

# The Effective Volumes of Waters of Crystallization & the Thermodynamics of Cementitious Materials

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**3 Supplementary Tables**

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**Table S1:** Thermodynamic data for AFm and AFt phases, from *Cemdata18*.<sup>1</sup>

<b>AFm-phases<sup>a</sup></b>	<b><math>n(\text{H}_2\text{O})</math></b>	<b><math>V_m</math> / <math>\text{cm}^3 \text{mol}^{-1}</math></b>	<b><math>S</math> / <math>\text{J K}^{-1} \text{mol}^{-1}</math></b>	<b><math>C_p</math> / <math>\text{J K}^{-1} \text{mol}^{-1}</math></b>	<b><math>C_p/S</math></b>
$C_4AH_{19}$	19	369	1120	1382.5	1.23
$C_4AH_{13}$	13	274	831.5	1141.5	1.37
$C_4AH_{11}$	11	257	772.7	1061.4	1.37
$C_2AH_{7.5}$	7.5	180	450	540.1	1.20
$CAH_{10}$	10	193	610	668.2	1.10
$C_4AC_{0.5}H_{12}$	12	285	713	920.0	1.29
$C_4AC_{0.5}H_{10.5}$	10.5	261	668.3	845.6	1.27
$C_4AC_{0.5}H_9$	9	249	622.5	785.6	1.26
$C_4ACH_{11}$	11	262	657	881.6	1.34
$C_4ACH_9$	9	234	640.6	801.2	1.25
$C_4ASH_{16}$	16	351	975	1114.8	1.14
$C_4ASH_{14}$	14	332	960.9	1028.5	1.07
$C_4ASH_{12}$	12	310	791.6	948.4	1.20
$C_4ASH_{10.5}$	10.5	282	721	888.2	1.23
$C_4ASH_9$	9	275	703.6	828.2	1.18
$C_2ASH_8$	8	216	546	615.0	1.13
$C_2ASH_7$	7	215	487.6	562.6	1.15
$C_2ASH_{5.5}$	5.5	213	454.8	502.4	1.10
$C_4AS_{0.5}ClH_{12}$	12	289	820	940.7	1.15
$C_4ACl_2H_{10}$	10	272	731	851.9	1.17
$C_4A(\text{NO}_3)_2H_{10}$	10	296	821	934.6	1.14
$C_4A(\text{NO}_2)_2H_{10}$	10	275	799	900.9	1.13
<b>Ferrates</b>					
$C_4FH_{13}$	13	286	630	1118.5	1.78
$C_4FC_{0.5}H_{10}$	10	273	1270	841.2	0.66
$C_4FCH_{12}$	12	292	1230	892.5	0.73
$C_4FsH_{12}$	12	321	1430	967.6	0.68
$C_4FCl_2H_{10}$	10	278	1286	854.4	0.66

<b>Aft-phases</b>	<b>n(H<sub>2</sub>O)</b>	<b>V<sub>m</sub> / cm<sup>3</sup> mol<sup>-1</sup></b>	<b>S / J K<sup>-1</sup> mol<sup>-1</sup></b>	<b>C<sub>p</sub> / J K<sup>-1</sup> mol<sup>-1</sup></b>	<b>C<sub>p</sub>/S</b>
<i>C<sub>6</sub>AS<sub>3</sub>H<sub>32</sub></i>	32	707	1900	2174.2	1.14
<i>C<sub>6</sub>AS<sub>3</sub>H<sub>30</sub></i>	30	708	1792.4	2094.8	1.17
<i>C<sub>6</sub>AS<sub>3</sub>H<sub>13</sub></i>	13	411	1960.4	1412.9	0.72
<i>C<sub>6</sub>AS<sub>3</sub>H<sub>9</sub></i>	9	361	646.6	1252.7	1.94
<i>C<sub>6</sub>AC<sub>3</sub>H<sub>30</sub></i>	30	650	1858	2121.1	1.14
<i>C<sub>6</sub>F<sub>2</sub>S<sub>3</sub>H<sub>32</sub></i>	32	717	1937	2199.6	1.14
<i>C<sub>3</sub>ScsH<sub>15</sub></i>	15	330	897.1	1071.2	1.19
<i>C<sub>3</sub>AH<sub>6</sub></i>	6	150	422	445.4	1.06
<i>C<sub>3</sub>AS<sub>0.41</sub>H<sub>5.18</sub></i>	5.18	146	399	429.6	1.08
<i>C<sub>3</sub>AS<sub>0.84</sub>H<sub>4.32</sub></i>	4.32	142	375	412.9	1.10
<b>Ferrates</b>					
<i>C<sub>3</sub>FH<sub>6</sub></i>	6	155	870	645.5	0.74
<i>C<sub>3</sub>FS<sub>0.84</sub>H<sub>4.32</sub></i>	4.32	149	840	434.4	0.52
<i>C<sub>3</sub>A<sub>0.5</sub>F<sub>0.5</sub>S<sub>0.84</sub>H<sub>4.32</sub></i>	4.32	146	619	416.3	0.67
<i>C<sub>3</sub>FS<sub>1.34</sub>H<sub>3.32</sub></i>	3.32	145	820	414.8	0.51

<sup>a</sup> The chemical formulae, in cement shorthand notation, are: A=Al<sub>2</sub>O<sub>3</sub>; C=CaO; F=Fe<sub>2</sub>O<sub>3</sub>; H=H<sub>2</sub>O;

S=SiO<sub>2</sub>; c=CO<sub>2</sub>; s=SO<sub>3</sub>.

**Table S2:** Thermodynamics of hydrated mineral calcium silicates ex Table 10 of Blanc.<sup>2-3</sup> The final columns list the number of waters of crystallization per formula unit,  $n(\text{H}_2\text{O})$ , molar volume,  $V_m/\text{cm}^3 \text{mol}^{-1}$ , molar entropy,  $S/\text{J K}^{-1} \text{mol}^{-1}$ , heat capacity,  $C_p/\text{J K}^{-1} \text{mol}^{-1}$ , and ratio  $C_p/S$ .

Mineral	Chemical Formula	$n(\text{H}_2\text{O})$	$V_m$ $/\text{cm}^3 \text{mol}^{-1}$	$S$ $/\text{J K}^{-1} \text{mol}^{-1}$	$C_p$ $/\text{J K}^{-1} \text{mol}^{-1}$	$C_p/S$
<b>Crystalline C-S-H</b>						
Gyrolite	$\text{Ca}_2\text{Si}_3\text{O}_7(\text{OH})_2 \cdot 2\text{H}_2\text{O}$	2	137.34	309.32	325.94	1.05
Xonotlite	$\text{Ca}_6\text{Si}_6\text{O}_{17}(\text{OH})_2$	0	256.9	573.74	628.64	1.10
Tobermorite-14	$\text{Ca}_5\text{Si}_6(\text{OH})\text{O}_{16.5} \cdot 10\text{H}_2\text{O}$	10	351.3	874.57	973.53	1.11
Tobermorite-11	$\text{Ca}_5\text{Si}_6(\text{OH})\text{O}_{16.5} \cdot 5\text{H}_2\text{O}$	5.5	286.19	692.55	764.91	1.10
Foshagite	$\text{Ca}_4\text{Si}_3\text{O}_9(\text{OH})_2 \cdot 0.5\text{H}_2\text{O}$	0.5	160.66	295.07	309.38	1.05
Jennite	$\text{Ca}_9\text{Si}_6\text{O}_{16}(\text{OH})_{10} \cdot 6\text{H}_2\text{O}$	6	456.4	839.25	933.21	1.11
Afwillite	$\text{Ca}_3\text{Si}_2\text{O}_6(\text{OH})_2 \cdot 2\text{H}_2\text{O}$	2	129.53	289.7	303.55	1.05
Hillebrandite	$\text{Ca}_2\text{SiO}_3(\text{OH})_2 \cdot 0.17\text{H}_2\text{O}$	0.17	72.58	179.71	177.46	0.99
<b>Crystalline C-S-H Estimated</b>						
Truscottite	$\text{Ca}_7\text{Si}_{12}\text{O}_{29}(\text{OH})_4 \cdot \text{H}_2\text{O}$	1	478.73	927.68	1034.1	1.11
Okenite	$\text{CaSi}_2\text{O}_4(\text{OH})_2 \cdot \text{H}_2\text{O}$	1	94.77	208.52	210.07	1.01
C2SH, $\alpha$	$\text{Ca}_2(\text{HSiO}_4)(\text{OH})$	0	71.12	122.38	111.88	0.91
Jaffeite	$\text{Ca}_6(\text{Si}_2\text{O}_7)(\text{OH})_6$	0	174.38	326.19	344.9	1.06

**Table S3:** Thermodynamics of three hydrated sulfate minerals.<sup>2</sup> The final columns list the number of waters of crystallization per formula unit,  $n(\text{H}_2\text{O})$ , molar volume,  $V_m/\text{cm}^3 \text{mol}^{-1}$ , molar entropy,  $S/\text{J K}^{-1} \text{mol}^{-1}$ , heat capacity,  $C_p/\text{J K}^{-1} \text{mol}^{-1}$ , and ratio  $C_p/S$ .

Mineral	Chemical Formula	$n(\text{H}_2\text{O})$	$V_m$ $/\text{cm}^3 \text{mol}^{-1}$	$S$ $/\text{J K}^{-1} \text{mol}^{-1}$	$C_p$ $/\text{J K}^{-1} \text{mol}^{-1}$	$C_p/S$
Ettringite	$\text{Ca}_6\text{Al}_2(\text{SO}_4)_3(\text{OH})_{12} \cdot 26\text{H}_2\text{O}$	26	705.1	1747.24	1794.55	1.03
		26		1900	2174.24	1.14
Monosulfoaluminate	$\text{Ca}_4\text{Al}_2(\text{SO}_4)(\text{OH})_{12} \cdot 6\text{H}_2\text{O}$	6	308.2	747.26	783.68	1.05
		6		821	942.24	1.15
Gypsum	$\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$	2	74.5	193.8	186.2	0.96

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