (1994) argues the limited PRICE influence is symptomatic of early adoption where endogenous network growth dominates the PRICE effect.
Three outliers in the upper-left segment of Figure 1 correspond to Korea, Portugal and Taiwan.

5. MODEL ESTIMATION

The estimation strategy employed for (9) is as follows. Equation (9) corresponds to the Pooled model that assumes mobile telephone demand is identical across country. Variation in demand by country requires that (9) be modified. The alternative specifications considered are the one-way Fixed-Effect (FEM) and Random-Effect (REM) models. The FEM allow intercepts to vary by country at a point in time and is depicted by:

\[
\Delta \text{Log}(\text{SUBSCRIBERS})_i = \alpha_{i0} + \alpha_i \text{Log}(\text{INCOME})_i + \alpha_i \text{Log}(\text{PRICE})_i - \alpha_i \text{Log}(\text{SUBSCRIBERS})_{i-1} + \varepsilon_{it}
\]

(10)

where subscript \(i = \{1, 2, 3, \ldots, 56\}\) is country specific. The REM model specification considers country variation is randomly distributed and uncorrelated with explanatory variables, the result is a complex disturbance term:

\[
\varepsilon_{it} = \alpha_{i0} + \nu_{it}
\]

(11)

and \(\nu_{it}\) is a white noise error process with zero mean and constant variance.
Table 1 reports the final results of the estimation of (10), which is conducted in stages. In Stage 1, the null hypothesis of no country-specific intercepts (or \( \alpha_{i0} = \alpha_{20} = \alpha_{30} = \ldots = \alpha_{40} \)) is tested using the Pooled model. Rejection leads to choice between FEM and REM specifications. A Hausman (1978) test of the correlation between the error and the regressors is used to check whether the REM is appropriate. A test of the significance of group effects rejects the Pooled model. Hausman’s (1978) test rejects the null that the REM estimator is efficient. The appropriateness of the FEM over the REM supports the use of dummy variables to control for country-specific effects or differences in the cross-country demand for mobile telephony. Finally, since a number of studies (e.g. Perl, 1983 and Ahn and Lee, 1999) have reported significant non-linear income effects, tests for non-linear income terms are conducted. Second-order income terms are found to be statistically insignificant. However, re-estimating (10) across the high-income countries results in substantially smaller coefficients. Finally, reported t-statistics indicate INCOME, PRICE and SUBSCRIBER\(_{1}\) are all significant.

The calculated PRICE and INCOME elasticities variables are also presented. The identified income elasticities are large and imply, for the global model, that a percent increase in income yields close to 4.8% increase in mobile subscription growth. Income elasticity for high-income countries is 27% less than the global model, but is also highly elastic. Large income elasticities provide an indication
that subscribers place high value on mobile telephony. Price elasticities for both models are inelastic and close in magnitude. Hence, price reductions will yield the same response in subscription growth, irrespective of location. The identified subscriber parameters (network effect) are 0.33 and 0.15 for global and high-income countries, respectively. This implies that for the global model, a 1% increase in subscribers yields an average 0.33% increase in network subscription growth. The network effect for high-income countries is approximately half of the global model. Given the higher penetration rates for high-income countries, the results indicate that the network effect is also non-linear. The effect appears to decrease with an increasing subscriber base, with the marginal effect least in high-income countries where upper critical mass is achieved. Nevertheless, the INCOME and SUBSCRIBER estimates show that rising GDP and subscription positively effects network size.

<Table 1>

*Impulse Response Function*

The plot of an impulse response function for PRICE and INCOME is provided by Figure 3 and visually depicts the behaviour of the SUBSCRIBERS series in response to INCOME and PRICE shocks (Enders, 1995). The impulse response function for an INCOME shock is

\[
\frac{\partial \text{SUBSCRIBERS}_{it}}{\partial \text{INCOME}_{i}} = \beta \gamma (1 + (1 - \gamma) + (1 - \gamma)^2 + (1 - \gamma)^3 + .... + (1 - \gamma)^t)(12)
\]
where \[ \frac{\partial \text{SUBSCRIBER}_{t+i}}{\partial \text{INCOME}_t} \] is the change in network size resulting from a unit INCOME shock at \( t \). \( \beta \) is the estimated INCOME coefficient, \( \gamma \) is the network externality and \( i \) is the number of countries. The corresponding impulse response function for a unit PRICE shock at \( t \) is:

\[
\frac{\partial \text{SUBSCRIBER}_{t+i}}{\partial \text{PRICE}_t} = \alpha \gamma (1 + (1 - \gamma) + (1 - \gamma)^2 + (1 - \gamma)^3 + ... + (1 - \gamma)^i). (13)
\]

Plot of shocks (12) and (13) are contained in Figure 3. Changes in INCOME are shown to have a more substantial effect on SUBSCRIBERS in successive periods. Indeed, for the global model, the cumulative impact of a percent change in income is 8.6 times larger than the price effect.

<Figure 3>

6. CONCLUSION

Global mobile telephony markets achieved substantial growth since their inception. Since 1990, from a base of 11 million the market has grown to over half a billion subscribers. Average global penetration at June 1999 is 27%. Advances in mobile technology from FG to 2G (and eventually 3G) have relaxed the spectrum constraint. Innovations in regulation have enabled entry of competitive operators into these former monopoly markets. The sum of these effects had seen declining mobile telephony prices, apparently further expanding
the market to attract marginal users. The purpose of this study is to model this exponential network growth in terms of economics drivers of income, price and network externalities without directly considering these institutional changes in individual markets.

Because only short time-series are available the modelling framework adopted is explicit utility maximization. The resulting econometric model is amenable to panel data estimation. Toward this end data are collected from ITU, UN, World Bank and IMF sources to construct national income, mobile telephony pricing and mobile subscription series (1995-2000) for 56 nations classified by GNP level. Panel data estimation of mobile subscription controls for cross-country heterogeneity. In particular, a pooled cross-section, time-series model, FEM and REM are estimated from the panel data set using OLS and GLS estimation techniques. The FEM is preferred and suggests GDP and the network externality effect are important in explaining network growth. Low-income countries are more income elastic. Network effects are inelastic, but nevertheless provide an important explanation for the rapid growth in mobile telephony. Moreover, both the income and network effects exhibit signs of non-linearity with the marginal effects reducing as subscription growth increases. Finally, price is shown to have a uniform effect across the two models and is inelastic. While price is clearly important, the impulse response functions highlight that increases in income will yield a cumulative subscription effect 8.6 times larger than the equivalent change in price.

However, to take comfort in this tentative conclusion requires better pricing data
that takes account of both subscription and use be employed. That is, the mobile telephony pricing data used here is for cellular monthly subscription only. A more complete pricing series would encompass both cellular connection charges and usage sensitive pricing. Another aspect of pricing that needs addressing in future studies is the impact of prepaid telephony cards. This form of mobile telephony usage sensitive pricing is particularly important for young users in developed economies, and more generally in developing economies.
### TABLE 1. Global Mobile Telephone Demand Elasticities

<table>
<thead>
<tr>
<th>Variable</th>
<th>Global Coefficient</th>
<th>t-statistic</th>
<th>Elasticity</th>
<th>High-Income Countries Parameter</th>
<th>t-statistic</th>
<th>Elasticity</th>
</tr>
</thead>
<tbody>
<tr>
<td>INCOME</td>
<td>1.57</td>
<td>3.83</td>
<td>4.76</td>
<td>0.52</td>
<td>2.09</td>
<td>3.47</td>
</tr>
<tr>
<td>PRICE</td>
<td>-0.18</td>
<td>-2.60</td>
<td>-0.55</td>
<td>-0.08</td>
<td>-1.83</td>
<td>-0.53</td>
</tr>
<tr>
<td>SUBSCRIBERS_1</td>
<td>-0.33</td>
<td>-10.45</td>
<td>-0.15</td>
<td></td>
<td>-5.32</td>
<td></td>
</tr>
<tr>
<td>$\bar{R}^2$</td>
<td>0.42</td>
<td></td>
<td></td>
<td>0.51</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

*Note.* t-statistics are in parentheses. The Hausman (1978) test rejects the REM specification. All coefficients are statistically significant at the 5% level. Parameter refers to the identified structural parameters derived from the estimated coefficients. INCOME and PRICE parameters are elasticities.
REFERENCES


Telephone Adoption. *Technological Forecasting and Social Change*, 57, 105-132.


National Statistics of Taiwan (2001). *Splicing Table of Consumer Price Indices in Taiwan Area 2001*. Available:


CAPTIONS TO ILLUSTRATIONS

Figure 1. SUBSCRIBER AND INCOME, 1995-2000

Figure 2. SUBSCRIBER AND PRICE, 1995-2000

Figure 3. INCOME AND PRICE IMPULSE RESPONSE FUNCTIONS
Figure 1. MOBILE SUBSCRIBERS AND INCOME, 1995-2000

Correlation=0.850

Note. Observations are six year averages for each country.
Figure 2. MOBILE SUBSCRIBERS AND MOBILE PRICE, 1995-2000

Correlation = -0.098

*Note.* Observations are six year averages for each country.
APPENDIX

The primary data source is the International Telecommunication Union World Telecommunication Indicators 2002 database. Missing data are sourced as follows.

*Consumer Price Index*

MOBILE TELEPHONY SUBSCRIPTION


Cellular Monthly Subscription Price

Nicaraguan Telecommunications Regulatory website at http://www.telcor.gob.ni/. This average value for 2002 was $417.97 (local currency unit) and did not include the ‘extra’ plans. Poland (1997, 1998 and 1999) sourced from Teligen. Monthly rental is the arithmetic average of subscription rates for pricing plans: Halo, White, Simply, Blue, Navy—Blue and VIP.

Gross Domestic Product


Residential Monthly Telephone Subscription Price

Ireland, Netherlands, Sweden (2000), is sourced Communications Outlook 2001, OECD from Table 7.18, page 204. Canada and Sweden (1998) are sourced from Communications Outlook 1999, OECD, Table 7.22, page 190. Missing observations for China (1995, 1996) sourced directly from staff at ChinaNex.com. Columbia (2000) was sourced from Colciencias, Colombian Institute for the Development of Science and Technology. The year 2000 residential monthly fixed line subscription price was taken directly from the National Nicaraguan Telecommunications Regulatory website at http://www.telcor.gob.ni/. It is defined there as the basic residential subscription.
price and is quoted in local currency unit. Further, it states on this website that this tariff maintains its value in relation to the US dollar as of the 10th of June 2000.

1 Gruber and Valletti (2003) provide a discussion of such developments with particular reference to the OECD.

2 Gruber and Verboven (2001) found that entry by a competitor into a national mobile telecommunications market slightly increased diffusion.

3 Roaming is the use of handsets with the same number in areas not covered by the firm the user subscribes to (Gruber and Valletti, 2003).


5 $U(Y,N)$ is based on duality theory. See Diewert (1974), and Train (1986, page 78) and Economides and Himmelberg (1995) for an explanation.

6 The two-stage instrumental variables technique is used for all models. In the first step, total mobile subscribers is regressed on current and previous period fixed-line prices and fixed-line subscribers, along with the previous period’s mobile price and mobile subscribers are used and a time index. Tests of homoeoscedasticity are rejected in the FEM and pooled models. Therefore,
generalised least squares is applied in estimation.