1	Fracturing Process Analysis of the Beishan granite Based on
2	Acoustic Emission and Strain Energy under True Triaxial
3	Compression
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30 Abstract

The study of rock fracturing is a fundamental research in rock mechanics and engineering. In this paper, based on the complete stress-strain curves under TTC, the corresponding AE and strain energy results, the mechanical properties and fracturing process of the Beishan granite are studied. A representative test result (σ_2 =75 MPa, σ_3 =20 MPa) is selected to analyse and illustrate the three-dimensional fracturing process of the Beishan granite. The results show that the variations in the brittle fracture behaviours, AE and strain energy characteristics of the Beishan granite change with σ_2 or σ_3 following certain relationships and the mechanisms driving these various relationships are very different. The AE and strain energy characteristics during the five fracturing evolution stages of the Beishan granite are also quite different. The variations of the increments of AE count, AE event and total elastic strain energy per unit time $(\Delta S_c/\Delta t, \Delta S_c/\Delta t \text{ and } \Delta U_c/\Delta t)$ are mainly studied with the different time and stress level during the rock failure. The rock fracturing evolution process can be illustrated with deep insight through the variation of these parameters. This research gives a perspective to study the deep underground fracture formation processes such as earthquake, tunnel sudden failure, spalling, splitting and rockburst. Keywords: Fracturing process; Acoustic emission; Strain energy; Beishan granite; True triaxial compression

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63 1. Introduction

64 The occurrence of hazards in natural and engineered cases such as spalling and rockburst in deep underground rock engineering is related to the evolution of the true triaxial stress field ($\sigma_1 >$ 65 $\sigma_2 > \sigma_3$) in which the rock mass is located.¹ Research on the fracturing of deep rock masses by 66 laboratory true triaxial testing is quite helpful for studying the evolution and mechanisms of 67 various hazards.²⁻⁴ Many research methods have been applied to study this problem. However, due 68 69 to the limitations of observation techniques and methods, it is still more difficult to monitor and 70 quantify the initial position of micro-cracks inside a rock and thus the dynamic evolution of 71 cracks.

72 Acoustic emission (AE) can directly reflect the internal damage of rock during the evolution of deformation and failure.^{5,6} The relationships of the AE characteristic parameters that change 73 74 with time and stress can visually express the crack initiation rate in rock at different damage 75 development stages. The AE hypocenter location technique can stereoscopically show the spatial 76 location, spatial morphology, initiation rate and propagation direction of cracks. 7-10 Many applications of the AE technique have been carried out in rock studies, mainly focusing on four 77 aspects: the AE time series,¹¹ AE spectrum characteristics,¹² AE spatial distribution¹³ and AE 78 79 mechanism.¹⁴ AE has been proven to be one of the best ways to study dynamic crack propagation.

By utilizing strain energy theory, the rock fracturing process can be totally analysed and interpreted.^{15,16} The energy evolution mechanism is closely related to the micro-cracking and damage state inside the rock. The rock fracturing is a process of energy input, elastic strain energy accumulation, energy dissipation and energy release.^{17,18} Most of the research on strain energy is focused on three aspects about the experiments study of energy evolution process and characteristic,¹⁹ energy-based constitutive relations, criteria and index,²⁰ numerical simulation of energy evolution.²¹

In this study, a series of true triaxial compression (TTC) tests of the Beishan granite are carried out. Some tests are monitored by AE, and strain energy analysis is also used to study the test results. Furthermore, the stress–strain relationship, AE and strain energy characteristics of the Beishan granite under different TTC stress states are studied. The spatial fracture evolution of a representative test result are also investigated. This research offers a helpful insight to internal 92 mechanism of rock fracturing and hazards formation and possible timely prevention.

93 2. Methodology

94 2.1. Rock description and specimen preparation

The Beishan area is located in Gansu Province in Northwestern China, which has been preliminarily chosen as the preferred area for China's potential high-level radioactive nuclear waste (HLW) repository.^{22,23} The Beishan granite tested in this study is medium- to coarse-grained monzonitic granite with relatively good isotropy (Fig. 1). Some basic physical and mechanical properties of the tested Beishan granite are presented in Table 1.

100 The specimens of the Beishan granite used in the TTC tests are rectangular prisms with 101 dimensions of $50 \times 50 \times 100$ mm³. The flatness and roughness of the specimen ends are controlled to 102 no more than 10 µm and 3 µm, respectively. The tolerances for the end surface dimensionality and 103 perpendicularity are limited no more than ± 0.01 and ± 0.02 mm, respectively. To reduce the 104 experimental error and the differences among the specimens, all the specimens are taken from the 105 same block of granite rock and in a consistent sampling direction.

106 **2.2. Testing apparatus and methods**

The TTC tests in this study are performed using the novel true triaxial testing apparatus at 107 Northeastern University in China. The deformations in the ε_1 and ε_2 directions are measured by 108 109 mini linear variable differential transformers (LVDTs), and the deformations in the ε_3 directions are measured by a beam type strain gauge, which can determine the centre point of the 110 111 deformation of the specimen in the ε_3 direction. A series of anti-friction measures are adopted, and the friction coefficient is reduced to 0.02.²⁴ Detailed descriptions of the true triaxial testing 112 apparatus can be found in Feng et al.² The PCI-2 AE system is also used during the TTC tests in 113 114 this study. Improved high-frequency and anti-pressure AE sensors are developed, to make the AE signal as much as possible and the noise as little as possible, the AE amplitude threshold is finally 115 116 selected to be 45 dB. Because the rock specimen is covered by four metal fixtures in the σ_1 and σ_2 directions, the AE sensors can be mounted on only the two specimen faces in the σ_3 direction. 117 Eight AE sensors are mounted on these two faces of the specimen; the distribution of the AE 118 119 sensors is shown in Fig. 2.

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The stress paths used for the TTC tests in this study are as follows (Fig. 3): At the beginning of the test, σ_1 , σ_2 and σ_3 are simultaneously loaded to the preset σ_3 value at a rate of 0.5 MPa/s. Then, σ_3 is kept constant, while σ_1 and σ_2 are simultaneously loaded to the preset σ_2 value at a rate of 0.5 MPa/s. Finally, σ_2 and σ_3 are kept constant, while σ_1 is loaded at a rate of 0.5 MPa/s; when σ_1 approaches the damage stress σ_{cd} , the loading method is changed to load σ_1 with a rate of 0.015 mm/min in ε_3 until the rock specimen failure.

126 **3. Experimental Results**

127 3.1. Stress–strain relationships of the Beishan granite under TTC

128 The strength and deformation properties of rocks under various true triaxial stress conditions are diverse. Fig. 4 shows the variation in the stress-strain relationships of the Beishan granite with 129 different σ_2 values under TTC. When σ_3 is constant ($\sigma_3=5$ MPa) and the σ_2 values are set to 20 130 131 MPa, 75 MPa, 100 MPa and 150 MPa, the peak strengths (σ_1) of the Beishan granite are 267.8 132 MPa, 300.4 MPa, 316.1 MPa and 281.9 MPa, respectively, while the peak strains (ε_1) are 0.68 %, 133 0.62 %, 0.58 % and 0.36 %, respectively (Fig. 4). Therefore, under TTC stress state, the rock failure strength first increases and then decreases with increasing σ_2 , and the peak strain of the 134 rock decreases with increasing σ_2 , which is consistent with previous research results.^{2,25,26} Results 135 136 also shows that, with the increase in σ_2 , the rock tends to experience brittle failure (Class II 137 failure), and the stress drop at post-peak of the stress-strain curve is more obvious, which 138 indicates that an increase in σ_2 makes the rock more inclined to brittle failure. In addition, with the 139 increase in σ_2 , the σ_1 - ε_2 curve and the σ_1 - ε_3 curve of the rock become increasingly bifurcated, that 140 is, the difference between ε_2 and ε_3 increases with increasing σ_2 . Therefore, under TTC stress state, 141 the control of σ_2 on rock deformation is very important; the larger the difference between σ_2 and σ_3 142 is, the greater the difference between ε_2 and ε_3 .

Fig. 5 shows the variation in the stress-strain relationships of the Beishan granite with different σ_3 values under TTC. We found that when σ_2 is constant ($\sigma_2=75$ MPa) and the σ_3 values are 5 MPa, 10 MPa, 20 MPa and 30 MPa, respectively, the peak strengths (σ_1) of the Beishan granite are 300.4 MPa, 353.4 MPa, 437.1 MPa and 495.9 MPa, respectively, and the peak strains (ε_1) are 0.62 %, 0.75 %, 0.81 % and 0.9 %, respectively (Fig. 5). Therefore, the rock failure strength and peak strain increase with increasing σ_3 under TTC conditions. The rock ductility 149 (Class I failure) tends to increase with increasing σ_3 , indicating that an increase in σ_3 weakens the 150 rock brittleness. Moreover, comparison of Fig. 5a to Fig.5d shows that, when σ_3 is increased by 25 151 MPa, the failure strength of the rock is increased by 195.5 MPa. However, comparison of Fig. 4c 152 with Fig. 4a reveals that, when σ_2 is increased by 80 MPa, the failure strength of the rock is 153 increased by only 48.3 MPa. Therefore, the influence of σ_3 on the strength of the Beishan granite 154 is much greater than the corresponding influence of σ_2 .

155 3.2. Strain energy characteristic of the Beishan granite under TTC

Firstly, it should be declared that the strain energy in this paper actually means the strain
energy density. When calculating the strain energy under TTC, for any time step *t* during the test,
27-29

the total strain energy U of rock can be calculated through Eq. (1), 27-29 as shown in follows:

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$$U = U_1 + U_2 + U_3 = \int_0^{\varepsilon_1} \sigma_1 d\varepsilon_1 + \int_0^{\varepsilon_2} \sigma_2 d\varepsilon_2 + \int_0^{\varepsilon_3} \sigma_3 d\varepsilon_3$$
(1)

160 where ε_1^t , ε_2^t and ε_3^t are the strains per unit volume of rock corresponding to σ_1 , σ_2 and σ_3 161 at any time step *t*, respectively.

162 It is assumed that the physical process of rock deformation and failure under TTC is a closed 163 system without heat energy exchange with the external environment. The total strain energy U of 164 rock can be divided into two parts: the elastic strain energy U^e and the dissipated strain energy 165 U^d . The elastic strain energy U^e can be calculated through Eq. (3), the dissipated strain energy 166 U^d can be obtained through Eqs. (2) and (3),^{15,30,31} as shown in follows:

$$U = U^e + U^d \tag{2}$$

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$$U^{e} = U_{1}^{e} + U_{2}^{e} + U_{3}^{e} = \int_{0}^{\varepsilon_{1}^{e}} \sigma_{1} d\varepsilon_{1}^{e} + \int_{0}^{\varepsilon_{2}^{e}} \sigma_{2} d\varepsilon_{2}^{e} + \int_{0}^{\varepsilon_{3}^{e}} \sigma_{3} d\varepsilon_{3}^{e}$$
(3)

169 where U_1^e , U_2^e and U_3^e are the elastic strain energy per unit volume of rock corresponding to 170 σ_1 , σ_2 and σ_3 , respectively. ε_1^{et} , ε_2^{et} and ε_3^{et} are the elastic strains per unit volume of rock 171 corresponding to σ_1 , σ_2 and σ_3 at any time step *t*, respectively.

Fig. 6 shows the time history curves of the complete energy evolution of the Beishan granite under the same TTC stress states. The time history curves of the total strain energy U, total elastic strain energy U^e and total dissipated strain energy U^d and the strain energy U_1 , elastic strain energy U_1^e and dissipated strain energy U_1^d corresponding to σ_1 are shown in Fig. 6a, c, e. The time history curves of the total strain energy U_2 , elastic strain energy U_2^e and dissipated strain energy U_2^d corresponding to σ_2 and the total strain energy U_3 , elastic strain energy U_3^e and dissipated strain energy U_3^d corresponding to σ_3 are shown in Fig. 6b, d, f. The complete stress-strain curves of the Beishan granite corresponding to the abovementioned stress levels are shown in Fig. 4b, d and Fig. 5c.

181 Notably, the pre-peak strains corresponding to σ_2 and σ_3 undergo a change: they first increase 182 and then decrease, that is, the strain is not monotonically increasing (Fig. 4 and Fig. 5). The strain 183 and strain energies corresponding to σ_2 and σ_3 during the pre-peak stage transform from 184 loading-induced compression and energy storage to loading-induced dilation and energy 185 dissipation. Therefore, the strain energy values of the Beishan granite corresponding to σ_2 and σ_3 186 are first positive and then become negative as the test continues (Fig. 6b, d, f). When the difference between σ_2 and σ_3 is large, this change is particularly obvious on the resultant time 187 188 history curves of strain energy (Fig. 6d).

The strain energy evolution processes of the Beishan granite are basically similar at pre-peak 189 190 while they are very different at post-peak under different TTC stress states. In general, the 191 pre-peak plastic deformation of the Beishan granite under the above TTC stress states is not 192 remarkable. Therefore, although a certain strain energy dissipation occurs in the Beishan granite 193 during the pre-peak stage, the magnitude is not large. The time history curves of the pre-peak total 194 strain energy U and total elastic strain energy U^e coincide or are parallel. The two curves begin 195 to bifurcate after reaching the stress yield point, decreasing the rate of increase in the total elastic strain energy U^e , while the rate of increase in the total dissipated strain energy U^d increases 196 197 (Fig. 6a, c, e).

198 The time history curves of the strain energy at post-peak are complicated due to the 199 formation of macroscopic fractures in Beishan granite. When σ_2 is relatively small, the strain 200 energies corresponding to σ_2 and σ_3 are smaller than that corresponding to σ_1 , so the variation 201 trends and differences of the total strain energy U, the total elastic strain energy U^e and the total 202 dissipated strain energy U^d of the Beishan granite at post-peak are similar to the strain energy U_1 , 203 the elastic strain energy U_1^e and the dissipated strain energy U_1^d (Fig. 6a). When σ_2 is relatively 204 higher, the strain energies corresponding to σ_2 and σ_3 are relatively higher than that corresponding to σ_1 . The higher σ_2 has a great influence on the variation trends and differences of the total strain energy U, the total elastic strain energy U^e and the total dissipated strain energy U^d of the Beishan granite at post-peak compared to the strain energy U_1 , the elastic strain energy U_1^e and the dissipated strain energy U_1^d (Fig. 6c). It can be depicted that the variation trend and differences of the total dissipated strain energy U^d of the Beishan granite at post-peak is quite different from the dissipated strain energy in the σ_1 direction (Fig. 6c).

211 3.3. AE characteristic and AE hypocenter location of the Beishan granite under TTC

Fig. 7a, b show the time history curves of the stress (σ_1), AE count and cumulative AE count 212 and the corresponding failure behaviour of the Beishan granite under σ_2 =75 MPa and σ_3 =5 MPa. 213 214 Fig. 7c, d show the same situations of the Beishan granite under $\sigma_2=150$ MPa and $\sigma_3=5$ MPa. The maximum AE count of the Beishan granite in Fig. 7a and Fig. 7c are occurred at the stress peak 215 points and are 18222 and 32320, respectively. The cumulative AE count at pre-peak are 74415 and 216 1043990, respectively; however, they are 1649305 and 18910927 at the end of the test, 217 218 respectively. The comparison shows that when σ_3 is constant ($\sigma_3=5$ MPa) and $\sigma_2=150$ MPa, the AE count and cumulative AE count of the Beishan granite are considerably higher than those under 219 220 σ_2 =75 MPa. From the perspective of AE, more severe brittle failure characteristics can be 221 observed at higher σ_2 values, the AE count and cumulative count increase even by a magnitude 222 (Fig. 7a, c). Meanwhile, when $\sigma_2=150$ MPa, the Beishan granite exhibits only one macroscopic fracture surface dominated by tensile failure (Fig. 7b). When $\sigma_2=75$ MPa, the Beishan granite 223 exhibits two macroscopic fracture surfaces, many secondary micro-cracks are also observed near 224 the main fracture surfaces (Fig. 7d). This trend also indicates that the brittle fracture characteristics 225 226 of the Beishan granite become more obvious with increasing σ_2 .

227 When $\sigma_2=75$ MPa, the number of macroscopic fracture surfaces and micro-cracks in the 228 Beishan granite are much greater than those when $\sigma_2=150$ MPa. However, when $\sigma_2=75$ MPa, the 229 overall AE activity in the Beishan granite is lower than that when $\sigma_2=150$ MPa. This may be 230 because when σ_2 is higher, the brittle failure of rock is more intense, the time from localized 231 failure to macroscopic fracture of rock is relatively short, thus the rate of crack propagation is 232 relatively high. Although the number of macroscopic fracture and micro-cracks is relatively small, the overall intensity and amplitude of the AE signal are relatively higher during rock fracturing,
which increases the overall AE activity of the Beishan granite.

235 Fig. 7e, f show similar conditions as Fig. 7a, b of the Beishan granite when σ_2 =75 MPa and 236 $\sigma_3=20$ MPa. The maximum AE count of the Beishan granite in Fig. 7a and Fig. 7e are occurred at 237 the peak stress point and the post-peak maximum stress drop point and are 18222 and 15489, 238 respectively. The pre-peak cumulative AE count are 74415 and 416212, respectively; however, they are 1649305 and 4527006 at the end of the test, respectively. When σ_2 is constant (σ_2 =75 MPa) 239 240 and $\sigma_3=20$ MPa, the maximum AE count of the Beishan granite is slightly lower than that when σ_3 =5 MPa. However, the cumulative AE count at σ_3 =20 MPa is greater than that at σ_3 =5 MPa, both 241 242 at pre-peak and at the end of the test (Fig. 7a, e). It can be found that when $\sigma_3=20$ MPa, the 243 number of macroscopic fracture surfaces and micro-cracks in the Beishan granite is considerably 244 higher than that when $\sigma_3=5$ MPa (Fig. 7b, f). This is because when σ_3 is higher, the time from 245 localized failure to macroscopic fracture of rock is relatively longer, thus the micro-cracks are 246 more developed and more cracks are produced. Therefore, with more AE signals are generated by 247 rock cracking, the cumulative AE count increase.

248 Fig. 8 shows the fracturing evolution of the Beishan granite based on an analysis of the AE hypocenter location under TTC (σ_2 =75 MPa, σ_3 =20 MPa) at different times and stress levels. Fig. 249 8h shows the fracture morphology characteristics and the reference coordinate system of the 250 251 Beishan granite during final failure. Comparing the actual crack distributions (Fig. 8f, j) of the 252 rock along plane ABCD and plane A'B'C'D' (Fig. 8h) and the corresponding AE hypocenter 253 location results (Fig. 8g, i) shows that the two results are very consistent, which indicates that the 254 AE hypocenter location results can accurately reflect the fracture morphology characteristics and 255 fracture evolution during the final failure of the rock.

Fig. 8a, b, c, d, e show the AE hypocenter location results of the Beishan granite at 365 s, 595 s, 1250 s, 1625 s and 3348 s corresponding to 43 %, 71 %, 100 %, 88 % and 37 % of the peak stress, respectively. Influenced by the composition and microstructure of the Beishan granite and the loading boundary conditions, different damage accumulations form a complex and variable rock fracturing process. According to the difference in damage evolution and accumulation in the rock, the AE hypocenter location results in the four elliptical regions in Fig. 8 are divided into three types, distinguished by three colours: red, blue and green. The analysis of these three typical 263 damage evolution and accumulation processes of the Beishan granite under the given TTC stress 264 state (σ_2 =75 MPa, σ_3 =20 MPa) is shown as follows:

(1) Fig. 8a-e show that when the rock is under 43 %, 71 %, and 100 % of the peak stress (Fig. 265 8a-c), there are almost no AE hypocenter location points in the blue elliptical region of the lower 266 left and upper right corners of the rock specimen. When the stress decreases from 100 % to 88 % 267 268 of the peak stress (Fig. 8d), more AE hypocenter location points are concentrated in the blue 269 elliptical region, and until the final failure of the rock specimen (Fig. 8e), the AE hypocenter 270 location points in this region only slightly increase. Therefore, in practice, the lower left and upper 271 right corners of the rock specimen along the X-Y plane (Fig. 8f, j) are not destroyed before the 272 stress peak is reached, but sudden fracturing occurs in these areas during the first post-peak stress 273 drop. This behaviour may be due to the sudden change in the stress rate and strain rate during the 274 stress drop process, amplifying the stress concentration effect between the edge angle of the rock 275 specimen and the rigid indenter and leading to a final and sudden failure of the rock.

276 (2) The AE hypocenter location points in the red elliptical region in Fig. 8a-e show a random 277 and irregular scattering from the early loading (Fig. 8a), and the number of AE hypocenter 278 location points in this region grows with the rises of stress up to the rock macro fracturing or 279 overall failure (Fig. 8e). This process indicates that with the incremental change in stress state, the 280 micro-cracks of the rock in this area transform from a random irregular distribution to gradually aggregating along an internal fracture surface, which then gradually coalesces to form a 281 282 macroscopic fracture surface. This process generally results in the progressive formation of 283 complex fractured bands or regions consisting of multiple macroscopic fractures and 284 micro-cracks.

285 (3) Unlike the above two regions, the green elliptical region in Fig. 8a-e does not exhibit AE 286 hypocenter location points when the rock is under only 43 % of the peak stress (Fig. 8a). A small 287 number of AE hypocenter location points begin to appear in the green elliptical region when the 288 rock is under 71 % of the peak stress (Fig. 8b), which indicates the development of micro-cracking inside the rock. When the rock is under 100 % of the peak stress (Fig. 8c), the AE hypocenter 289 290 location points increase and concentrate at the tip of the green fracture surface, as shown in Fig. 291 8h. When the stress decreases from 100 % to 88 % of the peak stress (Fig. 8d), a large number of 292 AE hypocenter location points concentrating near the macroscopic fracture surface appear in the

green elliptical region, and the macroscopic fracture surface is basically throughgoing. Then, the AE hypocenter location points in this region only increase in number and do not change the overall shape and trend of the macroscopic fracture surface. Unlike the above two cases, the crack initiation and propagation within the green elliptical region is relatively quick, and fractures will quickly penetrate the rock specimen, representing a failure behaviour between sudden failure and progressive failure.

299 4. Discussion

300 4.1. Fracturing process analysis combining the AE and strain energy characteristic301 parameters

302 The rock fracturing can be precisely captured by AE and it is also a energy evolution process.^{15,18} Hence, the entire fracturing process of the Beishan granite under TTC is studied by 303 304 combining AE and strain energy characteristics in this section. Fig. 9 shows the complete 305 fracturing process of the Beishan granite under TTC (σ_2 =75 MPa, σ_3 =20 MPa) in terms of the AE and strain energy characteristics. The time history curves of σ_1 , the AE and strain energy 306 307 parameters are shown in Fig. 9a-e. Additionally, according to the different damage evolution and accumulation processes, the complete stress-strain curve under TTC (Fig. 9a) can be divided into 308 309 five stages: micro-cracks closure (OA), elastic deformation (AB), stable propagation of 310 micro-cracks (BC), accelerated extension of cracks (CD) and post-peak strength loss and residual 311 shearing (DE).

During the micro-cracks closure stage (OA), the original micro-cracks and micro-defeats of 312 the rock are compacted and closed, and the internal particles become interlocked. Therefore, a 313 314 small number of AE signals are generated at this stage, and the AE count and the cumulative AE 315 count are relatively low (Fig. 9a). The AE amplitude is also generally low (less than 50 dB), mostly near the detection threshold (45 dB) (Fig. 9b). During this stage, the energy is input by the 316 testing machine through compressing and working on the rock, and most of the input energy is 317 318 transformed into elastic strain energy and stored. Only a small amount of the energy is dissipated 319 by the compaction of original micro-cracks and the interaction of particles inside the rock. The 320 total elastic strain energy and total dissipated strain energy are both very low (Fig. 9c, d), but the strain energy ratio curves change very sharply. The ratio of total elastic strain energy decreases 321

322 rapidly to a minimum, while the ratio of the total dissipated strain energy increases rapidly to a323 maximum (Fig. 9e).

During the elastic deformation stage (AB), very few micro-cracks events occur in the rock, AE activity is in a quiet period, the AE count and the cumulative AE count remain very low (Fig. 9a) The AE amplitude is relatively low, generally lower than 50 dB (Fig. 9b). During this stage, all the work done by the testing machine is transformed into elastic strain energy in the rock, which is the main energy storage stage of the rock. Therefore, the total elastic strain energy continuously increases, while the total dissipated strain energy remains unchanged (Fig. 9c, d). The ratio of total elastic strain energy continuously increases, while the ratio of total dissipated strain energy

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continuously decreases (Fig. 9e).

332 After loading to the stable propagation of micro-cracks stage (BC), the micro-cracks initiate and propagate steadily. Consequently, AE activity gradually increases, and the AE count and 333 334 cumulative AE count also increase, but the values are not high (Fig. 9a). The AE amplitude 335 continuously increases but is still lower than 70 dB (Fig. 9b). In this stage, because of the stable 336 propagation of micro-cracks in the rock, the energy input by the testing machine is partly 337 transformed into elastic strain energy and partly transformed into dissipated strain energy, but the 338 elastic strain energy in the rock is still dominant (Fig. 9c, d). The total elastic strain energy ratio continues to increase, but the rate of increase decreases, and a maximum total elastic strain energy 339 340 ratio is reached at the end of this stage. The variation in the total dissipated strain energy ratio is 341 opposite to that of the total elastic strain energy ratio (Fig. 9e).

342 During the stage of accelerated extension of cracks (CD), the micro-cracks propagate rapidly 343 and consequently AE event activity increases significantly. The AE count increases rapidly and it 344 has a sharply increases at the peak stress point. The cumulative AE count shows dramatic 345 increases and its curve increases rapidly (Fig. 9a). The AE amplitude increases rapidly, and its 346 maximum value is approximately 100 dB (Fig. 9b). During this stage, the total elastic strain 347 energy decreases, and the total dissipated strain energy increases due to the accelerated 348 propagation of the micro-cracks in the rock (Fig. 9c, d). Additionally, the total elastic strain energy 349 ratio begins to decrease, and the total dissipated strain energy ratio begins to increase (Fig. 9e).

Finally, in the post-peak strength loss and residual shearing stage (DE), a large number of micro-cracks inside the rock rapidly aggregate and form macroscopic failure surfaces. Meanwhile, 352 the AE event activity is extremely frequent and active. The AE count is relatively high and reaches its maximum value at the maximum post-peak stress drop point. The cumulative AE count 353 354 increases rapidly and a sudden jump occurs at the maximum post-peak stress drop point (Fig. 9a). 355 The AE amplitude generally remains above 70 dB, and the maximum AE amplitude is approximately 100 dB (Fig. 9b). During this stage, the total elastic strain energy decreases rapidly 356 357 and the total dissipated strain energy increases rapidly due to the stored elastic strain energy is 358 released quickly (Fig. 9c, d). The total elastic strain energy ratio decreases rapidly, while the total 359 dissipated strain energy ratio increases rapidly (Fig. 9e).

It is worth mentioning that the damage stress threshold (σ_{cd}) of the rock can be determined by 360 a maximum value of the elastic strain energy ratio or a minimum value of the dissipated strain 361 362 energy ratio (Fig. 9e). The damage stress threshold (σ_{cd}) defined in Fig. 9e is also the starting point of the bifurcation between the total strain energy curve and the total elastic strain energy curve of 363 the rock (Fig. 9c). Clearly, this point is point C, which represents the start of the accelerated 364 extension of cracks stage (CD). Besides, the damage stress threshold point (σ_{cd}) is also 365 366 corresponding to the maximum AE count within the blue circle (Fig. 9a). Starting at the 367 accelerated extension of cracks stage (point C), the crack propagation rate increases rapidly, and the AE count responds by suddenly increasing. This may be that a sudden increase in the rate of 368 crack propagation causes high-frequency vibration signals to be released from the micro-crack tips, 369 370 leading to an increase in the number of oscillations of the monitored AE voltage signal, exceeding 371 the threshold voltage and creating a local peak in the AE count.

4.2. Fracturing process analysis combining the AE hypocenter location and strain energy

The AE hypocenter location results of the Beishan granite under TTC (σ_2 =75 MPa, σ_3 =20 373 374 MPa) are shown by the stress-time curve (Fig. 10a) and stress-strain curve (Fig. 10b). The 375 reference coordinate system used to analyse the fracturing process in Fig. 11 is shown with the 376 specimen model in Fig. 10a. The total duration time of the TTC and AE test is 0.93 h (Fig. 10 and Fig. 11). Corresponding to Fig. 11a-h, the increments of the AE count $S_{\rm e}$, AE event $S_{\rm e}$ and the total 377 378 elastic strain energy U_e per unit time ($\Delta S_c / \Delta t$, $\Delta S_e / \Delta t$ and $\Delta U_e / \Delta t$) and the increments of the total elastic strain energy (ΔU_e) shown in Fig. 11i, j can be solved according to the following Eqs. (4), 379 380 (5), (6) and (7):

$$\frac{\Delta S_c}{\Delta t} = \frac{S_c^i - S_c^{i-1}}{t^i - t^{i-1}} \tag{4}$$

$$\frac{\Delta S_e}{\Delta t} = \frac{S_e^i - S_e^{i-1}}{t^i - t^{i-1}} \tag{5}$$

$$\frac{\Delta U_e}{\Delta t} = \frac{U_e^i - U_e^{i-1}}{t^i - t^{i-1}} \tag{6}$$

$$\Delta U_e = U_e^i - U_e^{i-1} \tag{7}$$

385 Where i = 1, 2, ..., 8; $t^0 = 0$ s, $t^1 = 365$ s, ..., $t^8 = 3348$ s; $S_c^0 = 0, S_c^1 = 734, ..., S_c^8 = 472000$; 386 $S_e^0 = 0, S_e^1 = 25, ..., S_c^8 = 9612$; $U_e^0 = 0$ kJ/m³, $U_e^1 = 304$ kJ/m³, ..., $U_e^8 = 233$ kJ/m³.

As shown in Fig. 11a-h, during the initial loading stage, the AE event representing the 387 388 micro-cracking are randomly scattered over the specimen. With increasing loading, the AE event 389 gradually increase and concentrate near the fracture surfaces inside the rock, finally forming a 390 macroscopic fracture zone. It can be found that when the stress of the rock increases from 43 % to 391 92 % of the peak stress, the increase in stress is as high as 49 %, and the number of AE event increases by 474 (Fig. 11a, c); however, when the stress level of the rock increases from 92 % to 392 393 100 %, the increase in stress is only 8 %, and the number of AE event increases by 1141 (Fig. 11c, 394 d). Meanwhile, the $\Delta S_c/\Delta t$ and $\Delta S_c/\Delta t$ are considerably low before 92 % of the peak stress. While 395 their magnitudes rapidly increase and their curve slopes increase significantly when the stress is increased from 92 % to 100 % of the peak stress (Fig. 11i). As shown in Fig. 11j, although the 396 $\Delta U_e/\Delta t$ shows reduction after 71 % of the peak stress, the ΔU_e increases until 92 % of the peak 397 398 stress. After 92 % of the peak stress, The ΔU_e and $\Delta U_e \Delta t$ decrease appreciably due to the 399 significant increase of the cracking and energy dissipation inside the rock.

400 Through the above analysis, we found that the AE activity of the micro-cracking of the 401 Beishan granite is not very active before 92 % of the peak stress. When the stress is as high as 92 % 402 of the peak stress, a lot of micro-cracks form and develop in the rock specimen, thus the AE 403 activity becomes very active. Clearly, for hard brittle rocks such as Beishan granite, when the 404 stress does not reach a very high level, few micro-cracks form in the rock and their AE activity is low. Only when the stress reaches a high level or approaches the peak stress, the micro-cracks 405 406 inside the rock suddenly increase, leading to instability and failure of the rock in a short time, 407 which reveals the reason why the rockburst of deep hard rock mass is in a sudden failure.

408 To analyse the post-peak fracturing processes of the Beishan granite, it can be seen that when

the stress drop of the rock is only 12 % (from 100 % of the peak stress to 88 %) and 10 % (from 409 410 88 % of the peak stress to 78 %) of the peak stress, the increments of the AE event are as high as 411 4762 and 3194 (Fig. 11d, e, f); however, when the stress drop of rock is as high as 41 % (from 78 % 412 of the peak stress to 37 %), the increment of the AE event is only 16 (Fig. 11f, h). As shown in Fig. 413 11i, the $\Delta S_c/\Delta t$ and $\Delta S_c/\Delta t$ increase rapidly when the rock stress decreases from 100 % to 88 % of 414 the peak stress. While the $\Delta S_0/\Delta t$ and $\Delta S_0/\Delta t$ decrease rapidly when the rock stress decreases from 88 % to 78 % of the peak stress and from 78 % to 37 % of the peak stress. Moreover, it also can be 415 416 found that the former change (88 % to 78 %) is greater than the latter change (78 % to 37 %) in terms of the reduction in magnitude and curve slope. In term of the strain enegy, during the first 417 post-peak stress drop process (from 100 % to 88 % of the peak stress), the ΔU_e and $\Delta U_e/\Delta t$ 418 419 decrease continuously and their curve slopes also decrease. While during the second post-peak 420 stress drop process (from 88 % to 78 % of the peak stress), the stress-strain curve has a process of 421 slightly rising and then falling (Fig. 10b), thus both the elastic strain energy storage and release 422 occur inside the rock during this process. Eventually, the $\Delta U_e/\Delta t$ increases slightly while the ΔU_e 423 remains basically unchanged. When the stress drops from 78 % to 37 % of the peak stress (test 424 termination point), due to the formation of the rock macroscopic fracture, the changes in the ΔU_e 425 and $\Delta U_e/\Delta t$ are not large and their curve slopes are relatively gentle.

426 Through the above analyses, it can be found that the formation of macroscopic fractures and 427 the rapid release of elastic strain energy stored in the rock mostly occur during the first stress drop process. Meanwhile, the maximum values of $\Delta S_e/\Delta t$, ΔU_e and $\Delta U_e/\Delta t$ all occur during this process. 428 429 Therefore, for hard brittle rocks such as Beishan granite, once macroscopic fracturing occurs, the 430 strain energy in the rock will rapidly release and produce numerous AE event. Meanwhile, with 431 the further developing of the rock macroscopic fracturing, the post-peak fracturing of hard rock 432 can be more severe and difficult to control and ultimately leads to the strength loss and instability 433 failure of the rock. The findings are helpful to reveal and understand why the process of rockburst 434 in the hard rock is often very intense and uncontrollable.

435 **5. Conclusion**

In this paper, the TTC and AE tests of the Beishan granite are performed. The stress-strain
relationship, AE and strain energy characteristics of the Beishan granite under TTC conditions are

studied. The fracture process of the Beishan granite is illustrated with deep insight by combining 438 439 the AE and strain energy results. Within the scope of this study, we found that when σ_2 is high, the 440 rock tends to exhibit Class II failure, and its brittle failure is obvious; additionally, the overall AE activity is more intense, increasing the AE count and cumulative AE count. The damage evolution 441 and accumulation in the rock are identified into three types according to the AE hypocenter 442 443 location results. The strain energy variations of the Beishan granite at pre-peak are basically similar while they are quite different at post-peak especially when σ_2 is high. By integrating AE 444 445 and strain energy results, five fracturing evolution stages of the Beishan granite are discussed. Damage stress threshold (σ_{cd}) can be determined by a maximum value of the elastic strain energy 446 ratio or a minimum value of the dissipated strain energy ratio. For the hard brittle rocks such as 447 448 Beishan granite, only when the stress approaches the peak stres, the micro-cracks inside the rock will increase suddenly and lead to a rapid instability and failure. Once macroscopic fracturing 449 occurs during the post-peak stage, the rapid energy release will lead to further violent fracturing. 450

451 Acknowledgements

This study was supported by the 111 Project (No. B17009), the CAS Key Research Program
of Frontier Sciences (No. QYZDJ-SSW-DQC016), and the National Natural Science Foundation,
China (No. 51579043, 51709043).

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Fig. 1. Optical micrograph of Beishan granite showing the textures of major rock and ore types, with major crystals of quartz (Qtz), K-feldspar (Kfs), plagioclase (Pl) and biotite (Bt). (a) Crossed polars. (b) Plane polarized light.



Fig. 2. Illustration of the tested specimen and AE sensors distribution during the true triaxial compression test.



Fig. 3. Stress path applied during the true triaxial experiments.



Fig. 4. Stress–strain relationships of Beishan granite at different intermediate principle stress (σ_2) levels and constant minimum principal stress (σ_3) (σ_3 =5 MPa) during true triaxial compression. (a) σ_2 =20 MPa, σ_3 =5 MPa. (b) σ_2 =75 MPa, σ_3 =5 MPa. (c) σ_2 =100 MPa, σ_3 =5 MPa. (d) σ_2 =150 MPa, σ_3 =5 MPa.



Fig. 5. Stress–strain relationships of Beishan granite at different minimum principal stress (σ_3) levels and constant intermediate principal stress (σ_2) (σ_2 =75 MPa) during true triaxial compression. (a) σ_2 =75 MPa, σ_3 =5 MPa. (b) σ_2 =75 MPa, σ_3 =10 MPa. (c) σ_2 =75 MPa, σ_3 =20 MPa. (d) σ_2 =75 MPa, σ_3 =30 MPa.



Fig. 6. Strain energy characteristics of Beishan granite during true triaxial compression test. (a) and (b) $\sigma_2=75$ MPa, $\sigma_3=5$ MPa. (c) and (d) $\sigma_2=150$ MPa, $\sigma_3=5$ MPa. (e) and (f) $\sigma_2=75$ MPa, $\sigma_3=20$ MPa.



Fig. 7. AE characteristics and failure behaviors of Beishan granite under true triaxial compression. (a) and (b) $\sigma_2=75$ MPa, $\sigma_3=5$ MPa. (c) and (d) $\sigma_2=150$ MPa, $\sigma_3=5$ MPa. (e) and (f) $\sigma_2=75$ MPa, $\sigma_3=20$ MPa.



Fig. 8. Fracturing evolution process of Beishan granite based on AE hypocenter location under true triaxial compression ($\sigma_2=75$ MPa, $\sigma_3=20$ MPa) at different elapsed times and stress levels. (a) 365s, $\sigma_1/\sigma_{1peak}=43$ %. (b) 595s, $\sigma_1/\sigma_{1peak}=71$ %. (c) 1250s, $\sigma_1/\sigma_{1peak}=100$ % (the peak stress point). (d) 1625s, $\sigma_1/\sigma_{1peak}=88$ % (the first stress-drop point at post-peak). (e) 3348s, $\sigma_1/\sigma_{1peak}=37$ % (test termination point). (h) Schematic spatial model of fracture morphology of tested rock in reference coordinate system. Corresponding to the different color of ellipse regions in (a-e), spatial failure planes with corresponding color in (h) show the time difference and formation process difference of cracking behavior of tested rock. (f, g) Comparison of actual crack distribution (f) and AE hypocenter location (g) on plane ABCD of the final failure specimen. The morphology and distribution of cracks are depicted on AE hypocenter location map (g) according to the actual fracture characteristics on plane ABCD. (i, g) The case of (i, g) on plane A'B'C'D' is the same as (f, g), (i) is the AE hypocenter location and (j) is the actual crack distribution.



Fig. 9. Complete behavior process of Beishan granite under true triaxial compression associate with AE and strain energy characteristic. The maximum principal stress (σ_1) time history curves of one representative test result with true triaxial stress state of σ_2 =75 MPa, σ_3 =20 MPa are shown in each subgraph. Additional to time history curves are shown as: (a) AE count (red bars) and cumulative AE count (blue line), (b) amplitude, (c) total strain energies and strain energies at σ_1 direction, (d) strain energies at σ_2 and σ_3 directions, and (e) strain energy ratios.



Fig. 10. AE hypocenter location results at selected states during complete behavior process of Beishan granite under true triaxial compression (σ_2 =75 MPa, σ_3 =20 MPa) corresponds to different (a) elapsed times and (b) stress levels. The time points corresponding to the points a-h are 365 s, 595 s, 916 s, 1250 s, 1625 s, 2250 s, 2880 s and 3348 s, respectively. The stress levels (σ_1/σ_{1peak}) corresponding to the points a-h are 43 %, 71 %, 92 %, 100 % of the peak stress at pre-peak and 88 %, 78 %, 55 %, 37 % of the peak stress at post-peak, respectively.



Fig. 11. AE hypocenter location and energy evolution characteristic at different time point of Beishan granite under true triaxial compression (σ_2 =75 MPa, σ_3 =20 MPa) (total duration 3348 s = 0.93 hour). The reference coordinate system used to analysis in this figure as shown in the Fig. 10a. (a-h) Orthographic views of AE hypocenter location at different elapsed times associate with AE count S_c and AE event S_e . (i) Increments of AE count S_c and AE event S_e per unit time ($\Delta S_c / \Delta t$ and $\Delta S_c / \Delta t$) and (j) increments of total elastic strain energy (ΔU_e) and total elastic strain energy per unit time ($\Delta U_c / \Delta t$) change with different time sections and different stress levels ($\sigma_1 / \sigma_{1peak}$).