

# Natural Gas Density Measurements and the Impact of Accuracy on Process Design

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## Abstract

The liquefaction of natural gas is an energy intensive processes, requiring 5% of the lower heating value. Key to estimating and optimizing these energy requirements are process simulations which rely upon calculated thermophysical properties of the natural gas. In particular, the prediction of thermophysical properties of natural gas mixtures at pressure-temperature conditions close to the mixture's critical point or cricondenbar is challenging but important as often natural gas processes operate close to these conditions. In this work, we present a comprehensive study of two natural gas related systems: (CH<sub>4</sub> + C<sub>3</sub>H<sub>8</sub> + CO<sub>2</sub>) and (CH<sub>4</sub> + C<sub>3</sub>H<sub>8</sub> + C<sub>7</sub>H<sub>16</sub>) with *n*-heptane fractions up to 15 mol %. High accuracy measurements of densities, at temperatures from 200 K to 423 K and pressures up to 35 MPa are presented. The extensive experimental data collected for these mixtures were compared with the GERG-2008 equation of state, as implemented in the NIST software REFPROP. The relative

28 deviations of the measured densities from those calculated using the GERG-2008 model  
29 range between (-2 to 4) % for all mixtures, presenting a systematic dependent on mixture  
30 density and *n*-heptane content. Finally, a case study is presented that probes the impact of  
31 the accuracy of density on the pinch point in a simulated LNG heat exchanger. An uncertainty  
32 in the density of 1 % is shown to cause significant 30 % reduction in the minimum approach  
33 temperature difference, suggesting that accurate thermophysical property calculations are key  
34 to reducing over-design of processing plant.

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36 **Keywords:** Methane + propane + *n*-heptane mixtures, Carbon dioxide, Density, Natural gas,  
37 Modelling

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## 52 1. INTRODUCTION

53 Natural gas consists mainly of light hydrocarbons such as methane, ethane, propane as well  
54 as contaminants such as carbon dioxide, hydrogen sulfide and nitrogen [1]. It produces (50 to  
55 60) % less CO<sub>2</sub> when burnt than coal and (15 to 20) % less greenhouse gases than gasoline  
56 when used in vehicles [2], making it central to the transition towards a low carbon-emissions  
57 society [3-9]. Prior to being fed into pipeline systems or liquefaction facilities [10], raw natural  
58 gas needs to be processed for it to meet product specifications. This involves separation of a  
59 series of undesirable components, like carbon dioxide, water, and hydrogen sulfide, and/or  
60 the recovery of more valuable components, for example, ethane, propane, butane, heavier  
61 hydrocarbons and helium [11-16]. The design of each stage in that transformation process  
62 uses predictions of the mixture's thermophysical properties as a function of temperature,  
63 pressure and composition [11, 12].

64  
65 Many different models are available for predicting a mixture's thermophysical properties, each  
66 with varying complexity and accuracy. All, however, are anchored to measured data with the  
67 model's reliability generally decreasing as predictions go beyond the range of these anchoring  
68 data. The data required to confidently design gas processing equipment at operating  
69 conditions near the gas mixture's critical point are deficient, and ultimately lead to the over-  
70 design of plants, higher operating costs and less energy efficient processing [17]. To achieve  
71 better designs that work more effectively over a wider range of conditions, the gas industry  
72 needs new fundamental property data, both to resolve discrepancies in our current predictive  
73 capabilities and to extend them to the higher-pressure conditions characteristic of many new  
74 gas fields. This requires new and accurate thermophysical property data for natural gas  
75 mixtures be measured at conditions often considered inaccessible.

76 Thermodynamic models used in natural gas industry range from empirical and semi-empirical  
77 correlations, such as cubic equations of state (for example, PR76 [18] developed by Peng and  
78 Robinson), activity coefficients models and molecular-based models such as Statistical

79 Associating Fluid Theory (SAFT) [19]. Most recent efforts to improve LNG process simulations  
80 have focussed on the use of complex equations of state [11-15] capable of more accurately  
81 describing the VLE, density and other properties of multi-component fluid mixtures. These  
82 include the GERG-2008 equation of state (EOS) by Kunz and Wagner [13] which is endorsed  
83 by the International Organisation for Standardization (ISO 20765-2 and 20765-3) for natural  
84 gas mixtures. All of the above models are tuned to existing experimental data from pure fluid  
85 and binary mixtures [20]. Thus, in terms of ternary or multi-component gas mixtures, their  
86 accuracy needs to be further tested with new high-quality experimental data [12]. Our recent  
87 studies of thermodynamic properties such as phase equilibrium [14, 21-33], heat capacity [34,  
88 35] and density [25, 36-38] clearly identified deficiencies in EOS commonly used by industry,  
89 and in several of the archival literature data to which those models have been tuned [14].

90 Therefore, in this work, the density of gas and liquid phases at high pressures and over a  
91 wide-range of temperatures, including near the mixture's critical point (where gas and liquid  
92 become indistinguishable and the existing predictive fluid property models used by engineers  
93 breakdown) were investigated. Here we present a comprehensive study of two prototype  
94 systems of natural gas related gases: ( $\text{CH}_4 + \text{C}_3\text{H}_8 + \text{CO}_2$ ) and ( $\text{CH}_4 + \text{C}_3\text{H}_8 + \text{C}_7\text{H}_{16}$ );  
95 comprising accurate measurements of the saturated-phase densities, and compressed-fluid  
96 (single-phase) densities at temperature from 200 K to 423 K and pressures up to 35 MPa over  
97 different ranges of compositions. These mixtures were chosen for investigation due to their  
98 relevance for natural gas gathering, treating and processing equipment design and  
99 optimization.

100 To our knowledge, no density data exists for the ternary mixtures considered in this work.  
101 Some researchers have measured the density of natural gas related binary mixtures. Karimi  
102 et al. [39] have measured the density of methane and propane mixtures at temperatures  
103 between (256 and 422) K and pressure from (24 to 35) MPa using a magnetic suspension  
104 densimeter. Yang et al. [40] have reported the density of methane and carbon dioxide gas  
105 mixtures at temperatures between (300.15 to 313.15) K and pressures between (8 and 10)

106 MPa measured using a single-sinker densimeter. Richter et al. [41] developed a special  
 107 densimeter and studied a synthetic five-component LNG mixture at temperatures between  
 108 (105 to 135) K and pressures up to 8.1 MPa. Other researchers' studies can be found in Ref.  
 109 [39-44]. We recently [36] extended the lowest operational temperature of a commercial  
 110 vibrating tube densimeter (VTD) down to 203 K, calibrated using a robust physically based  
 111 model [45]. The extended calibration was then employed for single-phase density  
 112 measurements of a 0.95 methane + 0.05 propane mixture at a temperature of 203 K and  
 113 pressure up to 35 MPa.

114 The experimental ranges of composition, temperature and pressure gathered in this work are  
 115 summarized in **Table 1**. Mixtures 1, 2, and 3 correspond to (0.85 C1 + 0.10 C3 + 0.05 C7),  
 116 (0.81 C1 + 0.09 C3 + 0.10 C7), and (0.71 C1 + 0.14 C3 + 0.15 C7), respectively. Mixture 4  
 117 corresponds to (0.640 C1 + 0.098 C3 + 0.261 CO<sub>2</sub>).

118 **Table 1.** Summary of investigated ternary mixtures including composition,  $x$ , pressure range  
 119  $p$  and temperature range  $T$ .

Mixture	$x_{C1}$	$x_{C3}$	$x_{C7}$	$x_{CO2}$	$T_{range}/K$	$p_{range}/MPa$
<b>Single and bubble points density measurements</b>						
Mixture 1	0.854	0.095	0.051	0	204 - 420	6 - 35
Mixture 2	0.809	0.090	0.101	0	203 - 420	7 - 35
Mixture 3	0.714	0.136	0.150	0	207 - 420	10 - 35
Mixture 4	0.640	0.098	0	0.262	273 - 421	10 - 35

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121 These data were compared with the predictions of the GERG-2008 EOS [13] as implemented  
 122 in the software REFPROP 10.0 [46]. The GERG-2008 EOS is a Helmholtz free energy model  
 123 as a function of temperature, pressure and composition. In describing binary mixture  
 124 thermodynamic properties, binary interaction parameters within reducing functions are  
 125 adjusted to force agreement with experimental data. Equation (1) and (2) represent the

126 composition-dependent reducing functions for binary mixture density ( $\rho_r$ ) and temperature ( $T_r$ ),  
 127 where  $\beta_{v,ij}$ ,  $\gamma_{v,ij}$ ,  $\beta_{T,ij}$  and  $\gamma_{T,ij}$  are adjusted binary parameters;  $\rho_{c,i}$  and  $T_{c,i}$  are critical  
 128 density and critical temperature of pure component  $i$ .

$$\frac{1}{\rho_r(\bar{x})} = \sum_{i=1}^N x_i^2 \frac{1}{\rho_{c,i}} + \sum_{i=1}^{N-1} \sum_{j=i+1}^N 2x_i x_j \beta_{v,ij} \gamma_{v,ij} \cdot \frac{x_i + x_j}{\beta_{v,ij}^2 x_i + x_j} \cdot \frac{1}{8} \left( \frac{1}{\rho_{c,i}^{1/3}} + \frac{1}{\rho_{c,j}^{1/3}} \right)^3 \quad (1)$$

$$T_r(\bar{x}) = \sum_{i=1}^N x_i^2 T_{c,i} + \sum_{i=1}^{N-1} \sum_{j=i+1}^N 2x_i x_j \beta_{T,ij} \gamma_{T,ij} \cdot \frac{x_i + x_j}{\beta_{T,ij}^2 x_i + x_j} (T_{c,i} \cdot T_{c,j})^{0.5} \quad (2)$$

129 Additionally, if a sufficient number of data were available at the time of the model's  
 130 development, a departure function may be added to describe the specific binary to improve  
 131 the accuracy of the model when describing that binary. The parameters and functions used  
 132 for the description of binary mixtures relevant to this work are summarized in **Table 2**.

133 **Table 2.** Overview of GERG mixing functions for five binary mixtures

Binaries	Reducing functions				Departure function
	$\beta_{v,ij}$	$\gamma_{v,ij}$	$\beta_{T,ij}$	$\gamma_{T,ij}$	
C1 + C3	1.0048	1.0385	0.98968	1.0987	Yes
C1 + C7	0.96205	1.1567	0.97743	1.3799	None
C3 + C7	1.0	1.0796	1.0	1.05	None
C1 + CO <sub>2</sub>	0.99952	1.0028	1.0226	0.97567	Yes
C3 + CO <sub>2</sub>	0.9969	1.0476	1.0336	0.90877	None

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## 135 2. Materials and Methods

### 136 2.1. Materials

137 The suppliers and supplier-analysed purities of all components used in this work are listed in  
 138 **Table 3**. No further purification was attempted. The supplied (C<sub>1</sub> + C<sub>3</sub>) gas mixtures for this

139 project had a certified standard relative uncertainty  $u_r(x)$  of 1%. *n*-Heptane was degassed  
140 under vacuum before use.

141 **Table 3.** Source and purities of chemicals used in this work

Compound	Supplier	Mole fraction	CAS Number
Methane	Coregas	0.99999	74-82-8
Propane	Coregas	0.99995	74-98-6
Carbon Dioxide	Coregas	0.99995	124-38-9
<i>n</i> -Heptane	Sigma Aldrich	0.99	142-82-5
C <sub>1</sub> + C <sub>3</sub> mixtures	CAC Gas	0.8999 C <sub>1</sub> + 0.1001 C <sub>3</sub> 0.8398 C <sub>1</sub> + 0.1602 C <sub>3</sub>	N/A

142

## 143 2.2. Density-Vibrating tube densimeter

144 A vibrating tube densimeter [36] (Anton Paar, DMA HPM) was used to measure the density of  
145 the hydrocarbon ternary mixtures (C<sub>1</sub> + C<sub>3</sub> + C<sub>7</sub>). Details regarding mixture preparation and  
146 compositional analysis, experimental setup, procedure, calibration and uncertainty are given  
147 in the Supplementary Information (SI). Initially a magnetic suspension densimeter was  
148 employed for this ternary system. However, due to the large volume of the magnetic  
149 suspension densimeter ( $\approx 100$  ml) effects of de-mixing (due to the presence of a heavy  
150 component, heptane) were quite apparent and adversely affected the achievable repeatability  
151 of data acquired over long time period. Consequently, a vibrating tube densimeter (VTD) was  
152 employed to measure densities at pressures up to 140 MPa and temperatures up to 473.15 K  
153 using a U-shaped vibrating tube of 2 ml total volume. This relatively small size prevented the  
154 de-mixing of *n*-heptane and improved the reproducibility of our data. The overall standard  
155 uncertainty of the cell temperature was estimated to be 0.1 K based principally on temperature  
156 gradients and fluctuations. The standard uncertainty of the pressure measurement was  
157 estimated to be 0.01 MPa for the entire pressure range considered in the present work. Overall,

158 the combined standard relative uncertainty of densities measured in this work span between  
159 (0.3 and 1.2) %, due mostly to the composition uncertainty.

### 160 **2.3. Density-Magnetic-suspension balance**

161 A commercial magnetic-suspension balance [39] developed primarily for sorption analysis  
162 (type: IsoSORP, Rubotherm, Germany, and since 2016, TA instrument, USA) was used to  
163 measure the density of the ternary system (0.640 C<sub>1</sub>+ 0.098 C<sub>3</sub> + 0.261 CO<sub>2</sub>). The  
164 experimental setup was as described previously [47] and further detailed in the Supplementary  
165 Information including composition and uncertainty calculations. The overall standard  
166 uncertainty of the cell temperature was estimated to be around 0.3 K considering gradients  
167 along the measuring cell wall, the self-heating of the PRT, heat dissipation of the test leads,  
168 temperature oscillations over time. The standard uncertainty of the pressure measurement  
169 was estimated to be around 0.01 MPa for the entire pressure range considered in the present  
170 work. The combined standard relative uncertainty in densities measured with this apparatus  
171 ranged from (0.29 to 0.51) %.

172

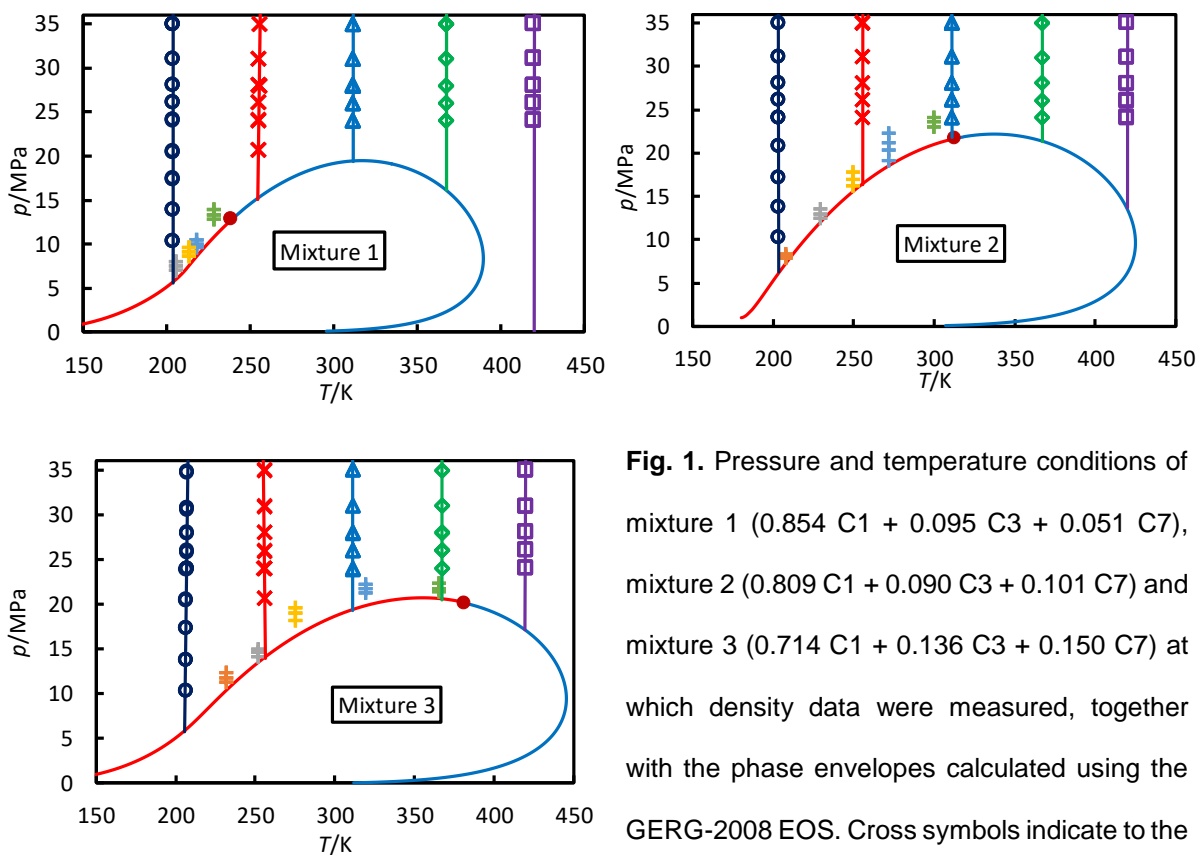
## 173 **3. Experimental Results and Discussion**

### 174 **3.1. Density of (C<sub>1</sub> + C<sub>3</sub> + C<sub>7</sub>) mixtures**

175 The vibrating tube densimeter was used to measure all the data acquired for methane +  
176 propane + *n*-heptane mixtures. Along each isotherm, density measurements were performed  
177 at every pressure for a minimum of 3 hours to check for drift with time. Additionally, a repeat  
178 measurement was made at one pressure value to check the degree of reproducibility. The  
179 experimental density results are presented in **Table 4**, together with the estimated standard  
180 uncertainties. A summary of the pressure and temperature conditions of the measurements  
181 is shown in **Fig. 1** for mixture 1 (0.854 C<sub>1</sub> + 0.095 C<sub>3</sub> + 0.051 C<sub>7</sub>), mixture 2 (0.809 C<sub>1</sub> +  
182 0.090 C<sub>3</sub> + 0.101 C<sub>7</sub>) and mixture 3 (0.714 C<sub>1</sub> + 0.136 C<sub>3</sub> + 0.150 C<sub>7</sub>), along with the



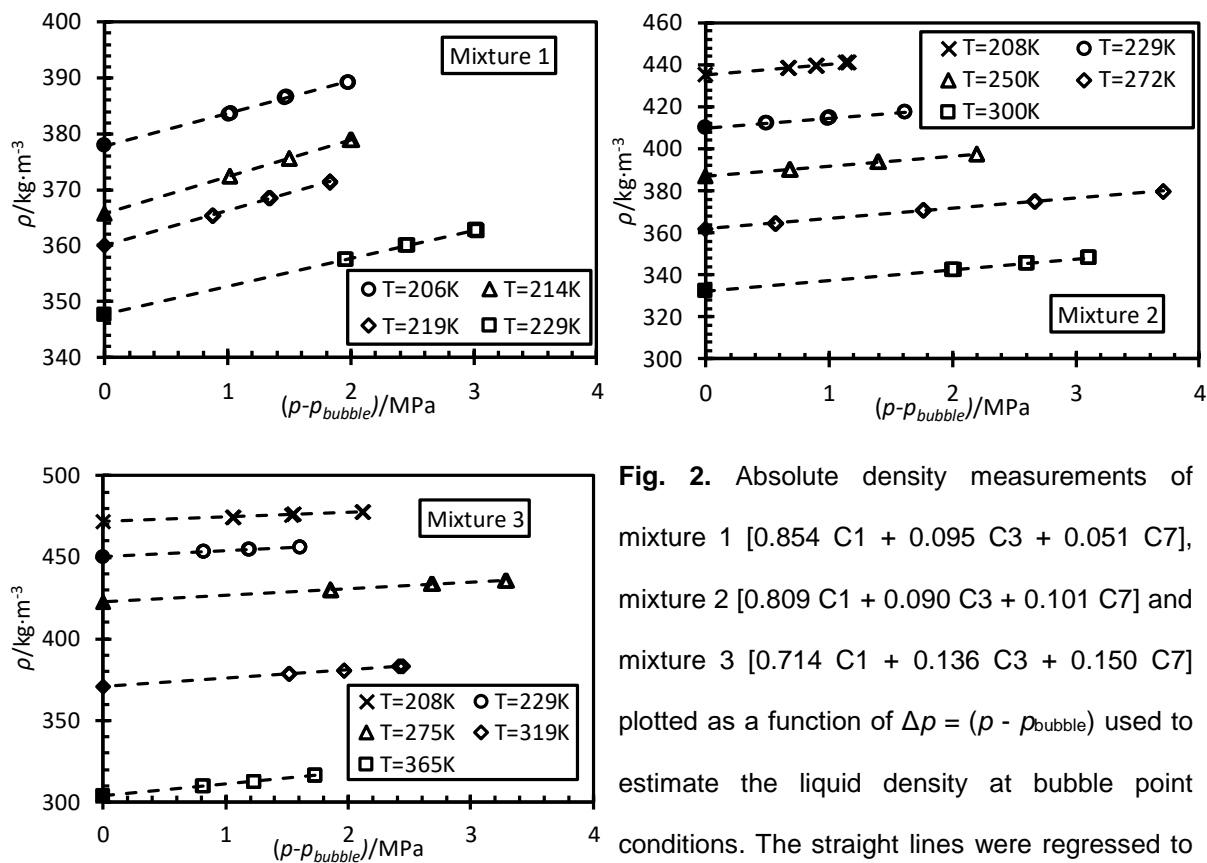
183 predicted phase envelope for each mixture as calculated from the GERG-2008 EOS [13]. The  
 184 cross symbols in **Fig. 1** correspond to the locations of the measurements used to determine  
 185 the bubble point densities via the method of linear extrapolation, which is shown in **Fig. 2**.  
 186 Overall a total of 99 density data were acquired from (170 to 548)  $\text{kg}\cdot\text{m}^{-3}$ .



**Fig. 1.** Pressure and temperature conditions of mixture 1 (0.854 C1 + 0.095 C3 + 0.051 C7), mixture 2 (0.809 C1 + 0.090 C3 + 0.101 C7) and mixture 3 (0.714 C1 + 0.136 C3 + 0.150 C7) at which density data were measured, together with the phase envelopes calculated using the GERG-2008 EOS. Cross symbols indicate to the measurements used to estimate the bubble point densities.

187 **Fig. 2** shows the measurements acquired to estimate the bubble point densities for mixtures  
 188 1, 2 and 3. The open symbols are the measurement points for each set of data and the straight  
 189 lines are linear fits of those data extrapolated to the bubble point condition predicted by the  
 190 GERG-2008 EOS. The filled black symbols are the calculated bubble point densities. A linear  
 191 extrapolation with respect to pressure was deemed sufficient given the proximity of the data  
 192 acquired to the saturation condition. Relative standard uncertainties of bubble point pressures  
 193 as predicted by GERG-2008 EOS for binary mixtures (C1 + C3, C1 + C7, C3 + C7) were

194 reported to be (1 to 3) % [13]. Consequently, estimated relative uncertainties in calculated  
 195 bubble pressures of ternary mixtures considered in this work were estimated to be 3.5%. This  
 196 contributed largely to the overall relative standard uncertainties of bubble point densities, as  
 197 shown in Table 4, which ranged from (0.5 to 1.8) %. However, this analysis does not include  
 198 errors associated with linear extrapolation with respect to pressure.

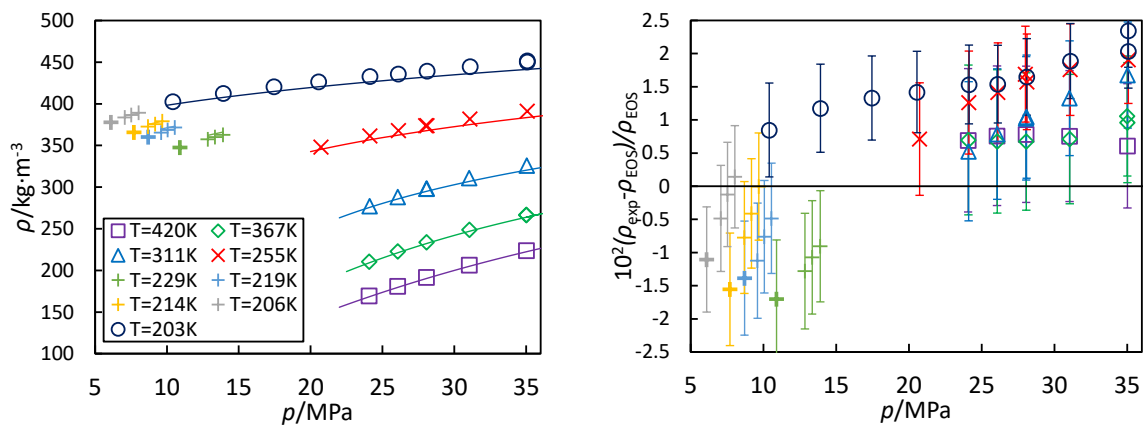


**Fig. 2.** Absolute density measurements of mixture 1 [0.854 C1 + 0.095 C3 + 0.051 C7], mixture 2 [0.809 C1 + 0.090 C3 + 0.101 C7] and mixture 3 [0.714 C1 + 0.136 C3 + 0.150 C7] plotted as a function of  $\Delta p = (p - p_{\text{bubble}})$  used to estimate the liquid density at bubble point conditions. The straight lines were regressed to the measured (hollow) data points and used to estimate the density at the EOS-predicted bubble pressure (black filled symbols)

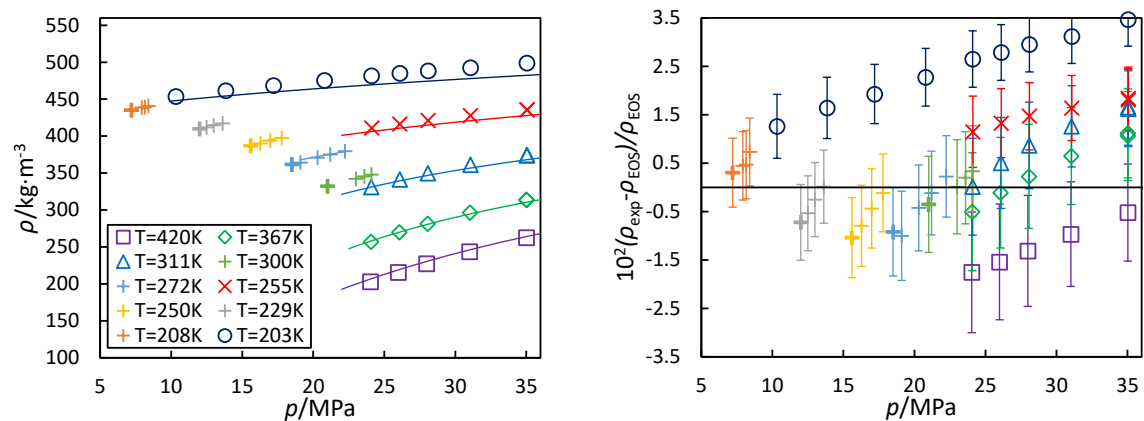
199  
 200 Density data measured for the single phase and bubble point conditions are shown in **Fig.**  
 201 **3, 4 and 5** for mixtures 1, 2 and 3, respectively. In these figures, the experimental density  
 202 is plotted as a function of pressure for each mixture. Additionally, relative deviations of the  
 203 measured densities from those calculated using the GERG-2008 model in REFPROP 10.0

204 are shown. The measured values for these mixtures follow the same trend as the predicted  
 205 values. The relative deviations between the present measurements and the predicted  
 206 values are between (- 1.5 to 2.5) %, (- 2 to 3.5) % and (0 to 4) % for mixture 1 (5 mol % n-  
 207 heptane), mixture 2 (10 mol % n-heptane) and mixture 3 (15 mol % n-heptane),  
 208 respectively. The deviations are systematically dependent on heptane content and  
 209 pressures/densities. For each isothermal measurement, observed relative deviations  
 210 increased with increasing pressures (densities). In addition, the highest relative deviations  
 211 were always observed at the lowest isothermal measurements (207 K) for all three ternary  
 212 mixtures.

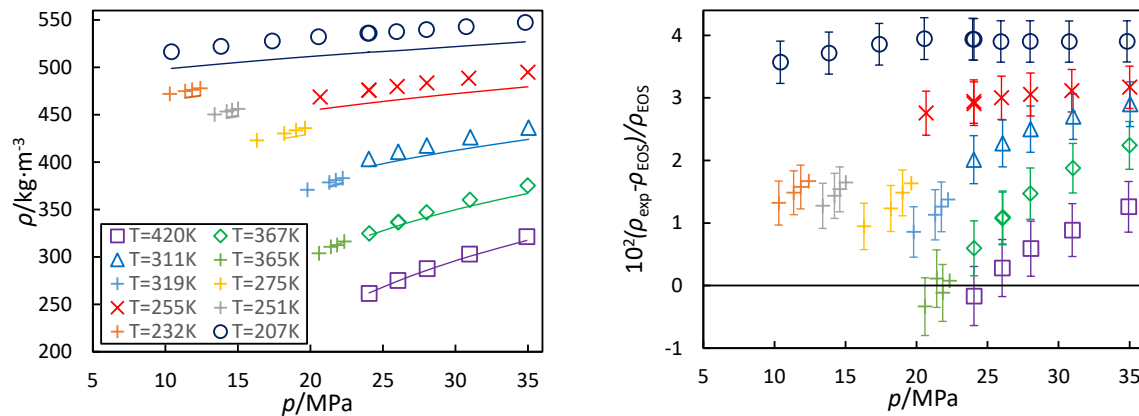
213



214 **Fig. 3.** Measured single-phase and bubble points densities for mixture 1 (0.854 C1 + 0.095 C3 + 0.051  
 215 C7) as a function of pressure, together with the densities calculated using the GERG-2008 EOS (solid  
 216 lines) (left), and relative deviations of the measured densities from those calculated using the GERG-  
 217 2008 model in REFPROP 10.0 (right).



218 **Fig. 4.** Measured single-phase and bubble points densities for mixture 2 (0.809 C1 + 0.090 C3 + 0.101  
 219 C7) as a function of pressure, together with the calculated densities using GERG-2008 EOS (solid lines),  
 220 and relative deviations of the measured densities from those calculated using the GERG-2008 model  
 221 in REFPROP 10.0  
 222



223 **Fig. 5.** Measured single-phase and bubble points densities for mixture 3 (0.714 C1 + 0.136 C3 +  
 224 0.150 C7) as a function of pressure, together with the calculated densities using GERG-2008 EOS  
 225 (solid lines), and relative deviations of the measured densities from those calculated using the GERG-  
 226 2008 model in REFPROP 10.0.

227 Overall, the relative deviations of the measured densities from those calculated using the  
 228 GERG-2008 model span from (-2 to 4) % for all mixtures. The larger deviations observed in  
 229 these mixtures reflect the absence of departure functions within the model for the component  
 230 binaries of methane + *n*-heptane and propane + *n*-heptane (as previously indicated in **Table**  
 231 **2**). Developing departure functions for these binaries would require the acquisition of sufficient  
 232 numbers of new data for them across a wide range of conditions. Unfortunately, there are  
 233 limited reference quality data to reliably represent natural gas mixtures that contain heavier  
 234 hydrocarbons (such as *n*-heptane) at high pressure and cryogenic conditions [20, 21]. For  
 235 example, the density data sets used for the two important binary systems methane and  
 236 propane, and methane and *n*-heptane in the GERG-2008 EOS have respective root mean  
 237 square relative density deviations of (0.4 to 0.8) % and (0.9 to 2.5) % from the EOS [21].

238 The extensive set of literature data available for the methane + propane system were used to  
 239 tune the binary interaction parameters and develop a departure function for this binary. As a  
 240 result, the deviations of the data measured for this binary from the GERG-2008 EOS were  
 241 generally within the experimental uncertainty, even though the new data were obtained at very  
 242 different conditions to those used in the model development [36, 39]. However, for the binaries  
 243 of methane + *n*-heptane and propane + *n*-heptane, no departure function was developed due  
 244 to the limited available data. Thus, increased deviations can be expected for the mixtures  
 245 containing *n*-heptane, as shown in this work.

246 **Table 4.** Measured single phase points and bubble points density data and their combined  
 247 uncertainty  $u_C(\rho)$  as a function of temperature  $T$  pressure  $p$  and composition for ternary Mixture  
 248 1 (0.854 C1 + 0.095 C3 + 0.051 C7), Mixture 2 (0.809 C1 + 0.090 C3 + 0.101 C7) and Mixture  
 249 3 (0.714 C1 + 0.134 C3 + 0.150 C7).

$T/K$	$p/MPa$	$x(CH_4)$	$x(C_3H_8)$	$x(C_7H_{16})$	$\rho/kg\cdot m^{-3}$	$10^2(\rho-\rho_{GERG})/\rho_{GERG}$	$u_C(\rho)/kg\cdot m^{-3}$
203.6	10.41	0.854	0.095	0.051	402.7	0.85	2.9
203.5	13.92	0.854	0.095	0.051	412.6	1.18	2.7
203.5	17.45	0.854	0.095	0.051	420.5	1.33	2.7
203.6	20.55	0.854	0.095	0.051	426.4	1.42	2.6
203.6	24.13	0.854	0.095	0.051	432.9	1.53	2.6
203.6	26.10	0.854	0.095	0.051	435.9	1.54	2.6
203.6	28.10	0.854	0.095	0.051	439.3	1.65	2.5
203.6	31.09	0.854	0.095	0.051	444.5	1.89	2.5
203.6	35.08	0.854	0.095	0.051	450.3	2.03	2.5
203.6	35.08	0.854	0.095	0.051	451.7	2.35	2.5
255.2	20.73	0.854	0.095	0.051	348.1	0.71	3.0
255.3	24.12	0.854	0.095	0.051	361.4	1.26	2.8
255.3	26.12	0.854	0.095	0.051	367.8	1.41	2.7
255.3	28.10	0.854	0.095	0.051	373.8	1.57	2.7

<i>T/K</i>	<i>p/MPa</i>	<i>x(CH<sub>4</sub>)</i>	<i>x(C<sub>3</sub>H<sub>8</sub>)</i>	<i>x(C<sub>7</sub>H<sub>16</sub>)</i>	<i>ρ/kg·m<sup>-3</sup></i>	<i>10<sup>2</sup>(ρ-ρ<sub>GERG</sub>)/ρ<sub>GERG</sub></i>	<i>u<sub>C</sub>(ρ)/kg·m<sup>-3</sup></i>
255.5	28.01	0.854	0.095	0.051	373.6	1.69	2.7
255.3	31.08	0.854	0.095	0.051	381.7	1.76	2.6
255.3	35.08	0.854	0.095	0.051	391.0	1.91	2.6
311.2	24.10	0.854	0.095	0.051	277.1	0.53	2.9
311.2	26.07	0.854	0.095	0.051	288.0	0.79	2.8
311.2	28.06	0.854	0.095	0.051	297.9	1.02	2.8
311.2	28.09	0.854	0.095	0.051	298.1	1.05	2.8
311.2	31.04	0.854	0.095	0.051	310.9	1.33	2.7
311.2	35.04	0.854	0.095	0.051	325.8	1.68	2.6
367.2	24.08	0.854	0.095	0.051	210.5	0.70	2.4
367.2	26.07	0.854	0.095	0.051	222.6	0.68	2.4
367.2	28.07	0.854	0.095	0.051	233.8	0.68	2.4
367.2	31.05	0.854	0.095	0.051	248.7	0.71	2.4
367.2	35.02	0.854	0.095	0.051	266.4	0.96	2.4
367.2	35.01	0.854	0.095	0.051	266.6	1.06	2.4
419.9	24.06	0.854	0.095	0.051	169.5	0.69	1.8
419.9	26.05	0.854	0.095	0.051	181.0	0.76	1.9
419.9	28.05	0.854	0.095	0.051	191.8	0.78	2.0
419.9	31.04	0.854	0.095	0.051	206.5	0.76	2.0
419.9	35.01	0.854	0.095	0.051	223.7	0.61	2.1
205.7	6.10	0.854	0.095	0.051	377.9*	-1.10	3.3
205.7	7.07	0.854	0.095	0.051	383.7	-0.48	3.1
205.7	7.53	0.854	0.095	0.051	386.6	-0.12	3.0
205.7	8.03	0.854	0.095	0.051	389.3	0.14	3.0
213.6	7.70	0.854	0.095	0.051	365.8*	-1.56	3.6
213.6	8.69	0.854	0.095	0.051	372.5	-0.77	3.1

<i>T/K</i>	<i>p/MPa</i>	<i>x(CH<sub>4</sub>)</i>	<i>x(C<sub>3</sub>H<sub>8</sub>)</i>	<i>x(C<sub>7</sub>H<sub>16</sub>)</i>	<i>ρ/kg·m<sup>-3</sup></i>	<i>10<sup>2</sup>(ρ-ρ<sub>GERG</sub>)/ρ<sub>GERG</sub></i>	<i>u<sub>C</sub>(ρ)/kg·m<sup>-3</sup></i>
213.6	9.18	0.854	0.095	0.051	375.6	-0.41	3.1
213.6	9.68	0.854	0.095	0.051	379.0	0.00	3.1
218.2	8.70	0.854	0.095	0.051	360.1*	-1.39	3.6
218.2	9.60	0.854	0.095	0.051	365.4	-1.12	3.2
218.2	10.06	0.854	0.095	0.051	368.5	-0.76	3.1
218.2	10.56	0.854	0.095	0.051	371.4	-0.48	3.1
228.5	10.90	0.854	0.095	0.051	347.7*	-1.70	3.6
228.5	12.85	0.854	0.095	0.051	357.5	-1.28	3.1
228.5	13.35	0.854	0.095	0.051	360.1	-1.07	3.1
228.5	13.91	0.854	0.095	0.051	362.8	-0.90	3.0
203.5	10.33	0.809	0.090	0.101	453.7	1.26	3.0
203.4	13.85	0.809	0.090	0.101	461.7	1.64	2.9
203.4	17.20	0.809	0.090	0.101	468.5	1.93	2.9
203.4	20.79	0.809	0.090	0.101	475.5	2.27	2.8
203.5	24.10	0.809	0.090	0.101	481.8	2.65	2.8
203.4	26.11	0.809	0.090	0.101	485.1	2.79	2.8
203.4	28.10	0.809	0.090	0.101	488.4	2.95	2.8
203.4	31.07	0.809	0.090	0.101	492.7	3.12	2.8
203.5	35.05	0.809	0.090	0.101	498.9	3.47	2.7
255.5	24.12	0.809	0.090	0.101	411.0	1.15	3.0
255.5	26.11	0.809	0.090	0.101	416.3	1.33	3.0
255.5	28.10	0.809	0.090	0.101	421.2	1.47	2.9
255.5	31.07	0.809	0.090	0.101	427.8	1.64	2.9
255.5	35.05	0.809	0.090	0.101	435.7	1.81	2.8
255.5	35.06	0.809	0.090	0.101	435.8	1.84	2.8
311.2	24.10	0.809	0.090	0.101	331.2	0.01	3.3

<i>T/K</i>	<i>p/MPa</i>	<i>x(CH<sub>4</sub>)</i>	<i>x(C<sub>3</sub>H<sub>8</sub>)</i>	<i>x(C<sub>7</sub>H<sub>16</sub>)</i>	<i>ρ/kg·m<sup>-3</sup></i>	<i>10<sup>2</sup>(ρ-ρ<sub>GERG</sub>)/ρ<sub>GERG</sub></i>	<i>u<sub>C</sub>(ρ)/kg·m<sup>-3</sup></i>
311.2	26.10	0.809	0.090	0.101	341.2	0.50	3.2
311.2	28.08	0.809	0.090	0.101	349.9	0.86	3.1
311.2	31.07	0.809	0.090	0.101	361.3	1.26	3.0
311.2	35.05	0.809	0.090	0.101	374.2	1.65	2.9
311.2	35.06	0.809	0.090	0.101	374.1	1.62	2.9
367.2	24.07	0.809	0.090	0.101	256.9	-0.50	3.1
367.2	26.06	0.809	0.090	0.101	269.8	-0.11	3.1
367.2	28.06	0.809	0.090	0.101	281.3	0.22	3.0
367.2	31.05	0.809	0.090	0.101	296.5	0.64	3.0
367.2	35.02	0.809	0.090	0.101	313.8	1.12	2.9
367.2	35.03	0.809	0.090	0.101	313.7	1.06	2.9
419.9	24.03	0.809	0.090	0.101	203.0	-1.76	2.5
419.9	25.99	0.809	0.090	0.101	215.5	-1.54	2.6
419.9	27.99	0.809	0.090	0.101	227.3	-1.32	2.6
419.9	31.01	0.809	0.090	0.101	243.6	-0.97	2.6
419.9	35.02	0.809	0.090	0.101	262.6	-0.52	2.6
207.8	7.20	0.809	0.090	0.101	435.1*	0.30	3.3
207.8	7.92	0.809	0.090	0.101	438.5	0.44	3.1
207.8	8.15	0.809	0.090	0.101	439.2	0.47	3.1
207.8	8.40	0.809	0.090	0.101	440.9	0.73	3.1
229.3	12.00	0.809	0.090	0.101	409.8*	-0.72	3.7
229.3	12.50	0.809	0.090	0.101	412.0	-0.54	3.2
229.3	13.00	0.809	0.090	0.101	414.5	-0.25	3.2
229.3	13.62	0.809	0.090	0.101	417.2	0.01	3.1
249.8	15.60	0.809	0.090	0.101	386.9*	-1.04	4.1
249.8	16.27	0.809	0.090	0.101	390.1	-0.80	3.3



<i>T/K</i>	<i>p/MPa</i>	<i>x(CH<sub>4</sub>)</i>	<i>x(C<sub>3</sub>H<sub>8</sub>)</i>	<i>x(C<sub>7</sub>H<sub>16</sub>)</i>	<i>ρ/kg·m<sup>-3</sup></i>	<i>10<sup>2</sup>(ρ-ρ<sub>GERG</sub>)/ρ<sub>GERG</sub></i>	<i>u<sub>C</sub>(ρ)/kg·m<sup>-3</sup></i>
249.8	16.99	0.809	0.090	0.101	393.7	-0.44	3.2
249.8	17.79	0.809	0.090	0.101	397.3	-0.12	3.2
272.2	18.50	0.809	0.090	0.101	361.8*	-0.92	4.6
272.2	19.10	0.809	0.090	0.101	364.3	-1.00	3.4
272.2	20.30	0.809	0.090	0.101	370.8	-0.43	3.3
272.2	21.20	0.809	0.090	0.101	375.0	-0.12	3.2
272.2	22.25	0.809	0.090	0.101	379.7	0.22	3.2
299.9	21.00	0.809	0.090	0.101	332.1*	-0.35	5.0
299.9	23.00	0.809	0.090	0.101	342.3	0.01	3.3
299.9	23.60	0.809	0.090	0.101	345.5	0.20	3.3
299.9	24.10	0.809	0.090	0.101	347.9	0.33	3.3
206.5	10.41	0.714	0.136	0.150	516.7	3.57	1.7
206.5	13.83	0.714	0.136	0.150	522.4	3.72	1.8
206.5	17.37	0.714	0.136	0.150	527.9	3.86	1.8
206.5	20.55	0.714	0.136	0.150	532.3	3.95	1.8
206.7	24.04	0.714	0.136	0.150	536.2	3.94	1.8
206.6	23.95	0.714	0.136	0.150	536.2	3.94	1.8
207.1	25.94	0.714	0.136	0.150	537.8	3.90	1.8
207.1	28.00	0.714	0.136	0.150	540.0	3.90	1.8
206.9	30.74	0.714	0.136	0.150	543.1	3.90	1.8
206.6	34.81	0.714	0.136	0.150	547.5	3.90	1.8
255.4	20.68	0.714	0.136	0.150	468.7	2.76	1.6
255.4	24.03	0.714	0.136	0.150	476.1	2.94	1.7
255.4	24.05	0.714	0.136	0.150	475.9	2.91	1.7
255.4	25.98	0.714	0.136	0.150	479.9	3.00	1.7
255.4	28.03	0.714	0.136	0.150	483.6	3.05	1.7

<i>T/K</i>	<i>p/MPa</i>	<i>x(CH<sub>4</sub>)</i>	<i>x(C<sub>3</sub>H<sub>8</sub>)</i>	<i>x(C<sub>7</sub>H<sub>16</sub>)</i>	<i>ρ/kg·m<sup>-3</sup></i>	<i>10<sup>2</sup>(ρ-ρ<sub>GERG</sub>)/ρ<sub>GERG</sub></i>	<i>u<sub>C</sub>(ρ)/kg·m<sup>-3</sup></i>
255.4	30.93	0.714	0.136	0.150	488.5	3.11	1.7
255.4	35.00	0.714	0.136	0.150	494.8	3.17	1.7
310.9	24.03	0.714	0.136	0.150	403.4	2.01	1.5
310.9	26.06	0.714	0.136	0.150	410.8	2.27	1.5
310.9	28.02	0.714	0.136	0.150	417.4	2.50	1.5
310.9	31.03	0.714	0.136	0.150	426.2	2.70	1.5
310.9	35.04	0.714	0.136	0.150	436.3	2.90	1.6
367.2	24.05	0.714	0.136	0.150	324.9	0.59	1.4
367.2	26.05	0.714	0.136	0.150	336.6	1.07	1.4
367.2	26.07	0.714	0.136	0.150	336.8	1.09	1.4
367.2	28.01	0.714	0.136	0.150	346.9	1.47	1.4
367.2	31.01	0.714	0.136	0.150	360.3	1.88	1.4
367.2	34.99	0.714	0.136	0.150	375.3	2.24	1.4
419.8	24.04	0.714	0.136	0.150	261.6	-0.17	1.2
419.8	26.03	0.714	0.136	0.150	275.4	0.28	1.3
419.8	28.05	0.714	0.136	0.150	287.7	0.59	1.3
419.8	30.97	0.714	0.136	0.150	303.2	0.89	1.3
419.8	34.93	0.714	0.136	0.150	321.4	1.26	1.3
231.6	10.30	0.714	0.136	0.150	472.0*	1.32	2.0
231.6	11.36	0.714	0.136	0.150	474.9	1.48	1.7
231.6	11.85	0.714	0.136	0.150	476.3	1.58	1.7
231.6	12.42	0.714	0.136	0.150	477.9	1.67	1.7
251.6	13.40	0.714	0.136	0.150	450.4*	1.27	2.3
251.6	14.23	0.714	0.136	0.150	453.4	1.43	1.6
251.6	14.60	0.714	0.136	0.150	454.8	1.54	1.6
251.6	15.02	0.714	0.136	0.150	456.2	1.65	1.6

$T/K$	$p/\text{MPa}$	$x(\text{CH}_4)$	$x(\text{C}_3\text{H}_8)$	$x(\text{C}_7\text{H}_{16})$	$\rho/\text{kg}\cdot\text{m}^{-3}$	$10^2(\rho-\rho_{\text{GERG}})/\rho_{\text{GERG}}$	$u_c(\rho)/\text{kg}\cdot\text{m}^{-3}$
275.0	16.30	0.714	0.136	0.150	423.0*	0.95	2.8
275.1	18.19	0.714	0.136	0.150	430.3	1.23	1.6
275.1	19.02	0.714	0.136	0.150	433.7	1.48	1.6
275.0	19.62	0.714	0.136	0.150	436.0	1.63	1.6
319.3	19.80	0.714	0.136	0.150	370.9*	0.86	3.8
319.3	21.31	0.714	0.136	0.150	378.6	1.13	1.5
319.3	21.76	0.714	0.136	0.150	380.9	1.26	1.5
319.3	22.22	0.714	0.136	0.150	383.2	1.37	1.5
365.1	20.60	0.714	0.136	0.150	303.9*	-0.34	5.3
365.1	21.42	0.714	0.136	0.150	310.7	0.11	1.4
365.1	21.84	0.714	0.136	0.150	312.6	-0.12	1.4
365.1	22.33	0.714	0.136	0.150	316.3	0.08	1.4

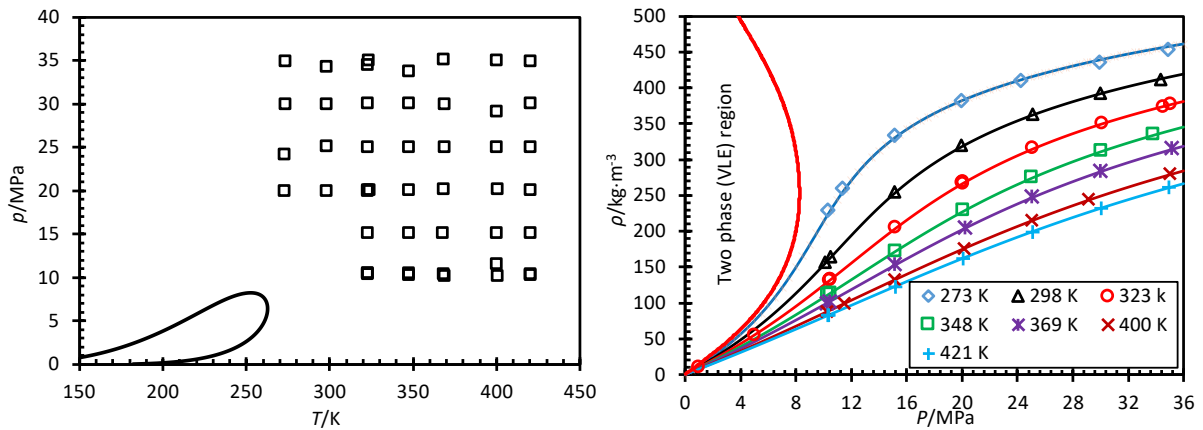
250 \* The bubble point result is obtained by the method of linear extrapolation

251 Uncertainties in temperatures:  $u(T) = 0.1$  K, pressure:  $u(p) = 0.01$  MPa and composition:  $u(x_1) = 0.008$ ,  
252  $u(x_2) = 0.008$ ,  $u(x_3) = 0.002$ .

### 253 3.2. Density of (C<sub>1</sub> + C<sub>3</sub> + CO<sub>2</sub>) mixture

254 Single-phase density measurements at temperatures of (273.3, 298.2, 323.0, 347.5, 368.6,  
255 400.2 and 420.5) K and pressures up to 35 MPa were obtained for mixture 4 (0.640 C<sub>1</sub> +  
256 0.098 C<sub>3</sub> + 0.261 CO<sub>2</sub>), using a magnetic suspension densimeter [39]. The experimental  
257 density results are given in **Table 5**, together with the estimated standard uncertainties. **Fig.**  
258 **6** shows the location in the ( $\rho$ ,  $p$ ) and ( $p$ ,  $T$ ) planes of the measurements conducted in this  
259 work for the ternary mixture, relative to its phase envelope, which was calculated using the  
260 GERG-2008 EOS [13] as implemented in the software REFPROP 10.0 [46]. Additionally,  
261 relative deviations of the measured densities from those calculated using the GERG-2008 are  
262 shown in **Fig.7**. Overall, a total of 47 density data were acquired from (83 to 456) kg·m<sup>-3</sup>. The  
263 relative deviations of the measured densities from those calculated using the GERG-2008

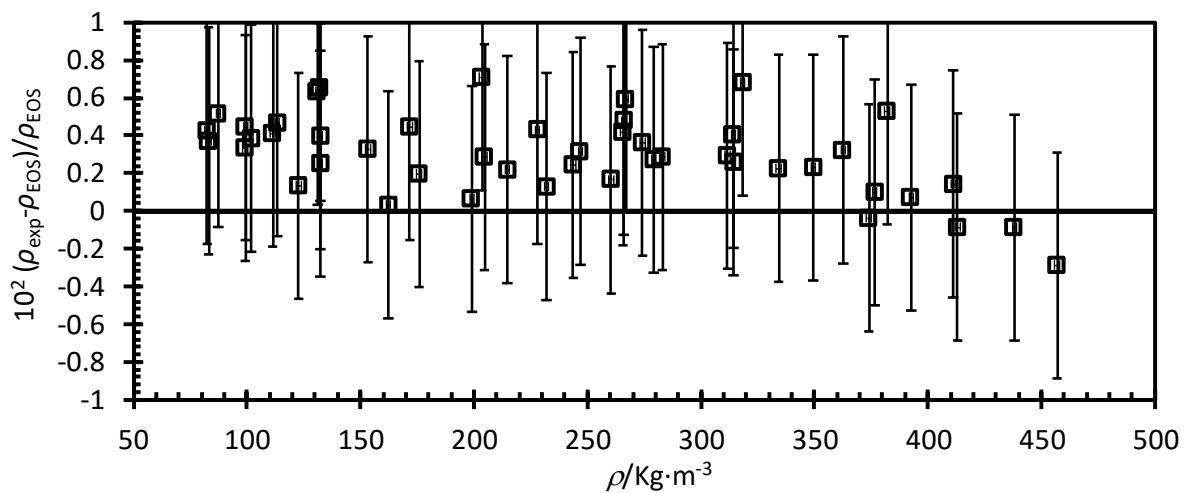
264 EOS [13] span from (-0.3 to +0.7) %, which is nearly within the combined uncertainty of the  
 265 measurements. Extensive literature data for the methane + propane and methane + carbon  
 266 dioxide were available and used to tune the binary interaction parameters and to develop  
 267 departure functions for these binaries. As a result, the deviations of the data measured from  
 268 GERG-2008 EOS are generally within the experimental and model uncertainty.



269

270 **Fig. 6.** Pressure, density and temperature conditions of the ternary mixture (0.640 C1 + 0.098 C3 +  
 271 0.261 CO<sub>2</sub>) density data measured in this work, together with its phase envelope calculated using the  
 272 GERG-2008 EOS.

273



274

275 **Fig. 7.** Relative deviations of the measured densities from those calculated using the GERG-2008  
 276 model in REFPROP 10.0.

277

278 **Table 5.** Experimental density data and combined standard ( $k = 1$ ) uncertainties for the (0.6401 C1 +  
 279 0.0984 C3 + 0.2615 CO<sub>2</sub>) mixture and their relative deviations from values calculated with the GERG-  
 280 2008 equation of state.

<i>T/K</i>	<i>p/MPa</i>	<i>ρ/kg·m<sup>-3</sup></i>	$10^2(\rho-\rho_{\text{GERG}})/\rho_{\text{GERG}}$	<i>uc(ρ)/kg·m<sup>-3</sup></i>
273.07	19.93	384.1	0.53	0.41
273.04	24.21	411.8	0.14	0.35
273.60	29.94	437.8	-0.09	0.31
273.49	34.89	455.7	-0.29	0.29
298.03	19.95	320.6	0.68	0.46
298.25	25.11	363.8	0.32	0.38
298.22	30.01	392.9	0.07	0.34
298.17	34.32	412.8	-0.08	0.32
322.95	10.42	131.9	0.63	0.48
322.93	15.17	205.0	0.71	0.51
322.96	20.10	268.6	0.59	0.46
323.01	25.06	315.5	0.40	0.40
323.01	30.09	350.4	0.23	0.36
323.03	35.06	376.9	0.10	0.33
322.94	10.50	133.1	0.66	0.49
322.96	10.50	132.8	0.40	0.50
323.68	20.10	266.9	0.42	0.46
323.00	20.01	267.2	0.48	0.46
323.02	34.53	373.9	-0.04	0.33
347.31	10.30	111.9	0.41	0.42
347.48	15.16	172.5	0.44	0.45
347.48	20.09	229.0	0.43	0.44
347.41	25.00	275.2	0.36	0.40
347.52	30.07	312.5	0.29	0.36
347.45	33.80	335.0	0.23	0.34
347.38	10.47	113.9	0.46	0.42

$T/K$	$p/\text{MPa}$	$\rho/\text{kg}\cdot\text{m}^{-3}$	$10^2(\rho-\rho_{\text{GERG}})/\rho_{\text{GERG}}$	$u_c(\rho)/\text{kg}\cdot\text{m}^{-3}$
368.95	10.22	99.8	0.45	0.39
367.90	15.15	153.7	0.33	0.41
368.18	20.22	205.3	0.28	0.41
368.58	25.04	247.7	0.32	0.39
368.52	29.95	283.9	0.29	0.36
368.50	35.13	315.3	0.26	0.34
368.07	10.41	102.2	0.38	0.39
400.30	10.20	87.8	0.52	0.36
400.29	15.14	132.7	0.25	0.38
400.40	20.14	176.3	0.19	0.38
400.28	25.04	215.3	0.22	0.37
400.29	29.15	244.3	0.24	0.36
400.17	35.02	280.1	0.27	0.34
400.03	11.49	99.5	0.33	0.37
420.30	10.30	82.7	0.43	0.35
420.50	15.16	122.8	0.13	0.36
420.18	20.08	162.3	0.03	0.37
420.36	25.06	199.2	0.07	0.36
420.57	30.08	232.3	0.13	0.35
420.37	34.94	260.8	0.17	0.33
420.31	10.40	83.4	0.37	0.35

281 Uncertainties in temperatures:  $u(T) = 0.3$  K, pressure:  $u(p) = 0.01$  MPa and composition:  $u(x) = 0.001$ .

282 **4. Case study - Impact of measured properties on LNG heat**  
283 **exchanger design**

284 The impact of thermodynamic property uncertainty on process simulations has been studied  
285 by multiple authors, concluding that a reference quality data for multicomponent hydrocarbon  
286 mixtures would improve the reliability of process simulations [48-50]. Dauber and Span [12]

287 examined the influence of different properties models on the simulation of the LNG liquefaction  
 288 process and LNG transport. They concluded that GERG-2008 EOS provides the highest  
 289 potential for accurate calculations of the thermodynamic properties of natural gas such as  
 290 density, heat capacity and enthalpy. However, in their work, the composition of the LNG  
 291 considered was only representative of the feed entering the main cryogenic heat exchange  
 292 (MCHE) and did not include heavy hydrocarbons (C<sub>6+</sub>) or vapor-liquid equilibrium data and  
 293 only focused on the liquefaction process.

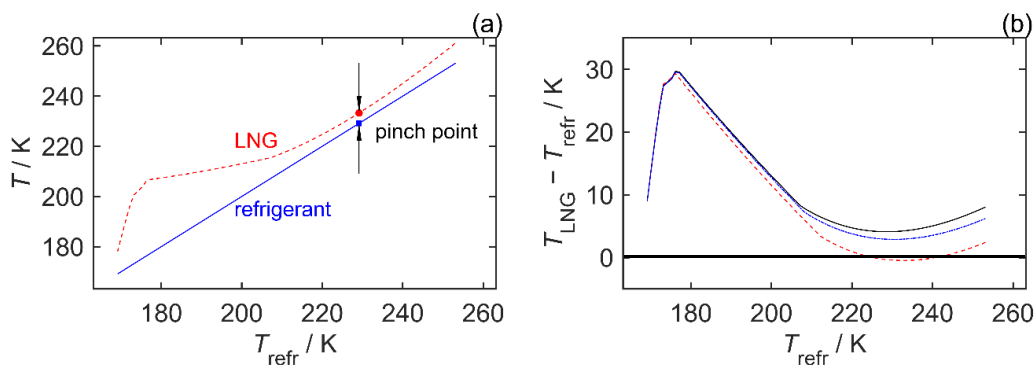
294 Here we present a case study of heat exchanger design to demonstrate the importance of the  
 295 accuracy of the fluid thermophysical properties in the LNG process. The purpose of the heat  
 296 exchanger is to cool and liquefy a quasi-LNG stream (vapour phase) to the outlet temperature  
 297  $T_{\text{LNG,out}} = 178 \text{ K}$  (liquid phase). The quasi-LNG stream is a binary (methane + ethane) mixture  
 298 with a methane mole fraction of 0.89 and with a normalized mole flowrate of  $\dot{m}_{\text{LNG}} = 1.00 \text{ mol/s}$ .  
 299 The refrigerant stream is a ternary (methane + ethane + nitrogen) mixture with an inlet  
 300 temperature  $T_{\text{refr,in}}$ , a flowrate  $\dot{m}_{\text{refr}}$  and designated mixture compositions  $x_{\text{refr}}$  of the refrigerant  
 301 stream ( $x_{\text{refr}} = [x_{\text{C1}}, x_{\text{C2}}, x_{\text{N2}}]$ ). The enthalpy profile of the quasi-LNG stream  $h_{\text{LNG}}$  can be  
 302 calculated as a function of the temperature of the refrigerant stream  $T_{\text{refr}}$  by:

$$\begin{aligned}
 h_{\text{LNG}}(T_{\text{LNG},j}) &= \left[ h_{\text{refr}}(T_{\text{refr},j}) - h_{\text{refr}}(T_{\text{refr},i}) \right] \cdot \frac{\dot{m}_{\text{refr}}}{\dot{m}_{\text{LNG}}} + h_{\text{LNG}}(T_{\text{LNG},i}) \\
 T_{\text{refr},i} &= T_{\text{refr,in}}, \text{ and } T_{\text{LNG},i} = T_{\text{LNG,out}} \text{ when } i = 0 \\
 T_{\text{refr},j} - T_{\text{refr},i} &= 1 \text{ K}
 \end{aligned}
 \tag{3}$$

303  
 304 Here the heat exchanger was broken into segments such that in each segment the  
 305 temperature changes of the refrigerant is 1 K and we assume that there are negligible heat  
 306 loss and pressure loss in both streams. In equation (3), the enthalpy of the refrigerant stream  
 307  $h_{\text{refr}}(T_{\text{refr},i})$  at each temperature  $T_{\text{refr},i}$ , and the enthalpy of the quasi-LNG stream at the outlet  
 308  $h_{\text{LNG}}(T_{\text{LNG,out}})$  can be estimated using the GERG-2008 EOS as implemented in the software  
 309 package REFPROP 10.0. Then, according to the calculated  $h_{\text{LNG}}(T_{\text{LNG},j})$ , the temperature of

310 the quasi-LNG stream  $T_{\text{LNG},j}$  can be determined. Therefore, the temperature profile of the  
 311 quasi-LNG stream  $T_{\text{LNG}}$  as a function of the temperature of the refrigerant stream  $T_{\text{refr}}$  can be  
 312 determined. An example with  $x_{\text{refr}} = [0.63, 0.32, 0.05]$ ,  $T_{\text{refr,in}} = 169$  K and  $\dot{m}_{\text{refr}} = 1.95$  mol/s in  
 313 the refrigerant stream is depicted in **Fig. 8(a)**.

314 The example as shown in **Fig. 8(a)** is a result of trial-and-error in choosing values of  $x_{\text{refr}}$ ,  $T_{\text{refr,in}}$   
 315 and  $\dot{m}_{\text{refr}}$  so that  $T_{\text{LNG}}$  is higher than  $T_{\text{refr}}$  but not by much; in this way the heat exchanger  
 316 between the two streams works efficiently. There is a pinch point, or minimum approach  
 317 temperature, where the temperature difference between the two streams  $\Delta T = T_{\text{LNG}} - T_{\text{refr}}$   
 318 reaches the smallest value with  $\Delta T_{\text{pinch}} = 4.1$  K. The value  $\Delta T_{\text{pinch}}$  is very sensitive to the values  
 319 of the fluid thermophysical properties. To demonstrate this, we present two other cases in **Fig.**  
 320 **8(b)**, one with a 1.0 % less flowrate ( $\dot{m}_{\text{refr}} = 1.93$  mol/s) and another with a change of 0.01  
 321 mole fraction in the mixture composition ( $x_{\text{refr}} = [0.64, 0.31, 0.05]$ ) in the refrigerant stream.  
 322 The first case which corresponds to a relative uncertainty in density calculation of 1.0 % shows  
 323 a reduction of  $\Delta T_{\text{pinch}}$  to 2.9 K or almost 30 % which is significant. The second case results in  
 324 a negative non-physical  $\Delta T_{\text{pinch}}$  of  $-0.5$  K which is unacceptable in the heat exchanger design.  
 325 Therefore, in order to avoid a negative value of  $\Delta T_{\text{pinch}}$  in the heat exchanger, the design  
 326 margin is high; however, if the uncertainty in the density and enthalpy calculation could be  
 327 reduced, the design margin could be reduced and thus the energy consumption and the  
 328 CAPEX and OPEX can be better optimized. The actual effect of uncertain properties such as  
 329 density in LNG heat exchanger design is even larger, because errors in calculated densities  
 330 also effect Reynolds and Nusselt numbers used in the heat exchanger design calculations.





331 **Fig. 8(a)** The temperature of the quasi-LNG stream  $T_{\text{LNG}}$  (red dashed curve) and the refrigerant stream  
332  $T_{\text{refr}}$  in a heat exchanger. (b) The temperature difference between the quasi-LNG stream and the  
333 refrigerant stream. The quasi-LNG stream is a binary (methane + ethane) mixture with a methane mole  
334 fraction of 0.89 and with a flowrate of 1.00 mol/s in both figures. The refrigerant streams are ternary  
335 (methane + ethane + nitrogen) mixtures with: mole fraction of (0.63, 0.32, 0.05) and flowrate of 1.95  
336 mol/s for (a) and the black solid curve in (b); mole fraction of (0.63, 0.32, 0.05) and flowrate of 1.93  
337 mol/s for the blue dashed dotted curve in (b); and mole fraction of (0.64, 0.31, 0.05) and flowrate of 1.95  
338 mol/s for the red dashed curve in (b).

## 339 **5. Conclusion**

340 In this work, we present a comprehensive study of two prototype systems: ( $\text{CH}_4 + \text{C}_3\text{H}_8 + \text{CO}_2$ )  
341 and ( $\text{CH}_4 + \text{C}_3\text{H}_8 + \text{C}_7\text{H}_{16}$ ); in the last of these the *n*-heptane content was up to 15 mol %,  
342 comprising accurate measurements of the saturated-phase densities and compressed-fluid  
343 (single phase) densities, at temperature from 200 K to 423 K and pressures up to 35 MPa  
344 over different ranges of compositions. The extensive experimental data collected for these  
345 mixtures were compared with the GERG-2008 EOS. The comparison shows that the relative  
346 deviations of the measured densities from those calculated using the GERG-2008 model span  
347 between (-2 to 4) % for all mixtures, exhibiting a systematic dependency on mixture density  
348 and *n*-heptane content, which is attributed to the limited experimental data available for the  
349 binary systems methane + *n*-heptane and propane + *n*-heptane. The case study on an LNG  
350 heat exchanger with a change in the density of 1 % resulted in an almost 30 % change in the  
351 minimum approach temperature, demonstrating the importance of accurate thermophysical  
352 properties to allow better equipment designs to lower energy consumption and operating  
353 costs. Current levels of uncertainty in the ISO standard for prediction of heavy hydrocarbon  
354 mixtures thermophysical properties cause predictions to be unreliable and may typically lead  
355 to significant equipment over design in industry.

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