Hydrodynamics of binary mixture fluidization in a compartmented fluidized bed

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Abstract - The paper represents an extensive study of hydrodynamic characteristics of a fluidized bed in a pilot-plant-scale fluidized bed reactor designed for syngas production and power generation from biomass as a source of renewable energy. An air-blown compartmented fluidized bed gasifier permitting heat transfer between adjacent discrete compartments via solid circulation consists of two compartments, the combustor and the gasifier, operating at bubbling fluidized mode.

Results of numerical simulation of the fluidized bed containing monodispersed size Geldart B particles are represented. A three-dimensional Eulerian-eulerian granular model with closure laws according to the kinetic theory of granular flow is chosen to simulate the multiphase environs at 0.2 – 3.2 times minimum fluidization velocity.

The present work reports also experimental results on the fluidization of palm shell-sand binary mixtures of 2, 5, 10, and 15 wt% of feedstock including the minimum fluidization velocity of palm shell-sand binary mixtures, fluidization quality for different bed diameter, particle size, bed height, and superficial velocity. The vertical and lateral palm shells distributions in the mixtures are also discussed.

Keywords: Binary mixtures, fluidization, CFD, biomass

1. INTRODUCTION

Fluidized bed is selected for gasification process due to its effectiveness of heat and mass transfer between the gas and solid phases [1]. Although this process is considered as one of the oldest technologies and has been made successful in some industrial-scale production of renewable energy from biomass, generally this industry still faces a lot of challenges including the availability of economically viable technology, sophisticated and sustainable natural resources management, and proper market strategies under competitive energy markets [2].

Most of the present gasifiers are oxygen-blown to maintain its calorific value and to prevent nitrogen contamination in the product gas. Oxygen is obtained from air separation unit, which imposes heavy capital and operation unit, which impose heavy capital and operating costs to any conventional gasification plant.

Compartmented Fluidized Bed Gasifier (CFBG) (for an extensive list of references see [3]) is capable of producing high calorific value syngas (>11 MJ/Nm³) with full compatibility for existing power generation and chemical synthesis technologies, without the needs of pure oxygen. CFBD permits heat transfer between adjacent discrete compartments via solid circulation consists of two compartments, the combustor and the gasifier, operating at bubbling fluidized mode.

Wu et al. [4] has reviewed the various minimum fluidization velocity, \(U_{mf}\) correlations for multicomponents system. These correlations were based on two distinct features, either requiring the determination of single component \(U_{mf}\) or as a whole. The latter is more likely applicable to biomass as the components cannot be solely fluidized [5]. Rao et al. [5] developed correlation from a 5cm ID reactor using rice husks, sawdust and groundnut shell powder, up to 15 wt% with sands. Noda et al. [6] developed correlation using glass beads, wood, martén shot, soybean, small bean, and rubber with sands in 16cm ID column. It is found that the \(U_{mf}\) strongly depends on the mixing condition in the bed and on the volume fraction of the fluidizing medium. The authors have developed correlation with standard deviation of ±35%. All the above-mentioned correlations have not been tested using the present biomass/sand mixtures and in large reactor where the mixing state is very much scale-dependent.

Vertical and lateral mixing of palm shells in mixture is of great importance to the reactor performance as well. In fluidized bed, mixing mechanism is governed by bubble bursting and displacement, which provoke particles vertical and horizontal motion. A gas fluidized bed containing a mixture of particles of differing densities will segregate into two layers if the density ratio differs significantly from unity [7]. Some previous studies and reviews have been conducted to investigate mixing/segregating behavior in binary mixtures [4, 8-11]. Papers [4, 9] report data on equidensity binary systems, mixing characteristic of different particle densities and sizes (≤ 928μm) are represented in [10]. Shen et al. [11] studied binary system but limited to 2-D bed.

Despite of the fact that CFD is at the development stage for multiphase systems such as fluidized beds, numerical simulation allows getting round many problems related to complex and expensive experiment in fluidized bed. The Eulerian-eulerian model treating each phase as continuous and interpenetrating continuum is the preferred choice for simulating macroscopic hydrodynamic parameters due to relative simplicity and reasonable computational time. The bubbles motion and properties has been examined in 2D and 3D simulations [12, 13]. Paola et al. [14], reported that the 2D and 3D simulations show similar voidage profile and consistent formation, shape and size of bubbles for uniform shape of reactor. A few authors, [12-17], carried out the modeling using Geldart A and Geldart B particles incorporated with different drag laws.
In this study, the Eulerian-eulerian CFD model has been applied to study the hydrodynamics of CFBG in terms of the pressure drop, bed expansion and voidage profiles at the gasifier side. The simulated results are then compared with experimental results for model validation.

The objectives of this study are, first, to apply the Eulerian-eulerian CFD model for study of the hydrodynamics of CFBG in terms of the pressure drop, bed expansion and voidage profiles at the gasifier side, and secondly, to provide data and practical recommendations for pilot-scale CFBG from experimental investigation of binary mixture hydrodynamics.

Palm shell is selected as gasification feedstock in view of its great potential in feasibility of syngas production and due to its abundance supply since oil palm is ranked as number 1 fruit crops produced in year 2007 [2].

The experiments are carried out on fluidization of palm shell-sand binary mixtures of 2, 5, 10, and 15 wt% of palm shells in CFBG cold model of 66cm ID consisting of 2 compartments, combustor and gasifier with 2:1 ratio respectively, fluidized with air. The $U_{mf}$ of these mixtures of different wt% is determined and compared with published $U_{mf}$ correlations developed for small diameter column and different biomasses. Fluidization quality, $Q$, at different bed diameter, D, bed height, H, superficial velocity, $U_m$, and palm shell sizes and wt% are studied. The vertical and lateral palm shells distributions in these mixtures are also presented.

2. COMPUTATIONAL MODEL

The simulation of 3-D fluidized bed in the complex geometry CFBG is performed by using the CFD commercial package, FLUENT 6.3.26. A multi-fluid Eulerian-eulerian model, which considers the conservation of mass and momentum for the gas and fluid phases, supplemented by kinetic theory of granular flow to describe the solid phase stress can be summarized as below:

Mass conservation equations of gas (g) and solid (s) phases:

$$\frac{\partial}{\partial t} \left( \alpha_g \rho_g \right) + \nabla \cdot (\alpha_g \rho_g \mathbf{v}_g) = 0 \quad (1)$$

$$\frac{\partial}{\partial t} \left( \alpha_s \rho_s \right) + \nabla \cdot (\alpha_s \rho_s \mathbf{v}_s) = 0 \quad (2)$$

Momentum conservation equations of gas and solid phases:

$$\frac{\partial}{\partial t} \left( \alpha_g \rho_g \mathbf{v}_g \right) + \nabla \cdot (\alpha_g \rho_g \mathbf{v}_g \mathbf{v}_g) = -\alpha_g \nabla p + \nabla \cdot \tau_g + \alpha_g \rho_g \mathbf{v}_g \cdot \mathbf{v}_g + K_{gs} (\mathbf{v}_g - \mathbf{v}_s)$$

$$\frac{\partial}{\partial t} \left( \alpha_s \rho_s \mathbf{v}_s \right) + \nabla \cdot (\alpha_s \rho_s \mathbf{v}_s \mathbf{v}_s) = -\alpha_s \nabla p - \nabla \cdot \tau_s + \alpha_s \rho_s \mathbf{v}_s \cdot \mathbf{v}_s + K_{gs} (\mathbf{v}_s - \mathbf{v}_g)$$

(3)

(4)

Fluctuation energy conservation of solid particles

$$\frac{3}{2} \left[ \frac{\partial}{\partial t} (\rho_s \Theta_s) + \nabla \cdot (\rho_s \mathbf{v}_s \Theta_s) \right] = (p_s \mathbf{v}_s \mathbf{v}_s + \nabla (k_{bs} \nabla \Theta_s)) - \gamma_{bs}$$

Table 1: Momentum exchange coefficients

| Gidaspow drag function
| $K_{gs} = \frac{3}{4} C_D \frac{\alpha_s \rho_s}{d_s} \left| \mathbf{v}_g - \mathbf{v}_s \right|^2 \alpha_s^{-2.65}$ for $\alpha_s > 0.8$
| $K_{gs} = 150 \frac{\alpha_s^2 \mu_s}{d_s} + 1.75 \frac{\alpha_s \rho_s}{d_s} \left| \mathbf{v}_g - \mathbf{v}_s \right|$ for $\alpha_s \leq 0.8$
| $C_D = \frac{24}{\alpha_s \cdot Re_s} \left[ 1 + 0.15 \cdot (\alpha_s \cdot Re_s)^{0.687} \right]$ and
| $Re_s = \frac{\rho_s \cdot d_s \cdot \left| \mathbf{v}_g - \mathbf{v}_s \right|}{\mu_s}$

The constitutive equations as recommended in FLUENT user guide [18] are needed to close the governing relations. The momentum exchange coefficient can be calculated by specifying drag functions as shown in Table 1. Despite of rigorous mathematical modeling the drag laws used in the model continue to be semi-empirical in nature. Therefore, it is crucial to use a drag law that correctly predicts the incipient fluidization conditions. In this study, Gidaspow drag function is applied as it is proposed for modeling dense fluidized beds [18, 19].

The governing equations are solved by finite volume method. First-order discretization schemes for the convection terms are used. A time step of 0.001s with 10 iterations per time step is chosen. This iteration is adequate to achieve convergence.

Table 2: Simulation model parameters

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<tr>
<th>Description</th>
<th>Value</th>
<th>Unit</th>
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<tr>
<td>Height of reactor</td>
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<tr>
<td>Particle density, $\rho_p$</td>
<td>2620</td>
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<td>Air density, $\rho_a$</td>
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<td>Mean particle diameter, $d_p$</td>
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<td>μm</td>
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<td>Restitution coefficient</td>
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<td>-</td>
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<td>Initial volume fraction</td>
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<td>Superficial velocity, $U$</td>
<td>0.02 - 0.2</td>
<td>m/s</td>
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<tr>
<td>Static bed height</td>
<td>0.3</td>
<td>m</td>
</tr>
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<tr>
<td>Maximum number of iterations</td>
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<td>-</td>
</tr>
<tr>
<td>Convergence criteria</td>
<td>$10^{-3}$</td>
<td>-</td>
</tr>
</tbody>
</table>

The relative error between two successive iterations is specified by using a convergence criterion of $10^{-3}$ for each scaled residual component. The phase-coupled SIMPLE algorithm is applied for the pressure-velocity coupling. Table 2 gives a summary of the flow parameters to be used in the simulation of 3D fluidized bed (gasifier).
3. EXPERIMENTAL SETUP AND METHODOLOGY

A pilot-scale compartmented fluidized bed gasifier (Fig. 1) of the overall diameter of 0.66m with a height of 1.8m, partitioned into two compartments, the combustor and the gasifier, in a ratio of 65:35 respectively.

Perforated plate distributor is used to uniformly distribute the fluidizing agent, ambient air at free area of 0.27% and 0.32% for the gasifier and combustor accordingly. The air flow rate is regulated relative to the minimum fluidization velocity, $U_{mf}$, between 1-2.5$U_{mf}$ by rotameters (Fig. 2) to maintain the bubbling mode of fluidization. Pressure drops, $\Delta P$, are measured using water manometers at 3 different positions to indicate the total $\Delta P$, across the distributor and bed respectively. The inert particles used are the Geldart B particles, river sand, of 272 $\mu$m in mean size diameter and 2620 kg/m$^3$ in density. Palm shell with moisture less than 10wt% and density of 1200kg/m$^3$ consists of 3 mean diameter ($d_{ps}$) of 1.77, 3.55 and 13.95mm (with respective size ranges of 1.18-2.36, 2.36-4.75 and 4.75-9.20mm). The present work studies the fluidization of biomass-sand binary mixtures of 0 (no feedstock), 2, 5, 10, and 15 wt%. Design of the experimental set-up allows visual observation during the experiment.

The standard experimental approach in determining monodisperse $U_{mf}$ is based on defluidization stage of $\Delta P-U_{o}$ profile. $U_{mf}$ is estimated from the intersection point of the fixed bed line with the constant pressure line. Though the profile and consequently, the determination of binary $U_{mf}$ would generally be affected by different initial conditions [9], the defluidization stage where the components are already mixed is preferred because they are more representative of binary system existing as a “single” bed material.

For the fluidization quality, $Q$, defined as experimental bed pressure drop / static weight per unit area, the bed $\Delta P$ is computed by subtracting distributor $\Delta P$ from total $\Delta P$.

"Thief" probe (diameter 5cm) and sieving method are preferred due to fast response and the ability of collecting samples while the bed is fluidized at different locations in the bed under various operating conditions.

The probe is removed vertically from the bed. The mixtures is then sieved and weighed to determine their component weight fraction.

Prior to the experiments, sands are filled to desired weight/height and packed. Palm shells are then uniformly stacked on the bed surface forming two segregated layers. This approach is selected to track palm shell migration. The $U_{mf}$, $Q$, and solids mixing behavior are simultaneously measured. Solid sample is collected from 3 different sections (v-valve, center and riser) in 3 different levels (L1 to L3 indicating top, center, bottom), which constitutes 9 imaginary cells ($n$) shown in Fig. 3.

Data on mixing is presented graphically such that the deviation of the perfect mixing line indicates segregation. Vertical or lateral mixing index, $m$, is defined as local palm shell wt% / load palm shell wt% or ($x/X$). $m=1$ represent perfect mixing, while segregation may lead to two conditions, either “dilution” ($m<1$) or accumulation ($m>1$).

Assuming that 9 locations are able to represent the whole bed composition, the overall mixing index, $M$, can therefore
be computed, in absolute terms according to the equation

\[ M = 1 - \left( \frac{1}{n} \sum\left( \frac{\text{local PS wt\%} - \text{load PS wt\%}}{\text{load PS wt\%}} \right) \right) \]  

(6)

Values \( m=1 \) and \( m<1 \) correspond to perfect mixing and segregation respectively. Three repetitive data are taken in each location with standard deviation of ±15%. Each set is in 15 minutes interval to allow steady state. Shen L.H et al. [11] observed that equilibrium mixing is achieved in 10 seconds. Notwithstanding the measurement for the study of the effect of bed height to \( Q \) and mixing, all the experiments are conducted at constant total bed weight of 77kg.

4. RESULTS AND DISCUSSION

COMPARISON OF NUMERICAL SIMULATION WITH EXPERIMENTAL RESULTS

The CFD simulations are carried out under transient state condition. Various superficial gas velocities from 0.02 to 0.2 m/s, which correspond to 0.3 – 3.2 \( U_{mf} \), are examined.

A comparison of the time-averaged bed pressure drop against superficial gas velocity is plotted in Fig.4. At \( U < U_{mf} \), the simulation results overestimate the bed pressure drop. The results show better agreement at velocities greater than \( U_{mf} \). This discrepancy at lower velocities may be attributed to the dominant interparticle frictional forces, which are not predicted by the multi-fluid model for simulating gas-solid phases [20]. Moreover, the drag model employed does not take into account effect of complex geometry at the gasifier side. The standard deviation of ±10% is observed for the simulation results in comparison with experimental results.

As can be observed in Fig. 4, the \( U_{mf} \) cannot be determined from the simulated results using typical pressure drop vs velocity profile. However, it can be obtained from the interception point of the constant expansion ratio line at \( U < U_{mf} \) during static state with the gradual increased expansion ratio line for \( U > U_{mf} \) where the bed expands in Fig. 5. The numerically obtained \( U_{mf} \) is 0.057 m/s as compared to the experimentally determined \( U_{mf} = 0.062 \) m/s.

Fig. 5 shows a contour plot of solids fraction viewing at the central part of gasifier front wall. At time 0.0s, the bed remains static. At early stage, waves of voidage are created (probably analogous to the continuity waves [21]), which travel through the bed and subsequently break to form bubbles as the process progresses. The bed height increases with bubble formation until it levels off at a steady-state bed height. The chaotic transient generation of bubble formation can be seen after 2.0s.

The fluidization quality, \( Q \), is defined as the ratio of experimental bed pressure drop to the static weight per cross sectional area of the bed. As can be seen from Fig. 7, no distinctive differences are observed with increase in bed height. The average quality over the range is approximately 0.8. The behavior of the fluidization is, in fact, an indication of channeling bed, where there is localized de-fluidization that leads to not fully suspended bed at gasifier. More
studies have been carried out on the quality aspect elsewhere [22, 23].

![Fluidization quality, Q, versus U/U\text{mf} at different bed height](image)

**EXPERIMENTAL DATA ON BINARY MIXTURE**

Generally, an increase in palm shell size or wt% leads to an increase in \(U_{mf}\). From Table 3, it is obvious that Noda’s et al. [6] correlation developed from combination of the component \(U_{mf}\) is not applicable to the mixtures where the biomass can not be solely fluidized, similarly to that high - lighted by Bilbao et al. [24] in sand/straw binary mixtures. Rao et al. [5] prediction is relative closer but significantly underestimates due to different bed characteristics, e.g. the sphericity and bed incipient porosity (\(\phi=0.86, \varepsilon_{mf}=0.42\)) differ from those for the present system (\(\phi=0.54, \varepsilon_{mf}=0.34\)).

![Table 3. Experimental (Exp) data, correlations results and percentage error (ER%) for various palm shell size and wt%](image)

**Fluidization Quality**

Experiments show, the increase in the bed diameter and palm shell sizes provides no significant changes in the Q value for the binary components. There were no also distinctive changes in the Q value with different bed aspect ratio, H/D (constant D, increasing H). A through-channeling is observed, and fluctuation becomes more intense with the increase in palm shell wt% (a single component bed has higher Q value than binary component in gasifier, and in single component experiments, the through-channeling changes to intermediate-channeling as the particle diameter increases). In Fig. 8 (from here on, experimental data for the palm shell size \(d_{ps} = 3.53\) mm are presented), \(Q = 0.8\) in single component while \(Q\) fluctuates between 0.6-0.7 in binary mixtures. This is due to the differing shape, size and density of the binary components, leading to more severe local pressure/density variation. Rhodes [25] stated that bubbles formed in group B and D particles will continue to grow but never achieve a maximum size associated with large pressure fluctuations.

Palmshell used in this study and classified as Geldart D [26] has a tendency to produce spouted beds. The effective particle size and bed voidage will increase while the effective density decreases, when the palm shell wt% increases in the mixtures. Abdullah et al. [27] stated that bulk density and voidage are the two main factors contributing to the bed fluidization quality.

![Vertical and lateral mixing](image)

**Vertical and lateral mixing**

Figure 9 shows the typical palm shell vertical distribution at various \(U_{mf}\) for 10 wt%-load of palm shell. Vertical mixing enhances with the \(U_{mf}\) increase approaching maximum accumulated value is \(M=10\), if a collected sample is purely palm shell. However, palm shells with lower density, tends to migrate towards the bed surface due to easiness of being swept away by the air through flow from distributor and carried up by rising bubbles. At higher \(U_o\), (2.0-2.5 \(U_{mf}\)), palm shells tend to become uniformly mixed, resulting in a smaller palm shells concentration gradient developed along the bed height.

Typical palm shell lateral distribution with various \(U_{mf}\) is shown in Fig. 10. Overall, the \(M\) indexes of three layers improve with increasing \(U_o\).

Lateral mixing of solids in a gas solid fluidized bed is caused by two mechanisms, which are bursting bubbles at the bed surface and bubbles displacement inside the bed [26]. At 1.25\(U_{mf}\) lateral mixing is initiated by bursting bubbles at the bed surface where a large fraction of the palm shells at the centre is dispersed. At L2 and L3, the mixing induced by bubbles displacement is insignificant. With increasing \(U_o\) (from 1.5 to 2.5\(U_{mf}\)), lateral palm shells distributions across fluidized bed at L1, L2, and L3 approach each other due to increasing bubbling rate, whereby lateral mixing induced by bubbles displacement...
becomes more significant resulting in enhanced lateral mixing.

Generally, the increase of superficial velocity $U_o$ will improve mixing in segregated systems of mixtures with different densities/sizes [28]. Shen et al. [29] reported that the wake exchange coefficient, which indicates vertical and lateral solid mixing intensity, reduced with the increase in $U_{mf}$. On the contrary, in Fig. 11, $M$-index increases although $U_{mf}$ increases with palm shell wt%. This is likely due to the increase in $\varepsilon_{mf}$ (Table 4) that leads to greater bed expansion, allowing effective vertical and lateral solid mixing.

In Fig. 12, maximum overall mixing index is achieved at $1.5U_{mf}$ for deep bed, whereas at shallow bed, the same degree of mixing is only achievable at higher $U_o$ ($\geq 2U_{mf}$).

With increasing bed height, the bed pressure drop increases resulting in a stable bubbling across bed distributor and uniform mixing of the fluidized bed. Conversely, in shallow beds, where the total bed pressure drop is reduced, the local preferential channeling forms. This contributes to non-uniform bubbling at the expense of the rest of the bed [30]. Therefore, if $U_o$ is held constant, poorer mixing occurs with a sensitivity to bed height in shallow beds and relatively good mixing in deep beds.
5. CONCLUSION

Numerical simulation shows reasonably well agreement with experimental results in terms of bed pressure drop, bed expansion ratio and minimum fluidization velocity.

From experimental study of CFBG hydrodynamics it follows that the minimum fluidization velocity correlations developed from small-scale laboratory reactors and different biomasses could not be extended to the present system. No significant effect on the fluidization quality value with respect of different geometry, particle sizes, bed height, and wt% of palm shells and through-channeling is observed throughout the experiments. However, it is found that the single component demonstrates the higher fluidization quality values compared with those for binary mixtures. It is interesting to note that uniform mixing is attainable for binary system studied even though the fluidization quality value less than 0.8.

As for mixing/segregation, the mixing indexes \( m \) and \( M \) increase with the superficial velocity increase. The bed diameter has more dominant effect as compared to the wt% and size of the feedstock; larger bed diameter and bed high require lower superficial velocity to achieve good mixing. There is an optimum value of the velocity where uniform mixing \( (M \geq 0.85) \) can be established, and it is found to be 1.5-2 times the minimum fluidization velocity over the whole range of experimental parameters studied.

6. NOMENCLATURE

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<tr>
<th>Symbol</th>
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<td>( e_{ss} )</td>
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**Greek letters**

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<td>( \alpha )</td>
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Subscripts
g  gas
mf  minimum fluidization
s  solids

REFERENCES