

Citation

Yuan, C. and Chen, W. and Pham, T.M. and Hao, H. and Cui, J. and Shi, Y. 2020. Dynamic interfacial bond behaviour between basalt fiber reinforced polymer sheets and concrete. International Journal of Solids and Structures. 202: pp. 587-604. <http://doi.org/10.1016/j.ijsolstr.2020.07.007>

1 **Dynamic Interfacial Bond Behaviour between Basalt Fiber Reinforced** 2 **Polymer Sheets and Concrete**

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9 **Abstract**

10 An experimental investigation on the dynamic interfacial bond behaviour between
11 basalt fibre (BFRP) sheets and concrete under different loading speeds (i.e. 8.33E-6
12 m/s, 0.1 m/s, 1 m/s, 3 m/s, 5 m/s, and 8 m/s) by using single-lap shear tests was carried
13 out in this study. Experimental results including bond strength, strain time histories,
14 strain distributions in the bonding areas, interfacial fracture energy, and bond-slip
15 curves are presented in this study. The test results show that the interface is strain rate
16 dependent. The interfacial fracture energy, bond strength, and interfacial bond shear
17 stress-slip are sensitive to strain rate. Empirical bond-slip model including strain rate
18 effect are established for the predictions of bond properties between BFRP sheets and
19 concrete under dynamic loadings.

20 **Keywords:** Basalt fibre-reinforced polymer (BFRP); Interfacial bond behaviour;
21 Dynamic loads; Strain rate; DIC.

22 **1. Introduction**

23 Fibre-reinforced polymer (FRP), as an effective strengthening composite with high
24 strength to weight ratio and excellent corrosion resistance, has been widely used to
25 strengthen existing reinforced-concrete (RC) structures [1-4]. The interfacial bond
26 between FRP and strengthened element is the dominated factor in determining the
27 efficiency of the strengthening [5-9]. Numerous researches have been conducted to
28 investigate the bond behaviour of FRP-to-concrete interface, and some empirical
29 models have been proposed for bond strength and bond-slip relationship [10-12].
30 Mechanical properties of concrete, FRP, and adhesive resin are the main factors
31 determining the interfacial bond capacity between FRP and strengthened element [13,
32 14].

33 However, the existing studies on the interfacial bond focus primarily on the static
34 loading conditions [13, 15-20]. During the service life of civil engineering structures,
35 it is likely to be subjected to dynamic loadings, such as seismic, impact, and blast
36 loadings. A few studies [21-26] have reported that FRP strengthening is effective in
37 enhancing structures to resist impact and blast loadings. It is noted that the mechanical
38 properties of concrete and FRP are strain rate dependent [27, 28]. Since there is less
39 time for damage to develop under high strain rate, material can sustain higher load and
40 rupture strain due to the reduced accumulated damage at a particular strain level [29].
41 All the dynamic strength, the dynamic fracture strain and the dynamic Young's
42 modulus of concrete are higher than the corresponding static values [30].

43 A few studies on the bond behaviour of FRP-to-concrete interface under low strain rate
44 have been reported [31-33]. Shi et al. [31] implemented an experimental study on FRP-
45 to-concrete joints and found that the interfacial bond was strain rate dependent, and the
46 ultimate debonding strain and the peak shear stress increased with the strain rate. The
47 strain rate considered in the latter study was relatively low and less than 0.1 s^{-1} . Shen et
48 al. [32] implemented an experimental study and concluded that the effective bond
49 length decreased, and shear stress enhanced with strain rate. The peak strain rate
50 considered was 0.63 s^{-1} in the study. Huo et al. [33] experimentally tested the FRP-
51 strengthened RC beam under impact loading and it was found that the loading rate
52 remarkably influenced the bond strength while moderately affected the effective bond
53 length. The maximum strain rate in the study was about 4.9 s^{-1} . An experimental study
54 on BFRP-to-SFRC subjected to high strain rate conducted by Yuan et al. [34] found
55 that the interfacial shear resistance and shear stress enhanced remarkably compared to
56 the quasi-static tests.

57 Since the strain rate under impact and blast can reach up to 100 s^{-1} or even higher, it is
58 necessary to carry out experimental study on the dynamic interfacial bond performance
59 of FRP-to-concrete interface under higher strain rate. In order to obtain a higher strain
60 rate, this study adopted various loading speeds to simulate the high strain rate. The
61 maximum strain rate of BFRP sheet surface measured in this study was 155.1 s^{-1} under
62 the loading speed of 8 m/s . To better understand the dynamic responses of the interfacial
63 bond, dynamic testing results are compared with the results obtained from quasi-static

64 tests, such as failure modes, strain distribution, interfacial shear stress, fracture energy,
65 and bond strength. Meanwhile, an empirical dynamic model was proposed according
66 to the testing data.

67 **2. Experimental program**

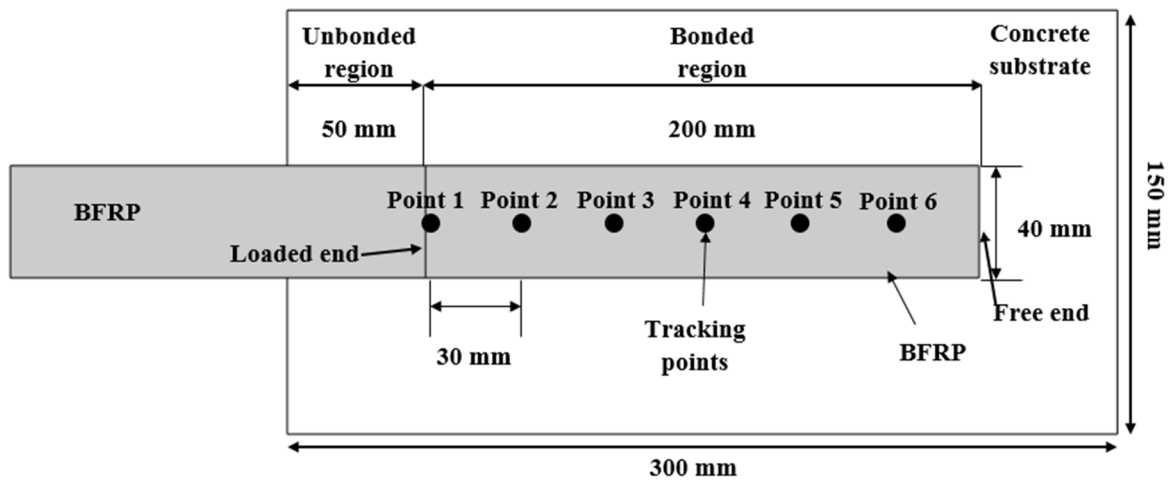
68 **2.1 Material properties**

69 The dimensions of concrete blocks were given as follows: the length was 150 mm, the
70 width was 150 mm and the height was 300 mm, as shown in Figure 1. Concrete blocks
71 with 30.14 MPa compressive strength and 2.89 MPa tensile strength were prepared in
72 this study. The maximum coarse aggregate size of 10 mm was used in the concrete
73 preparation. For the uni-directional basalt fiber (BFRP) sheet, the unit weight was 300
74 g/m²; the nominal thickness was 0.12 mm; the tensile strength was 1333 MPa; the
75 elastic modulus was 73 GPa; and the rupture strain was 1.88%. The adhesive consisting
76 two parts (i.e. epoxy resin and hardener) with a ratio of 5:1 has a rupture tensile strength
77 of 50.5 MPa, elastic modulus of 2.8 GPa and rupture strain of 4.5%.

78 **2.2 Test setup**

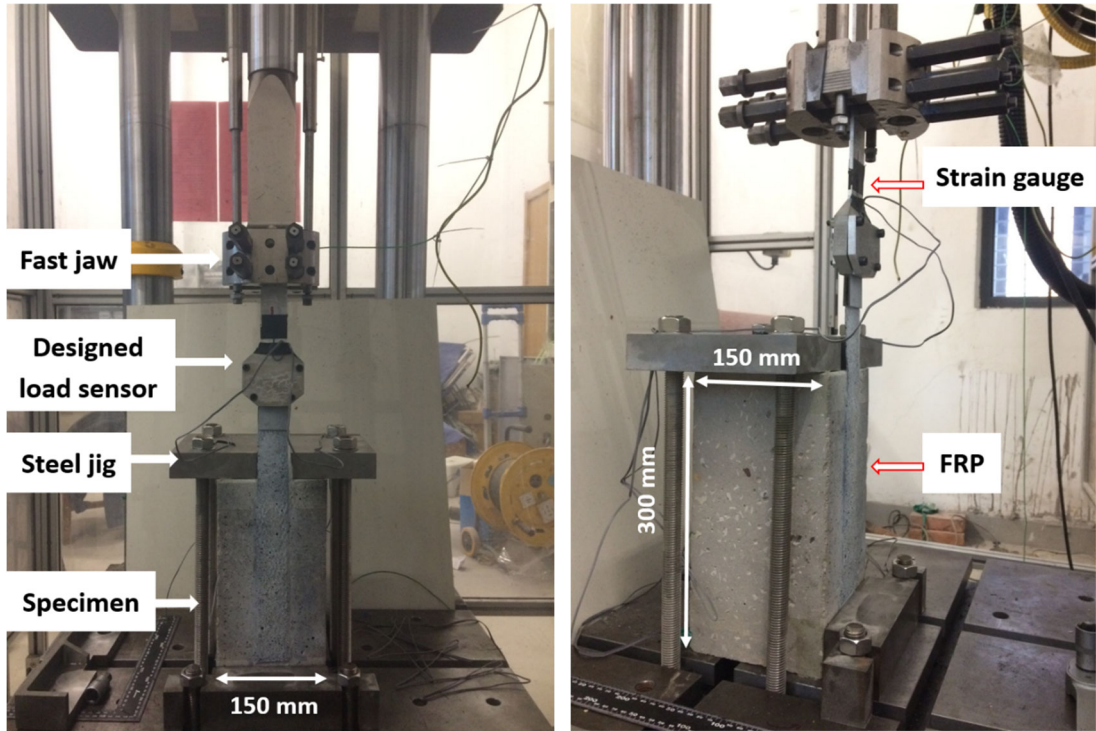
79 The single-lap shear tests (SST) were carried out by using Instron VHS 160-20 high
80 speed servo hydraulic testing machine. This machine is able to provide constant
81 velocity in the range of 0.1 m/s to 25 m/s. Figure 1 illustrates the specimen details and
82 Figure 2 shows the testing machine and experimental setup. Twenty-seven specimens
83 were tested with three specimens for each configuration in total. **Table 1** summarizes
84 the details of the specimens and the testing data. It should be noted that n_f refers to the

85 number of BFRP layers, L represents the bonding length of BFRP sheets, b_f refers to
 86 the bond width of BFRP sheets, s^{-1} is the measured strain rate, P_u represents the
 87 debonding loads, τ_m refers to the peak shear stress (PSS), s_o refers to the slip at the peak
 88 shear stress, G_f is the interfacial fracture energy (IFE), and L_e refers to the effective
 89 bond length (EBL).



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Figure 1. Specimen detail



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(a) SST: (L) Front view; (R) Side view



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(b) Test instruments: (L) Strain amplifier; (R) High speed camera

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Figure 2. Test setup and instruments

97 **Table 1.** Details of the specimens and main results for the static and dynamic tests

Specimen ID	n_f	L (mm)	b_f (mm)	Loading speed (m/s)	s^{-1}	P_u (kN)	τ_m (MPa)	s_o (mm)	G_f (N/mm)	A (%)	B (mm ⁻¹)	Le (mm)	$f_{t,DIF}$ (MPa)	Failure mode
QS_1	2	200	40	8.33E-6	2.50E-5	6.93	2.11	0.146	0.89	1.009	4.737	96	/	C
QS_2	2	200	40	8.33E-6	2.50E-5	7.87	2.20	0.131	0.70	0.897	4.897	89	/	C
QS_3	4	200	40	8.33E-6	2.50E-5	9.04	2.72	0.125	0.98	0.746	5.534	105	/	C
QS_4	4	200	40	8.33E-6	2.50E-5	8.65	2.80	0.133	1.07	0.780	5.210	96	/	C
QS_5	2	200	25	8.33E-6	2.50E-5	4.12	2.21	0.109	0.88	1.002	6.368	85	/	C
QS_6	2	200	25	8.33E-6	2.50E-5	3.69	1.97	0.138	0.78	0.946	5.021	80	/	C
D1_0.1MPS_1	2	200	40	0.1	4.50	7.00	2.95	0.131	1.11	1.128	5.295	94	3.27	C
D1_0.1MPS_2	2	200	40	0.1	4.20	7.80	2.67	0.129	0.99	1.066	5.372	87	3.21	C
D1_0.1MPS_3	2	200	40	0.1	4.11	8.08	2.65	0.139	1.06	1.103	4.978	92	3.19	C
D2_1MPS_1	2	200	40	1.0	25.80	8.01	5.34	0.130	2.00	1.512	5.331	66	5.20	C
D2_1MPS_2	2	200	40	1.0	33.20	8.02	4.89	0.131	1.84	1.452	5.297	55	5.53	C
D2_1MPS_3	2	200	40	1.0	29.40	8.40	4.85	0.125	1.75	1.415	5.541	78	5.37	C
D3_3MPS_1	2	200	40	3.0	46.60	9.91	7.03	0.119	2.41	1.661	5.815	59	6.00	C
D3_3MPS_2	2	200	40	3.0	53.50	9.50	6.85	0.127	2.51	1.694	5.457	65	6.20	C/CE
D3_3MPS_3	2	200	40	3.0	54.30	10.01	7.25	0.109	2.29	1.620	6.312	66	6.22	C/CE
D4_5MPS_1	2	200	40	5.0	103.10	12.00	8.66	0.099	2.49	1.688	6.947	48	7.19	C/CE
D4_5MPS_2	2	200	40	5.0	104.80	9.01	7.65	0.110	2.44	1.670	6.265	55	7.22	C/CE
D4_5MPS_3	2	200	40	5.0	101.60	13.12	8.64	0.101	2.51	1.693	6.879	50	7.17	C/CE
D5_8MPS_1	2	200	40	8.0	155.10	15.03	9.55	0.100	2.85	1.781	6.875	45	7.85	C/CE
D5_8MPS_2	2	200	40	8.0	150.10	12.95	9.05	0.099	2.60	1.726	6.939	48	7.80	C/CE
D5_8MPS_3	2	200	40	8.0	130.40	11.02	9.82	0.097	2.75	1.774	7.125	50	7.57	C/CE
D6_5MPS_1	4	200	40	5.0	98.70	15.62	8.47	0.101	2.47	1.182	6.860	42	7.12	C/CE
D6_5MPS_2	4	200	40	5.0	94.50	14.59	9.24	0.102	2.73	1.241	6.786	40	7.05	C/CE
D6_5MPS_3	4	200	40	5.0	92.70	13.72	9.23	0.114	3.03	1.310	6.087	46	7.02	C/CE
D7_5MPS_1	2	200	25	5.0	98.57	8.29	6.53	0.128	2.43	1.665	5.378	61	7.12	C/CE
D7_5MPS_2	2	200	25	5.0	104.51	7.33	7.60	0.139	3.05	1.866	4.984	57	7.21	C/CE
D7_5MPS_3	2	200	25	5.0	108.72	7.24	6.01	0.133	2.67	1.745	5.198	75	7.27	C/CE

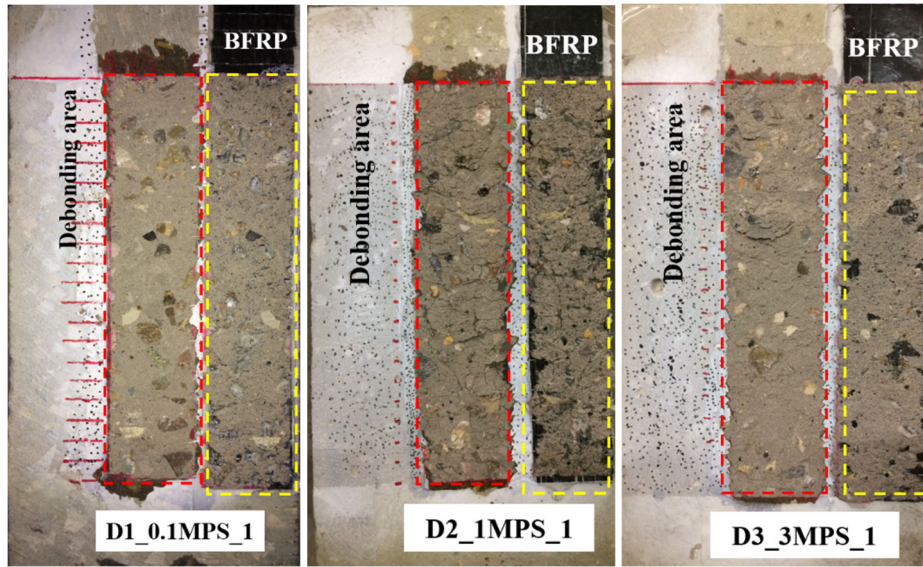
98 It should be noted that *C* refers to debonding due to concrete failure, *CE* refers to debonding in the interface of concrete-epoxy, *A* is the ultimate strain derived from the

99 regression analysis, *B* refers to the stiffness index obtained from the regression analysis, and $f_{t,DIF}$ refers to the estimated dynamic tensile strength of concrete.

100 **3. Experimental results and discussions**

101 **3.1 Failure mode**

102 The failure modes under different loading speeds are shown in Figure 3. For the specimens
103 under quasi-static loading and the dynamic loading speeds of 0.1 m/s, 1 m/s and 3 m/s,
104 debonding occurred owing to the failure of concrete substrates and a thin layer of concrete was
105 peeled off. In addition, the fracture path always penetrated through the aggregate-to-mortar
106 interface, where is the interfacial transition zone (ITZ). However, under the higher loading
107 speeds of 5 m/s and 8 m/s, the failure mode changed, as shown in Figure 3 (d), (e) and (f). The
108 peel-off failure of concrete substrate is no longer uniform. More concrete detachment was
109 observed near the loaded end. A small amount of adhesive layer, which is not very clear in the
110 photos, was found on the detached concrete substrates close to the free end. These results show
111 that the debonding failure not only occurred because of the concrete failure but also because of
112 the failure of the concrete-epoxy interface, and the failure was not uniform along the bonded
113 area. This indicates that the debonding failure was sensitive to the loading speed. The might be
114 due to the interfacial transition zone between aggregate and mortar is strong enough under
115 higher strain rate because of the enhanced concrete tensile strength. In general, high speed
116 loading leads to two possible debonding failure modes: (1) concrete failure (C) and (2)
117 concrete-epoxy (CE) interface failure. The cracking resistance of concrete and rupture
118 resistance of epoxy are enhanced under dynamic loadings. The debonding initiated from the
119 weaker layer of two interfaces (i.e. C and CE).



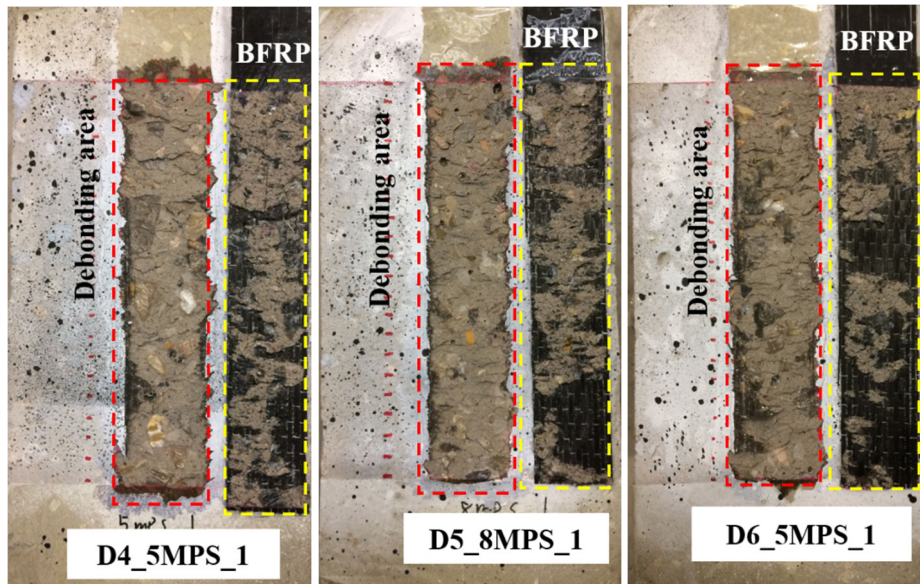
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(a) D1_0.1MPS_1

(b) D2_1MPS_1

(c) D3_3MPS_1



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(d) D4_5MPS_1

(e) D5_8MPS_1

(f) D6_5MPS_1

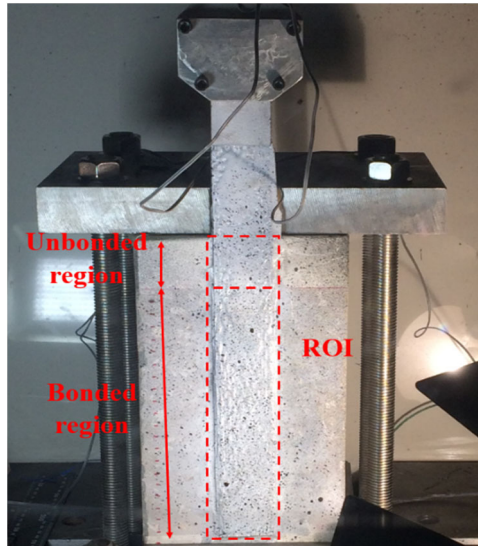
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Figure 3. Failure modes under different loading speeds

125 3.2 Load-slip relationship

126 Digital image correlation (DIC) technique was used to measure the fields of displacement and
 127 strain of the Region of Interest (ROI), which is shown in Figure 4. The reliability of the DIC
 128 technique is verified against actual reading from strain gauges as proven in the previous study
 129 by Yuan et al. [35]. Due to ringing effect, severe oscillation may be observed in the measured
 130 load-time curves. The system ringing in dynamic tests is a common phenomenon and cannot

131 be eliminated if contact measurement method is adopted [36, 37]. Therefore, DIC as the non-
132 contact measurement method was used to mitigate the vibration effect. The ROI consists of
133 two parts, one is the unbonded part which is reserved to eliminate the edge effect of concrete,
134 and the other region is the bonded part with a bond length of 200 mm.

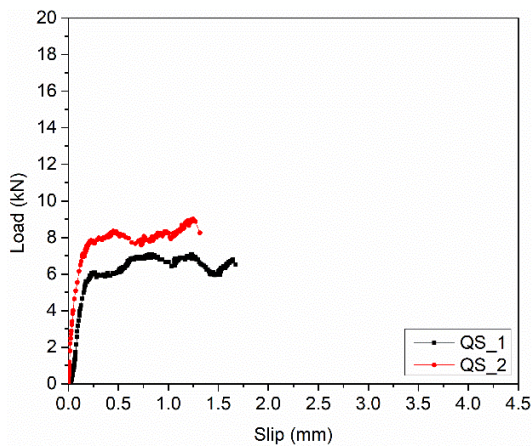


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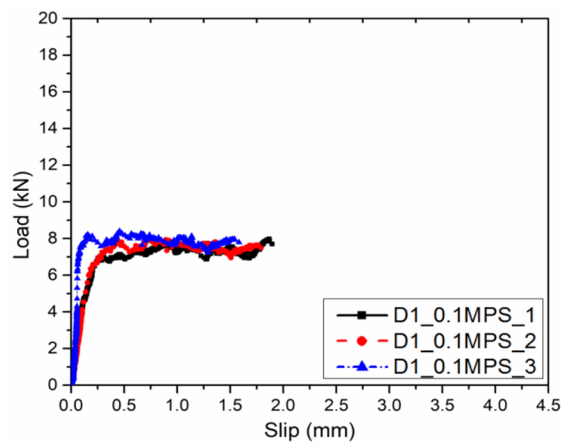
Figure 4. Region of interest (ROI)

137 Figure 5 illustrates the load-slip curves for all the tested specimens. As can be seen, the pattern
138 of the load-slip curves has not been affected by the strain rate as elastic stage and debonding
139 plateau under dynamic loadings are similar to that under quasi-static loading. The debonding
140 load and ultimate slip increased with the loading velocity. As listed in **Table 1**, the average
141 debonding loads of the specimens QS (i.e. QS_1 and QS_2), D1_0.1MPS, D2_1MPS,
142 D3_3MPS, D4_5MPS, and D5_8MPS were 7.63 kN, 8.14 kN, 9.81 kN, 11.38 kN, 13.00 kN,
143 and 14.64 kN, respectively. With the increasing strain rate from $2.59E-5 \text{ s}^{-1}$ to 4.27 s^{-1} , 29.47
144 s^{-1} , 51.47 s^{-1} , 103.17 s^{-1} , and 155.10 s^{-1} , the dynamic debonding loads increased by 3.06%,
145 10.05%, 32.52%, 53.74%, and 97.88%, respectively. This indicates that the interfacial bond
146 strength is enhanced due to the increased cracking resistance of concrete substrates under
147 dynamic loadings. In addition, the ultimate slip increased as well with the rising strain rate,
148 indicating that the debonding process under dynamic loadings is more ductile than that under

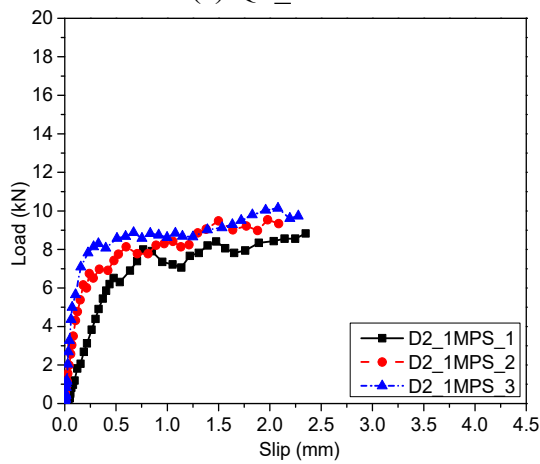
149 quasi-static loadings. Up to the loading velocity of 3 m/s, the slip at debonding load was
 150 approximately 0.25 mm while the corresponding values for the cases of 5 m/s and 8 m/s were
 151 about 0.5 mm and 0.6 mm, respectively. This is because the BFRP sheets can experience more
 152 deformation during the microcracking stage and debonding process to overcome the enhanced
 153 interfacial bond strength under dynamic loadings. The increased debonding load and slip
 154 indicate that the ductility of the single-lap shear specimens increases with the strain rate. It
 155 should be noted that only two specimens were tested under quasi-static tests.



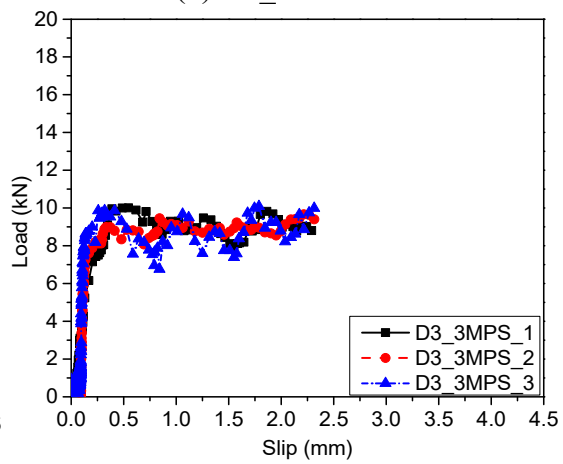
(a) QS_1 and 2



(b) D1_0.1MPS



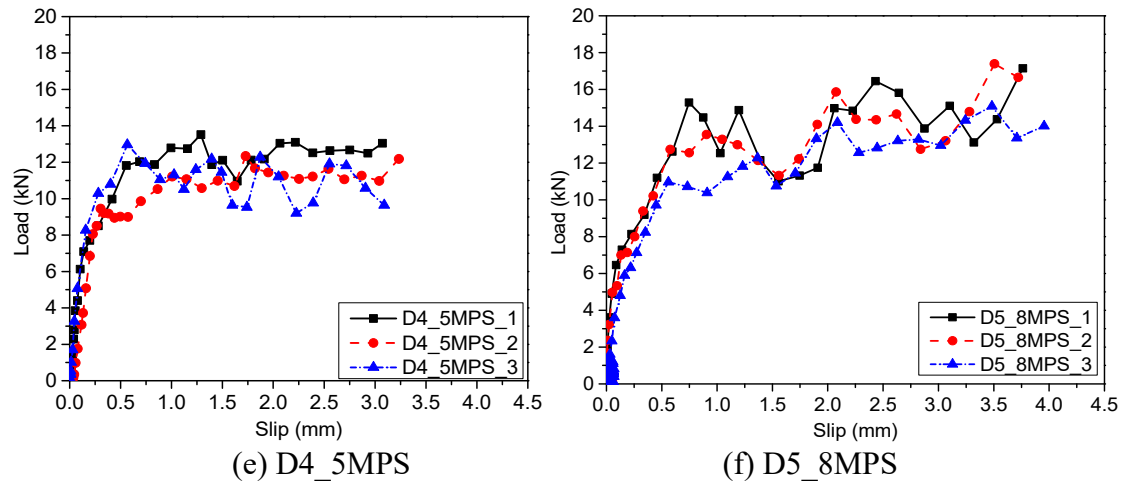
(c) D2_1MPS



(d) D3_3MPS

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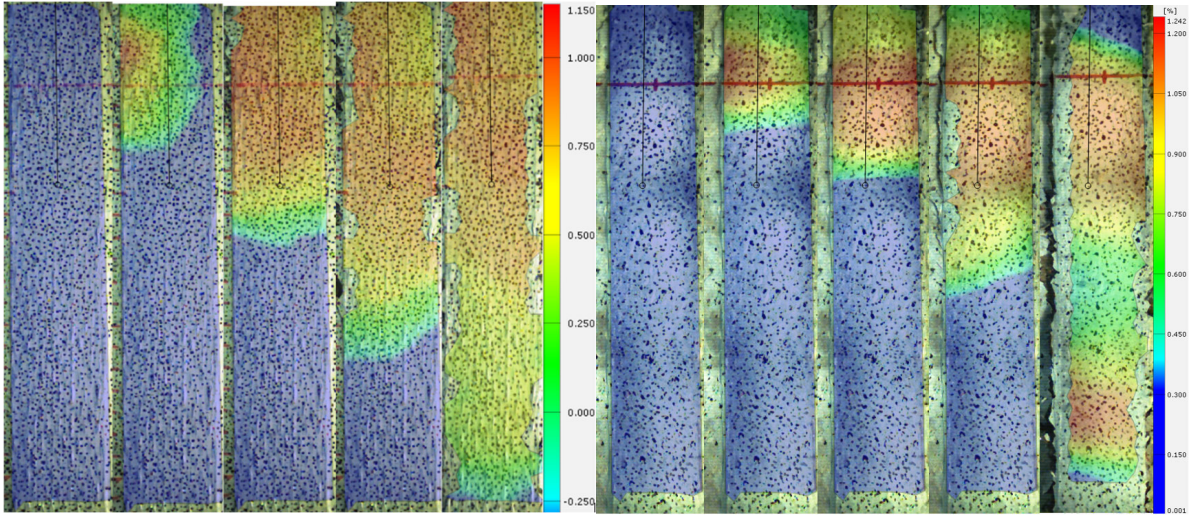
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Figure 5. Load and slip curves

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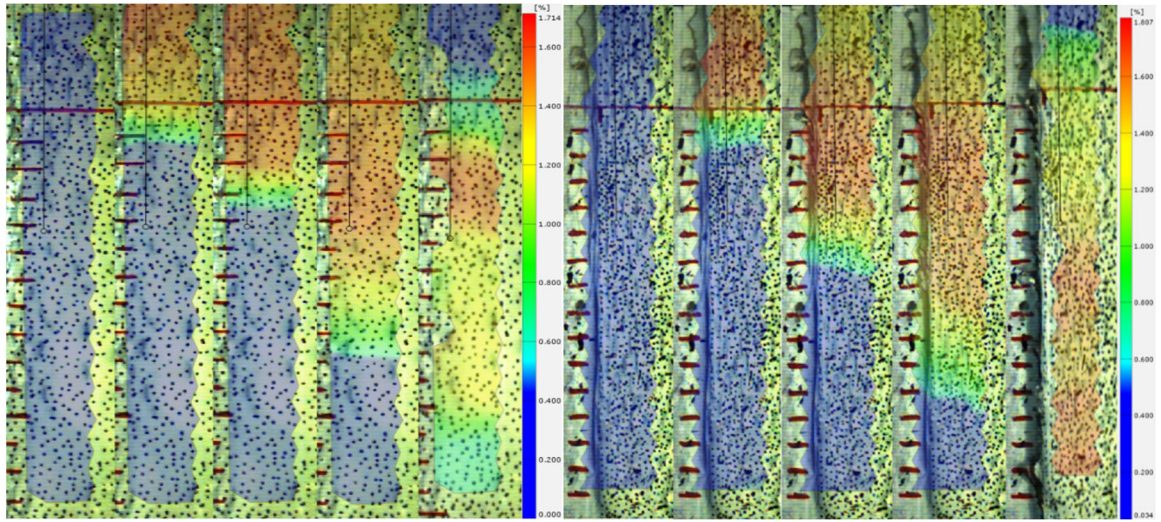
163 3.3 Strain distribution

164 FRP strain profile of each specimen under different loading stages was derived by the DIC
 165 technique. Figure 6 illustrates the strain contours with different colours. Red and blue colours
 166 represent the maximum and minimum strain. The strain contours also provide the strain value
 167 and strain transfer length of BFRP sheets. Overall, similar patterns of strain distribution along
 168 the loading direction were observed. It seems that the pattern of strain fields was not affected
 169 by strain rate. With the increasing loading speed, more uniform strain distribution was observed
 170 in the ROI. For the specimens under the loading speeds of $8.33E-6$ m/s and 0.1 m/s, non-
 171 uniform strain concentration was observed around the loaded end of the BFRP sheets at the
 172 beginning of loading, as shown in Figure 6 (a and b), indicating that the strain profile was
 173 marginally impacted by the strain rate because the cracking in the concrete layer had enough
 174 time to penetrate from the weak parts of the concrete under relatively lower loading speed (e.g.
 175 less than 0.1 m/s). The localization of strain indicates the concentration of shear stress in the
 176 red colour. The colours of yellow, green and light blue refer to the shear stress transition zone.
 177 The dark blue represents the non-stress transfer zone.



(a) QS_1

(b) D1_0.1MPS_1



(c) D3_3MPS_1

(d) D5_8MPS_1

Figure 6. Strain contours under different loading instants

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 184 Figure 7 plots the strain time histories of BFRP sheets at the selected six points indicated in
 185 Figure 1. The debonding initiated from Point 1 (closer to the loaded end) to Point 6 (closer to
 186 the free end), which is similar to the results under quasi-static loadings as reported by Baky et
 187 al. [38]. With the increase of loading speed, significantly higher ultimate debonding strain and
 188 shorter duration of loading time were obtained. As compared to the case of low loading speeds,
 189 the BFRP strain of specimens associated with high loading speeds raised much more rapidly.
 190 The FRP debonding strain raised with strain, indicating that the shear resistance of the BFRP-

191 to-concrete interface was enhanced with the strain rate. In addition, changing the BFRP sheets
 192 from two layers (Figure 7d) to four layers (Figure 7f) resulted in the decrease of the strain under
 193 the same loading velocity of 5 m/s, indicating that the increased thickness of BFRP sheets
 194 reduced the strain development under dynamic loading.

195 To obtain dynamic stress equilibrium, at least three reverberations of the loading wave in the
 196 specimen are required for a uniaxial tensile test [39, 40]. To estimate the velocity of the stress

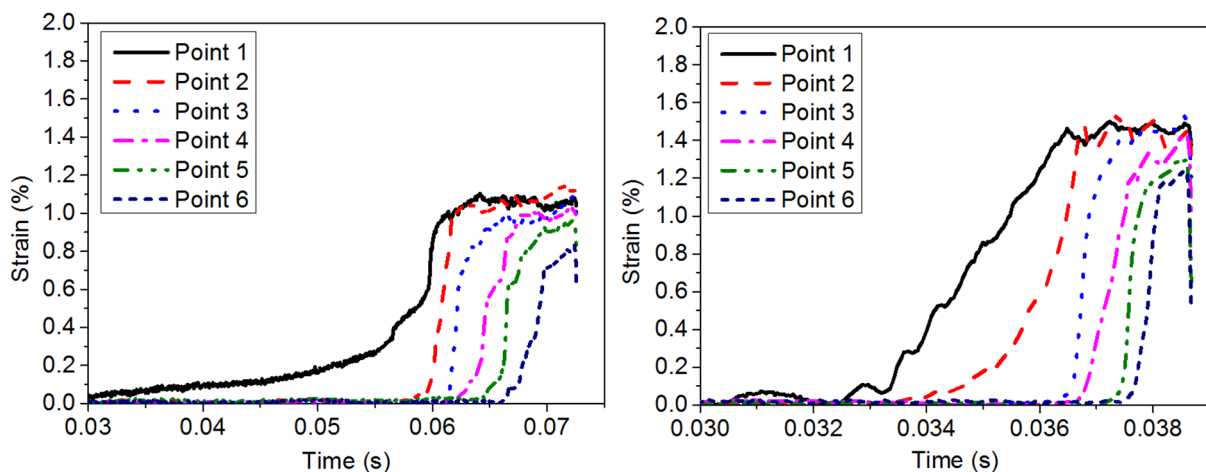
197 wave, the equation $c = \sqrt{\frac{E}{\rho}}$ can be employed. However, the stress wave velocity of the FRP-

198 to-concrete joints is not easy to estimate due to the two interfaces including BFRP-to-epoxy
 199 and epoxy-to-concrete in the FRP-to-concrete joints. The elastic modulus E and the density ρ
 200 cannot be confirmed due to the multiple interfaces. Thus, six points were selected from the

201 BFRP sheets to compare the strain distributions at different instants of time, as shown in Figure
 202 1 [41, 42]. As can be observed in Figure 7, once the strain of the first five selected points

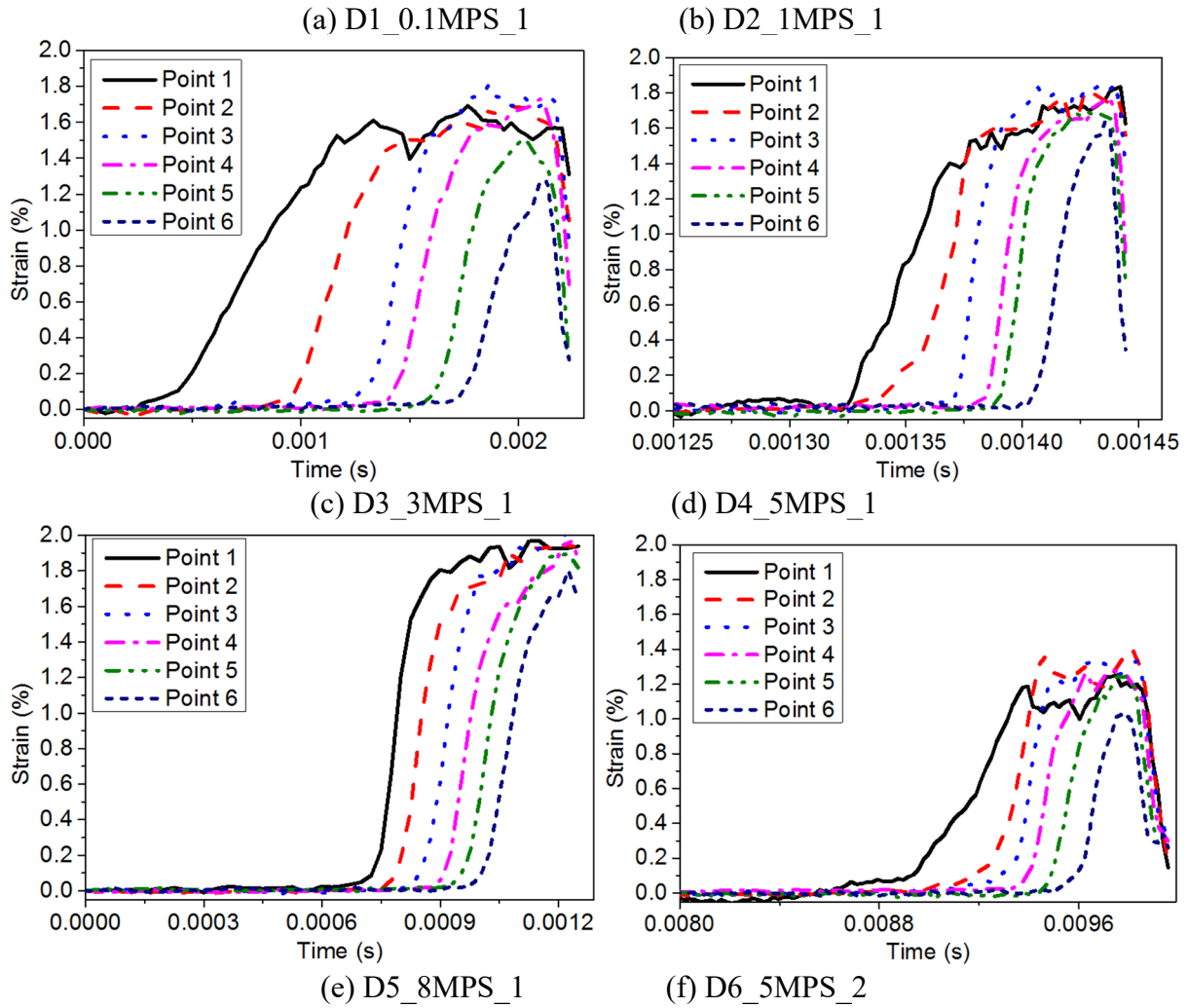
203 reaches the maximum value it remains almost a constant leading to a uniform strain distribution
 204 along the specimen, demonstrating that the dynamic SST satisfies the dynamic stress
 205 equilibrium. The reason for the different strain distribution of point 6 from the other points

206 including the shape and value is because the point closer to the free end of FRP cannot develop
 207 the full debonding process due to the brittle behaviour.



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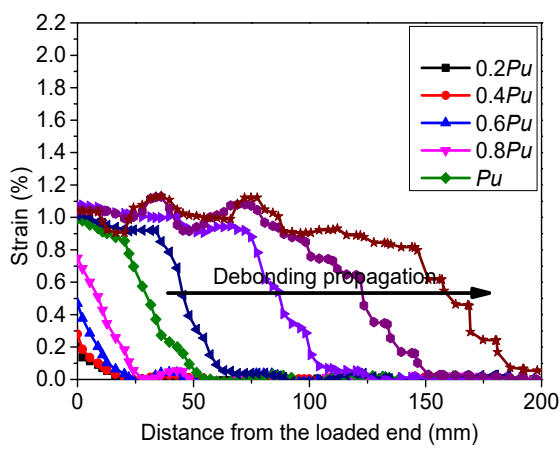
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Figure 7. Strain-time histories

215 Figure 8 shows the strain distributions along the bond length of BFRP sheets at different
 216 loading levels. For all the specimens, the strain firstly increased with the applied loads. As the
 217 applied load reached the initial debonding stage (P_u), there was nearly no further increment of
 218 the strain. The strain distribution remained “S” profile to develop the debonding process. As
 219 shown in Figure 8, the FRP debonding strain significantly raised with the rising loading rate,
 220 and the larger shear stress transfer region can be observed when the ultimate load was achieved.
 221 In addition, the BFRP strain profile under higher loading speeds is steeper than that obtained
 222 with lower loading speeds, indicating that the enhanced shear resistance is obtained for BFRP-
 223 strengthened concrete joints under higher speed loadings. Figure 8 (d) and (f) shows the strain

224 distributions by changing two layers of BFRP sheets to four layers under the same loading
 225 speed of 5 m/s. The measured results demonstrated that increasing BFRP stiffness significantly
 226 enhanced the shear resistance under dynamic loads. However, the loading speeds had marginal
 227 effect on the strain distribution gradient. The profile of the strain distribution subjected to
 228 dynamic loadings is similar to that under static tests, which has been also reported by Huo et
 229 al. [23].

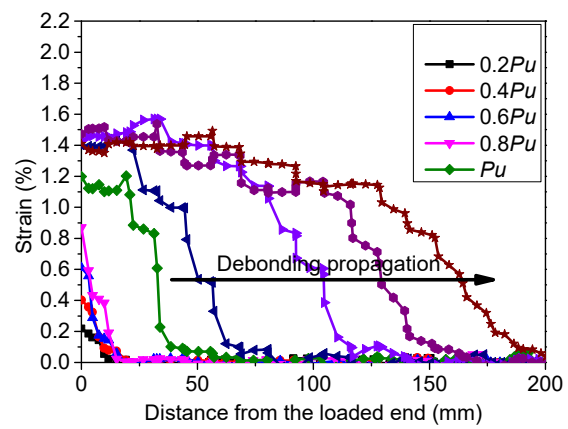
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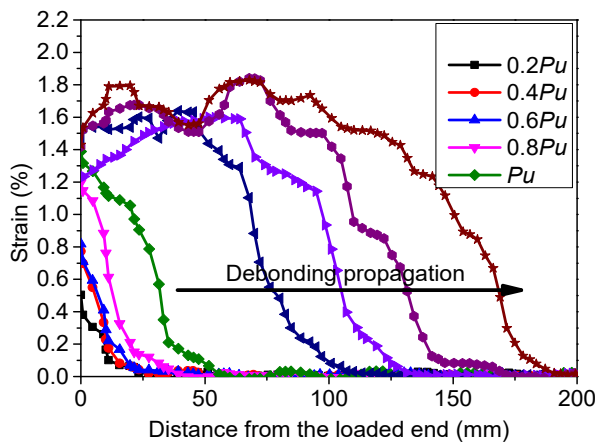
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(a) D1_0.1MPS_1



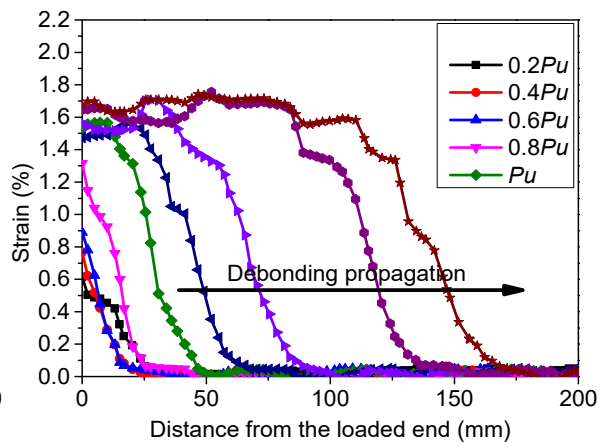
(b) D2_1MPS_1



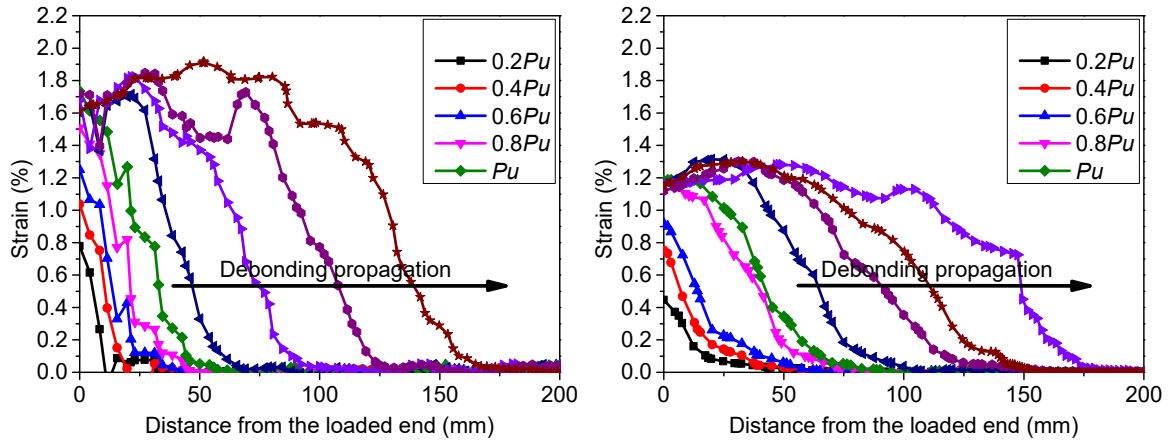
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(c) D3_3MPS_1



(d) D4_5MPS_1 (2 layers of BFRP sheets)



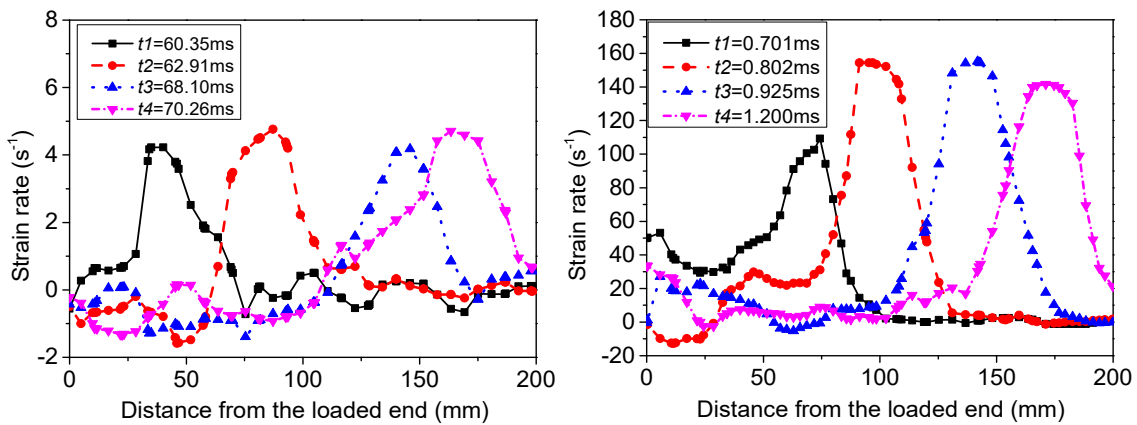
(e) D5_8MPS_1

(f) D6_5MPS_2 (4 layers of BFRP sheets)

Figure 8. Strain distributions under different loading speeds

Table 1 gives the maximum strain rate for all the tested specimens. The determination of strain rate in this study was based on the differentiation of strain time history, as given in Equation (1). In general, the peak strain rate increased with the loading speed. Figure 9 illustrates the relationship between strain rate and location at different time instants. The strain rates varied with time reaching the maximum strain rate and maintained its bell shape to propagate along the bonded length of BFRP sheets. The maximum strain rate was approximately 155.10 s^{-1} at the loading speed of 8 m/s while the strain rate was around 4 s^{-1} at the loading speed of 0.1 m/s .

$$\dot{\varepsilon} = \frac{d\varepsilon}{dt} \quad (1)$$



(a) D1_0.1MPS_1

(b) D5_8MPS_1

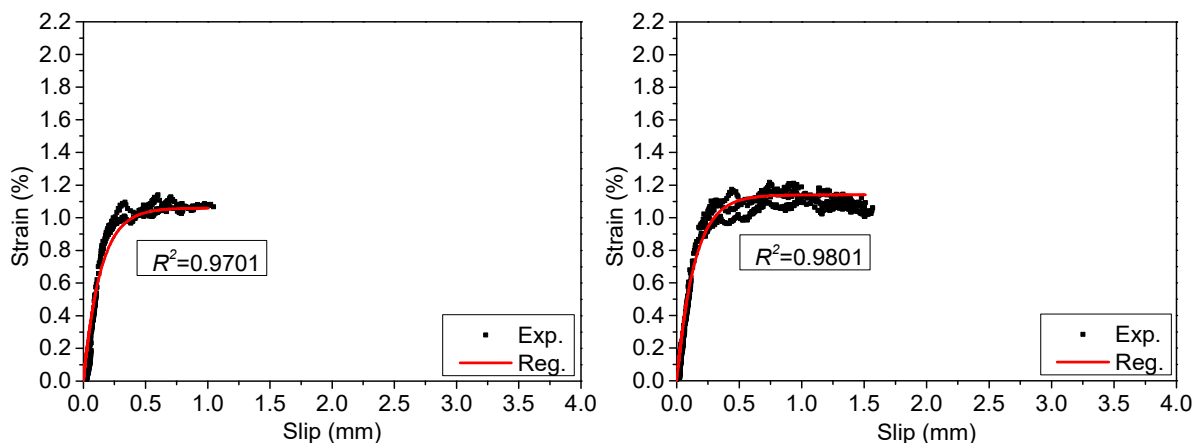
Figure 9. Strain rate distributions at different time instants

249 **3.4 Strain-slip relationship**

250 To obtain the interfacial bond-slip relationships between FRP and concrete, a non-linear fitting
 251 equation proposed by Dai et al. [16] was employed herein. Three sets of strain-slip curves
 252 corresponding to each specimen were adopted for regression analysis. Three points (i.e. Point
 253 1, Point 2, and Point 3 as shown in Figure 1) near the loaded end of BFRP sheets were selected
 254 from the DIC, as shown in Figure 10. The points close to the free end were not selected because
 255 the points near the free end cannot represent the debonding behaviour of the points close to the
 256 loaded end due to the brittle debonding of the BFRP-to-concrete interface. As proposed by Dai
 257 et al. [43], the relationship between strain and slip can be expressed as follows [10, 16]:

258
$$\varepsilon = f(s) = A(1 - e^{-Bs}) \tag{2}$$

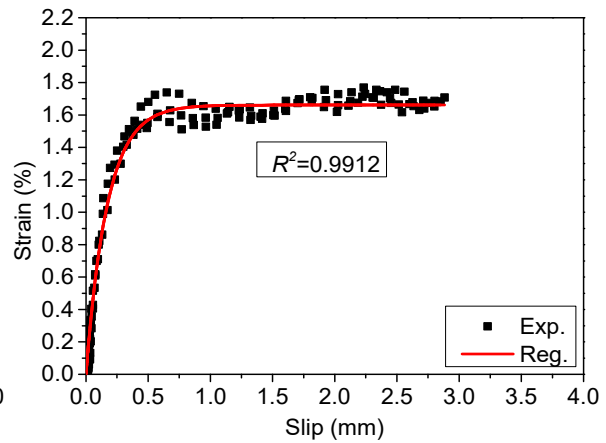
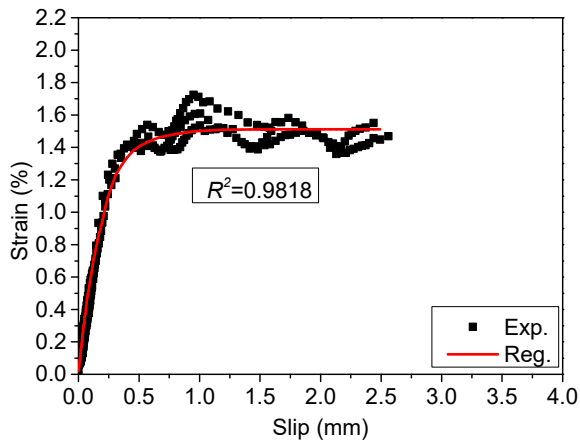
259 where A and B are the coefficients obtained from the fitted ε - s curves of experimental results,
 260 A is the ultimate debonding strain of the FRP with enough bond length, B refers to the stiffness
 261 index, which dominates the shape of the bond-slip curves [16].



262 (a) QS_1

263

(b) D1_0.1MPS_1

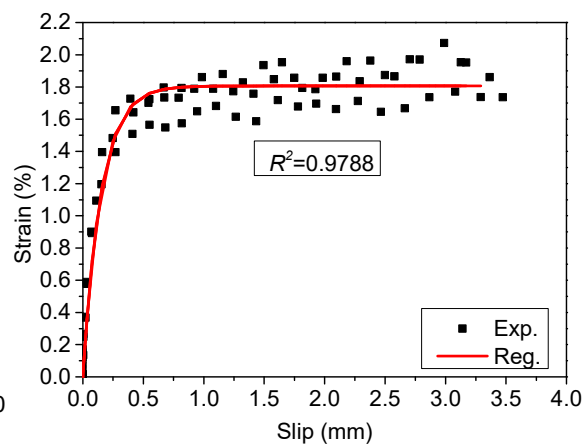
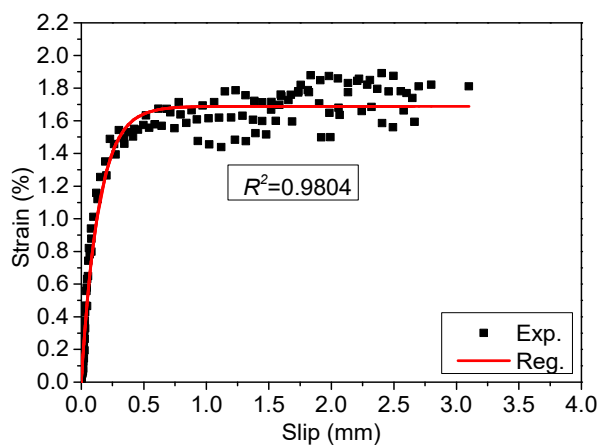


264

265

(c) D2_1MPS_1

(d) D3_3MPS_1



266

267

(e) D4_5MPS_1

(f) D5_8MPS_1

268

Figure 10. Strain-slip curves from the experimental results

269

270

271

272

273

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275

The selected three points measured in these tests had similar strain-slip relationship, and the tested and regressed strain-slip curves show non-linear behaviour because of concrete cracking [44]. Figure 11 illustrates the relationship between bond-slip curve (R) and strain-slip curve (L). After regression analysis of the strain-slip curves, two parts can be obtained including part 1 (red colour) and part 2 (black colour). A nonlinear exponential function can be employed to describe the bond-slip curve due to the cracking of concrete layer during the debonding process [16].

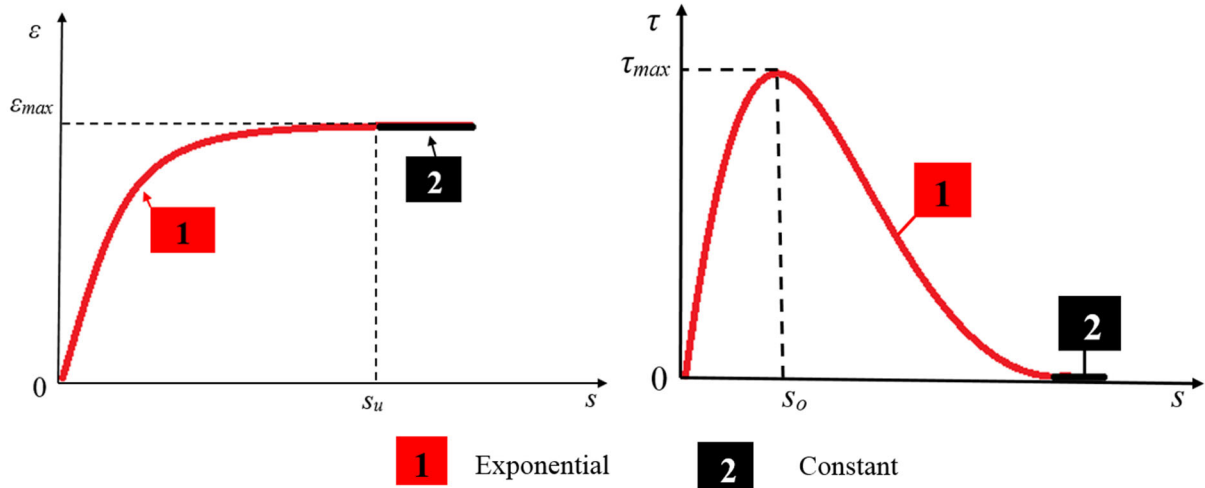


Figure 11. (L) Strain-slip curve; (R) Bond-slip curve

276
277

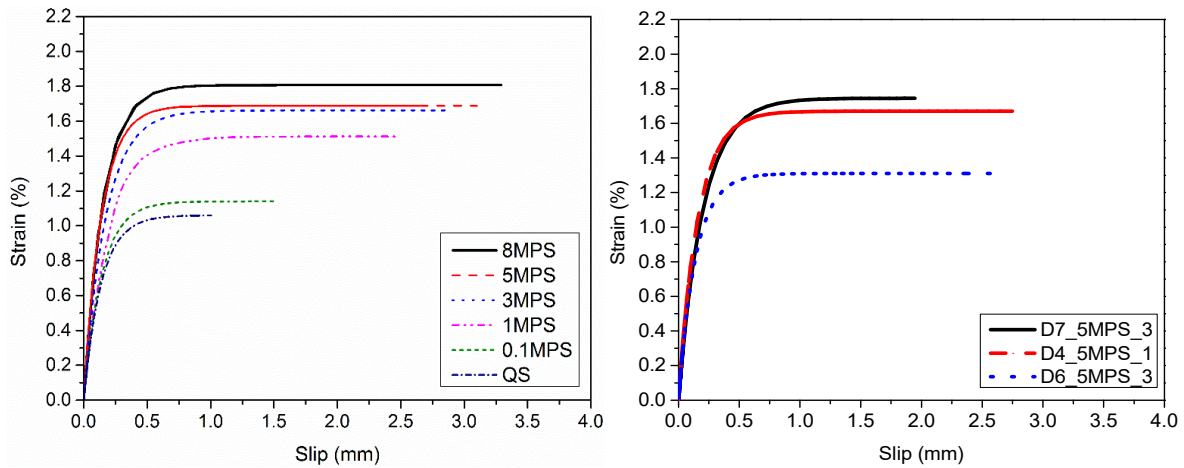
278 The coefficients A and B from regression analysis are listed in **Table 1**. The comparison of the
 279 best-fitted strain-slip curves is plotted in Figure 12 (L). With the rising loading rate, the BFRP
 280 strain and the ultimate slip raised significantly. The average ultimate debonding strains (i.e. A)
 281 of the specimens D1_0.1MPS, D2_1MPS, D3_3MPS, D4_5MPS, and D5_8MPS were 1.099%,
 282 1.459%, 1.658%, 1.683%, and 1.760%, respectively. With the increasing strain rate from
 283 $2.50E-5 \text{ s}^{-1}$ to 4.27 s^{-1} , 29.47 s^{-1} , 51.47 s^{-1} , 103.17 s^{-1} , and 155.10 s^{-1} , the dynamic debonding
 284 strains increased by 15.32%, 53.17%, 74.01%, 76.67%, and 84.12%, respectively, and the
 285 stiffness index B increased by 7.63%, 10.63%, 17.81%, 28.07%, and 30.99%, respectively. For
 286 the specimens subjected to dynamic loadings, a slight change in the initial interface stiffness
 287 can be observed in Figure 12. The improved initial stiffness indicates that the effect of strain
 288 rate on the interface was significant. The improved interfacial stiffness should be affected by
 289 the stiffness of concrete layer, the adhesive layer, and the FRP layer. Additionally, the bonding
 290 width of BFRP sheets has a limited effect on the interfacial stiffness except for the ultimate
 291 debonding strain under dynamic loading of 5 m/s by changing the BFRP width from 25 mm to
 292 40 mm, as given in **Table 1** and as shown in Figure 12 (R). By increasing the BFRP layers
 293 from 2 to 4, the interfacial stiffness is slightly improved due to the increased average value of
 294 B but the ultimate debonding strain drops significantly in the tests. This indicates that the

295 increased BFRP stiffness ($E_f t_f$) enhances the shear resistance of the BFRP-to-concrete interface
296 under dynamic loading, which is consistent with the results under static loading as reported by
297 Subramaniam et al. [45]. The interfacial stiffness K can be expressed as follows [46]:

$$298 \quad K = \frac{1}{\frac{t_c}{G_c} + \frac{t_a}{G_a} + \frac{t_s}{G_s}} \quad (3)$$

$$299 \quad G_i = \frac{E_i}{2(1+\nu_i)} \quad (4)$$

300 where G_c , G_a , and G_s are the shear modulus of concrete, adhesive, and FRP layer, respectively;
301 t_c , t_a , and t_s are the thickness of the concrete, adhesive, and FRP layer, respectively; G_i is the
302 shear modulus; and ν_i is Poisson's ratio [47]. The interfacial stiffness improved significantly
303 because Young's modulus of concrete is strain rate dependent [30, 48, 49]. Hao and Hao [49]
304 proposed equations to define the strain rate effect on the Young's modulus of concrete. Chen
305 et al. [50] proposed equations to describe the relation between strain rate and elastic modulus
306 of BFRP sheets. Liao et al. [48] demonstrated the effect of strain rate on the tensile strength of
307 epoxy. The interfacial stiffness K increased with the increase in G_c , G_a , and G_s according to
308 Equations (3) and (4). It should be noted that the thickness of the concrete, adhesive, and FRP
309 were assumed as a constant in this study.



310

311

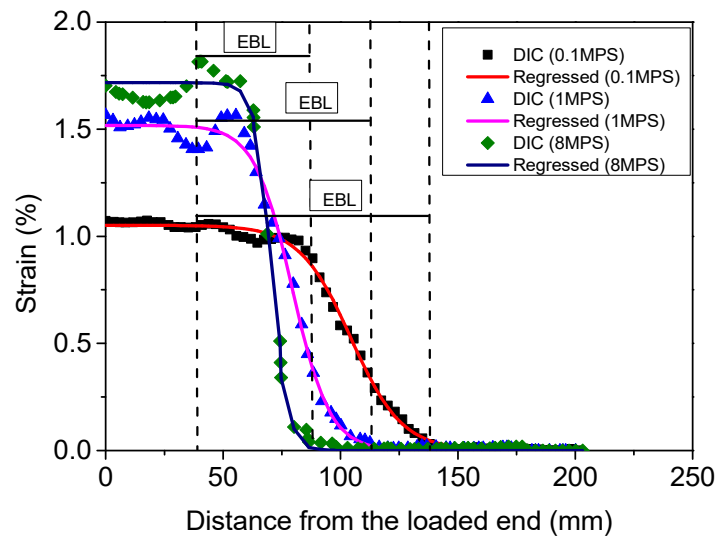
Figure 12. Strain-slip curves for the specimens under different loading speeds

312 3.5 Strain profile and effective bond length

313 EBL is the distance of stress transfer zone along which most of the bond shear stress is
 314 transmitted into the concrete [51]. Three regions can be observed in the measured strain
 315 distribution: (1) fully debonded stage near the loaded end; (2) bond shear stress transferring
 316 stage; and (3) unstressed stage near the free end. In addition, EBL can be obtained through the
 317 strain distribution derived from the DIC technique [35].

318 As shown in Figure 13, successive digital images were prepared and analyzed using DIC and
 319 the longitudinal strain profile at each loading level was obtained. The averaged EBL at 8 m/s
 320 was 47.7 mm which is lower than 91 mm at 0.1 m/s. This indicates that the EBL decreased
 321 with the raising strain rate, which is evident with the steeper strain distribution gradient in
 322 Figure 13. The steeper strain distribution gradient indicates the shorter distance of the shear
 323 stress transferring zone. **Table 1** gives the EBLs for all the tested specimens. The averaged
 324 EBLs for specimens QS, D1_0.1MPS, D2_1MPS, D3_3MPS, D4_5MPS, and D5_8MPS are
 325 92.5 mm, 91 mm, 66.3 mm, 63.3 mm, 51 mm, and 47.7mm, respectively. As the strain rate
 326 raised from $2.59E-5 \text{ s}^{-1}$ to 4.27 s^{-1} , 29.47 s^{-1} , 51.47 s^{-1} , 103.17 s^{-1} , and 155.10 s^{-1} , the dynamic
 327 EBL decreased by 1.62%, 28.29%, 31.53%, 44.86%, and 48.46%, respectively. In addition,
 328 changing the BFRP sheets from two layers to four layers resulted in the increasing effective

329 bond length under static loadings due to the increased BFRP stiffness ($E_f t_f$). For the specimens
 330 with four layers of BFRP sheets, the EBL decreased with the strain rate, which is the same as
 331 the specimens with two BFRP layers under dynamic loadings. The test results show that the
 332 descent rate after the loading speed of 3 m/s is slow indicating that the strain rate effect has a
 333 certain range of influence on the EBL, which agrees with the conclusions by Shen et al. [32]
 334 and Huo et al. [33].



335
 336 Figure 13. EBL under different loading speeds

337 3.6 Interfacial bond stress-slip relationship

338 The shear stress and the slip can be obtained by imposing the equilibrium condition of FRP
 339 sheets with the infinite length. The shear stress and slip can be obtained by the following
 340 equations:

$$341 \quad \tau = E_f t_f \frac{df(s)}{ds} f(s) \quad (5)$$

342 where $f(s)$ is the function of slip (s).

343
$$\frac{df(s)}{ds} = AB e^{-Bs} \quad (6)$$

344 By substituting Equation (6) into Equation (5), the interfacial bond-slip relationship can be
 345 expressed as a function of A and B as follows [16]:

346
$$\tau = A^2 B E_f t_f (e^{-Bs} - e^{-2Bs}) \quad (7)$$

347 The IFE G_f is defined as follows:

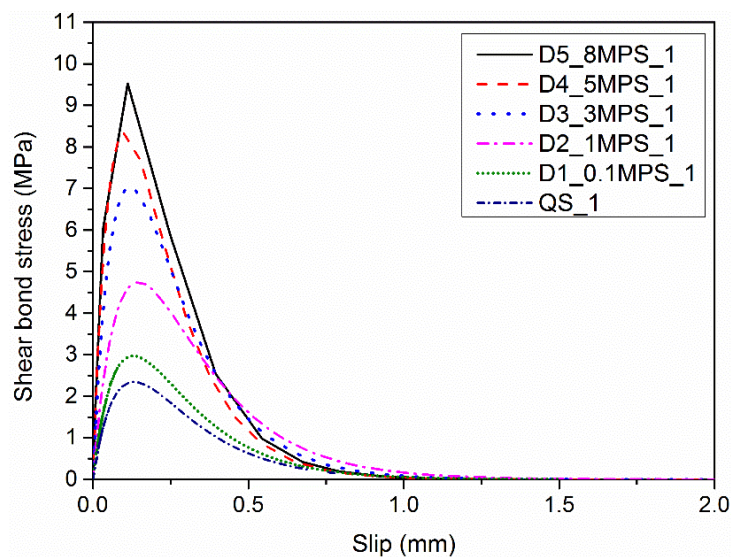
348
$$G_f = \int_0^{\infty} \tau ds \quad (8)$$

349 By substituting Equation (7) into Equation (8), G_f can be yielded:

350
$$G_f = \frac{1}{2} A^2 E_f t_f \quad (9)$$

351 The coefficients A and B can be obtained by fitting the strains-slip curves in section 3.3. Figure
 352 14 shows the fitted interfacial bond stress-slip curves at various loading rates. Table 1 gives
 353 the experimental results of PSS and the corresponding slip. It is obvious that the PSS raised
 354 remarkably with strain rate. The average PSS of specimens D1_0.1MPS, D2_1MPS,
 355 D3_3MPS, D4_5MPS, and D5_8MPS are 2.76 MPa, 5.03 MPa, 7.04 MPa, 8.32 MPa, and 9.47
 356 MPa, respectively. It can be observed that the IFE increases with the strain rate as well, which
 357 is defined as the enclosed area of bond-slip curve. The average IFE of specimens of
 358 D1_0.1MPS, D2_1MPS, D3_3MPS, D4_5MPS, and D5_8MPS are 1.05 N/mm, 1.86 N/mm,
 359 2.40 N/mm, 2.48 N/mm, and 2.73 N/mm, respectively. The reason for the increment of the IFE
 360 is because the shear modulus of concrete, adhesive and FRP increased with the strain rate and
 361 the interfacial stiffness K increases with the shear modulus according to Equations (2) and (3).
 362 The increase of PSS is mainly due to the increment of IFE.

363 To verify the dynamic interfacial shear stress of the BFRP-to-concrete interface, the dynamic
 364 tensile strength of concrete corresponding to the strain rate was estimated to compare with the
 365 interfacial shear stress because of stripping of the concrete layers. There was no normal stress
 366 applied in the single-lap shear test, shear stress penetrated into the concrete with a 45° angle
 367 and consequently the debonding always initiated on the tensile side of concrete substrate. The
 368 dynamic increase factor (DIF) of the concrete was employed herein to obtain the dynamic
 369 tensile strength of the concrete substrates ($f_{t,DIF}$) [52], as summarized in Table 1. It can be
 370 observed that the estimated dynamic tensile strength of the concrete substrates is close to the
 371 interfacial shear stress of the BFRP-to-concrete interfaces, indicating that the obtained PSS is
 372 reasonable and consistent with the tensile strength increment of concrete material with strain
 373 rate.



374
 375 Figure 14. Fitted bond-slip curves under different loading speeds

376 4 Theoretical predictions and proposed models

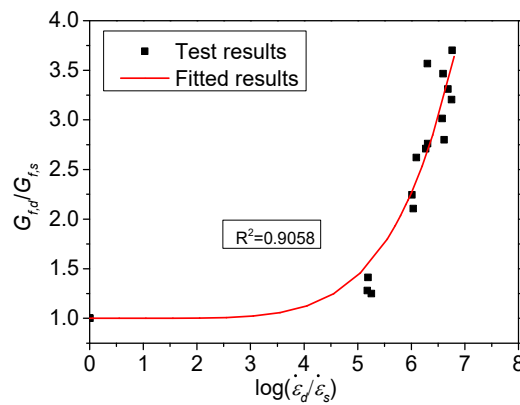
377 4.1 Effect of strain rate on IFE

378 Figure 15 shows the relationship of the IFE against strain rate. As the IFE increases with the
 379 strain rate, the relationship between $G_{f,d}$ and $G_{f,s}$ can be established by incorporating strain rate

380 effect. Yen and Caiazzo [53] proposed logarithmic functions to define the strain rate effects on
 381 the mechanical properties of composites. Shen et al. [54] also used logarithmic functions to
 382 describe the relationship between strain rate and bond properties of BFRP-to-concrete interface.
 383 Thus, the non-linear logarithmic function is employed herein to describe the impact of strain
 384 rate on the interfacial bond properties. After regression analysis, empirical equations
 385 incorporating strain rate effect are given below:

$$386 \quad \frac{G_{f,d}}{G_{f,s}} = 1 + 3.354 \times 10^{-5} \left(\log\left(\frac{\dot{\epsilon}_d}{\dot{\epsilon}_s}\right) \right)^{5.881} \quad \text{when } 2.5 \times 10^{-5} \leq \dot{\epsilon} \leq 155.10 \quad (10)$$

387 where $G_{f,d}$ and $G_{f,s}$ refer to the dynamic and static interfacial fracture energy, respectively; $\dot{\epsilon}_d$
 388 and $\dot{\epsilon}_s$ refer to the dynamic and static strain rate, respectively.



389
 390 Figure 15. Relationship between IFE and strain rate

391 Dai et al. [16] proposed an equation to predict the $G_{f,s}$ considering the concrete compressive
 392 strength (f_c'), FRP stiffness ($E_f t_f$), and interfacial stiffness (G_a/t_a). As the shear modulus of
 393 concrete, adhesive, and BFRP (i.e. G_c , G_a and G_F) together determine the interfacial stiffness,
 394 these factors (i.e. G_c , G_a and G_F) are incorporated into the interfacial stiffness (K) and
 395 consequently the static interfacial fracture energy ($G_{f,s}$). Then the effect of strain rate is
 396 incorporated into the proposed static model to obtain the dynamic interfacial fracture energy.
 397 The proposed model is given below:

398 $G_{f,s} = \varphi (E_f t_f)^\theta K^C$ (11)

399
$$K = \frac{\frac{G_c}{t_c} \frac{G_a}{t_a} \frac{G_F}{t_F}}{\frac{G_c}{t_c} + \frac{G_a}{t_a} + \frac{G_F}{t_F}}$$
 (12)

400 where φ , θ , and C are coefficients determined from the data collection [19]. After regression
 401 analysis according to the testing data, the coefficients are determined, and the static IFE is
 402 given as:

403 $G_{f,s} = 0.345 (E_f t_f)^{0.029} K^{-0.986}$ (13)

404 By substituting Equations (11), (12) and (13) into Equation (10), the dynamic interfacial
 405 fracture energy $G_{f,d}$ can be predicted by incorporating strain rate effect. It should be noted that
 406 the thickness of concrete $t_c = 20$ mm was selected according to [46]. The thickness of concrete
 407 should be 2 or 3 times the aggregate size [55]. E_c was determined by using $E_c = 4700\sqrt{f'_c}$ [56].

408 4.2 Effect of strain rate on bond strength

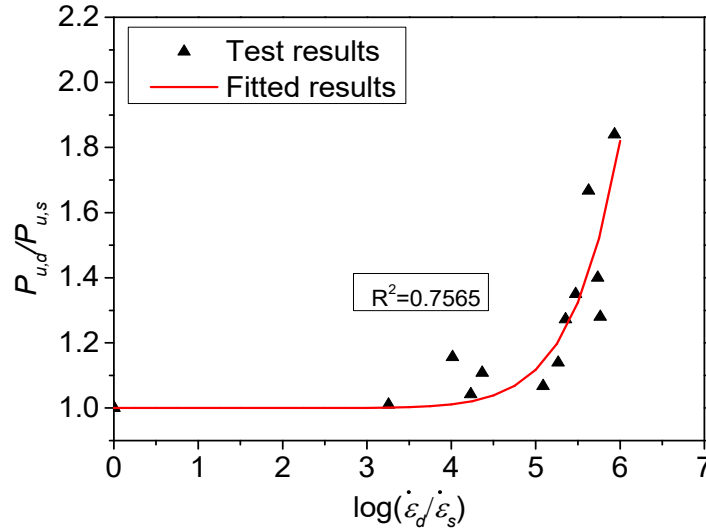
409 Figure 16 shows the relationship of the debonding load P_u against strain rate. As the debonding
 410 load increases with the strain rate, the relation between dynamic and static debonding loads
 411 ($P_{u,d}$ and $P_{u,s}$) can be established by incorporating the effects of strain rate. After regression
 412 analysis, empirical equation incorporating strain rate effect is given below:

413
$$\frac{P_{u,d}}{P_{u,s}} = 1 + 1.444 \times 10^{-10} \left(\log\left(\frac{\dot{\epsilon}_d}{\dot{\epsilon}_s}\right) \right)^{11.74} \quad \text{when } 2.5 \times 10^{-5} \leq \dot{\epsilon} \leq 155.10$$
 (14)

414 The debonding load can be expressed by considering the IFE, which has been widely applied
 415 in estimating the interfacial debonding loads [19, 44, 47]. The $G_{f,s}$ can be expressed by Equation
 416 (13) and the static debonding load ($P_{u,s}$) is given as:

417 $P_{u,s} = b_f \sqrt{2E_f t_f G_{f,s}}$ (15)

418 By substituting Equations (10) and (15) into Equation (14), the dynamic debonding load ($P_{u,d}$)
 419 can be obtained.



420

421

Figure 16. DIF of debonding load

422 **4.3 Effect of strain rate on interfacial shear stress and slip**

423 As discussed in section 3.4, two coefficients (i.e. G_f and B) can be obtained from the fitted
 424 strain-slip relationship. According to the previous model [16], both the IFE and the stiffness
 425 index B determine the bond stress-slip relationship.

426 $\tau = 2BG_f (e^{-Bs} - e^{-2Bs})$ (16)

427 $\tau_{\max} = \frac{1}{2} BG_f$ (17)

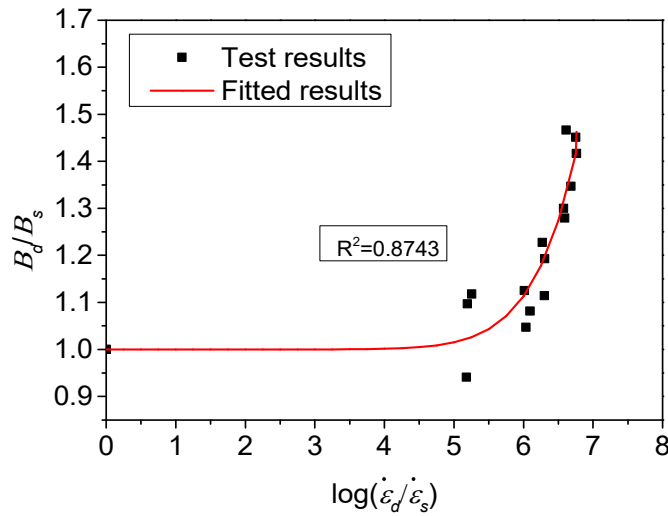
428 $s_{\max} = \frac{\ln 2}{B} = \frac{0.693}{B}$ (18)

429 As the stiffness index B increases with the strain rate, and using the testing results given in
 430 **Table 1**, the dynamic stiffness index B_d by incorporating strain rate can be expressed by
 431 Equation (20). The relationship between the static stiffness index (B_s) and the mechanical

432 properties of FRP, epoxy and concrete can be expressed by Equation (19). After regression
 433 analysis, the stiffness index model is proposed as Equation (20).

$$434 \quad B_s = 5.908 (E_f t_f)^{0.108} K^{0.833} \quad (19)$$

$$435 \quad \frac{B_d}{B_s} = 1 + 2.963 \times 10^{-10} \left(\log\left(\frac{\dot{\varepsilon}_d}{\dot{\varepsilon}_s}\right) \right)^{11.03} \quad \text{when } 2.5 \times 10^{-5} \leq \dot{\varepsilon} \leq 155.10 \quad (20)$$



436
 437 Figure 17. Relationship between stiffness index and strain rate

438 The PSS τ_m and the corresponding slip s_o are two critical factors determining the bond-slip
 439 response. The test results showed that the PSS increased while the corresponding slip decreased
 440 with the rising strain rate. After regression analysis, the τ_m and s_o can be obtained by the
 441 following equations:

$$442 \quad \frac{\tau_{m,d}}{\tau_{m,s}} = 1 + 1.328 \times 10^{-6} \left(\log\left(\frac{\dot{\varepsilon}_d}{\dot{\varepsilon}_s}\right) \right)^{7.795} \quad \text{when } 2.5 \times 10^{-5} \leq \dot{\varepsilon} \leq 155.10 \quad (21)$$

$$443 \quad \frac{s_{o,d}}{s_{o,s}} = 1 - 6.618 \times 10^{-9} \left(\log\left(\frac{\dot{\varepsilon}_d}{\dot{\varepsilon}_s}\right) \right)^{9.226} \quad \text{when } 2.5 \times 10^{-5} \leq \dot{\varepsilon} \leq 155.10 \quad (22)$$

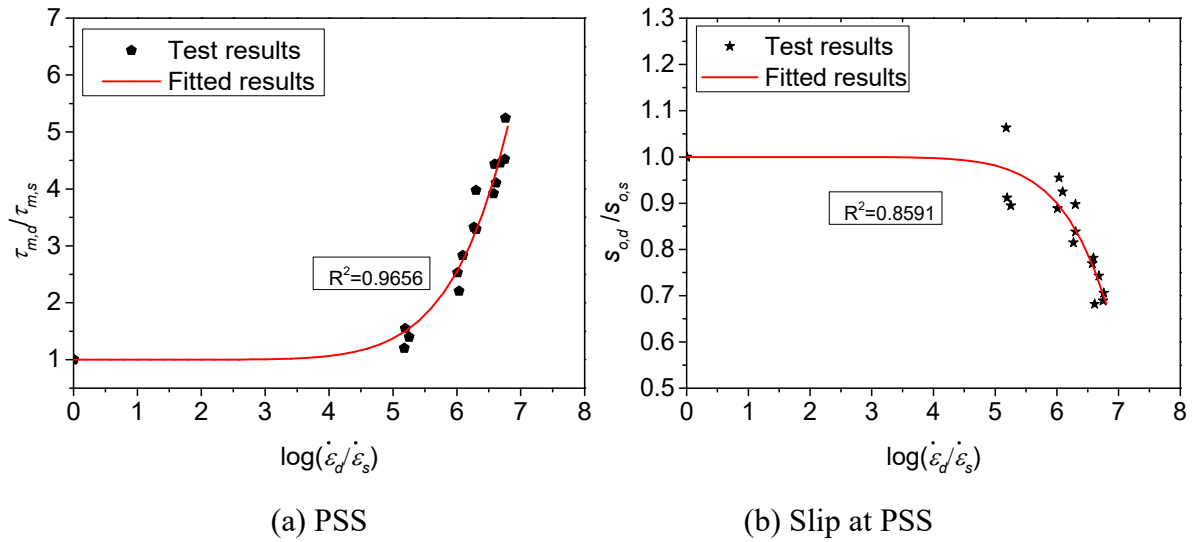


Figure 18. Relationship between (a) peak shear stress vs. strain rate; (b) slip vs. strain rate

447 By substituting Equations (10) and (20) into Equation (17) and substituting Equations (19) and

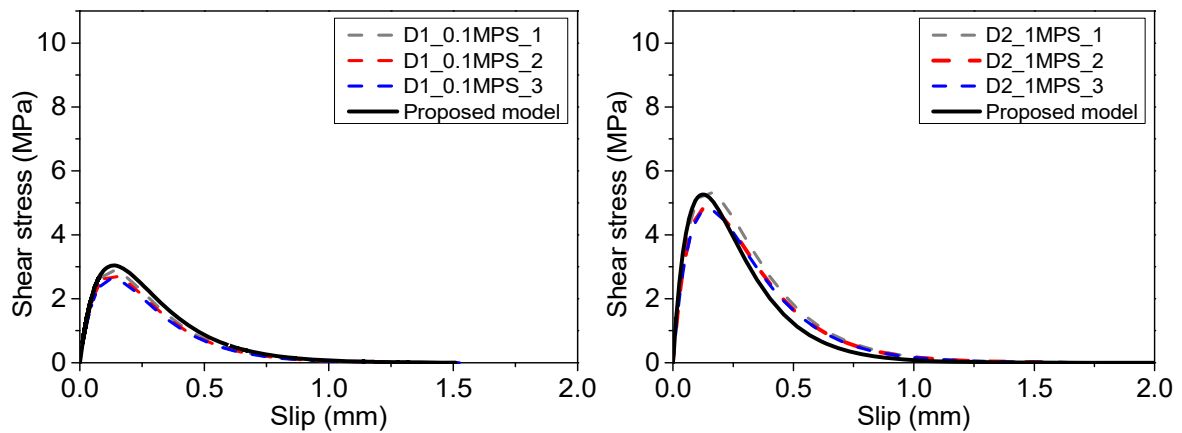
448 (20) into Equation (18), the dynamic PSS $\tau_{m,d}$ and the corresponding slip $s_{o,d}$ can be obtained.

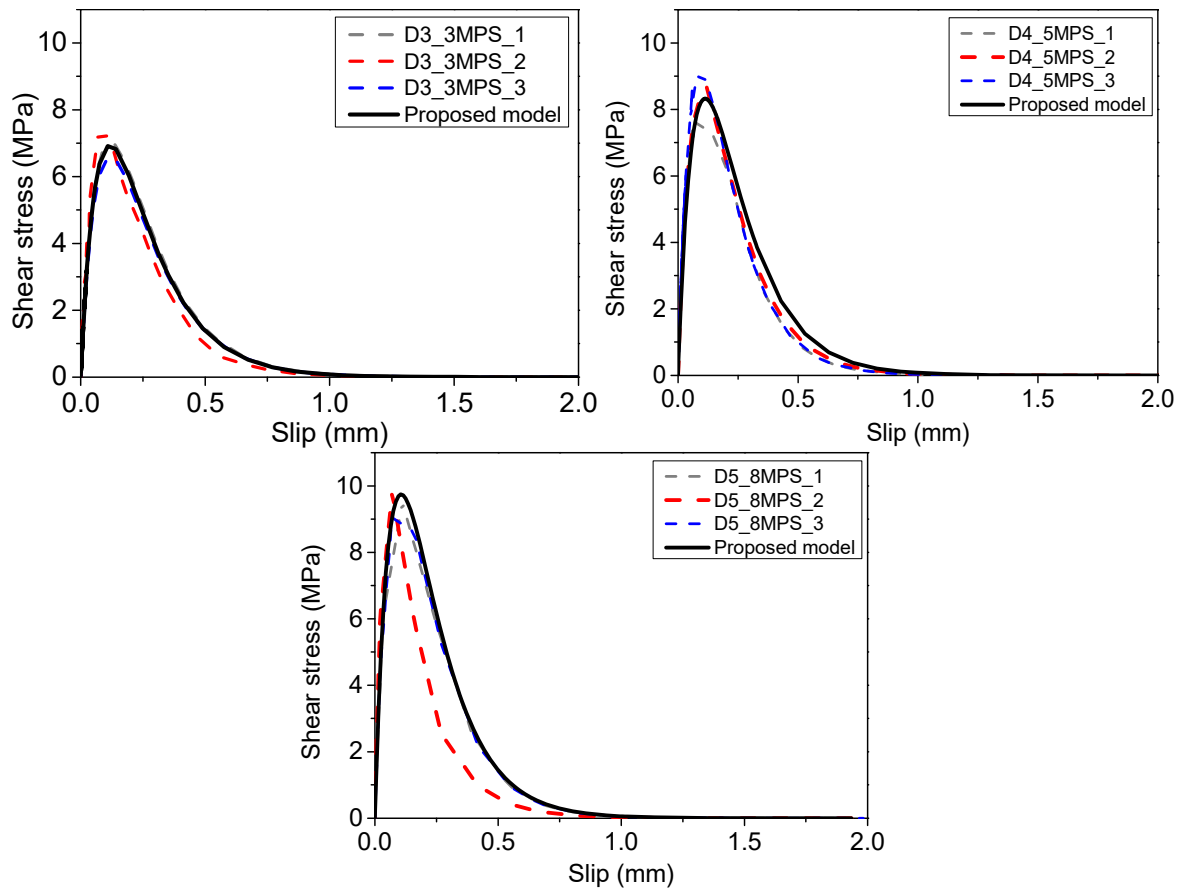
449 Additionally, the dynamic bond-slip relationships can be determined by substituting Equations

450 (10), (17), (18) and (20) into Equation (16). Figure 19 plots the comparison of the predicted

451 and tested bond-slip curves. It should be noted that all the proposed models in this study are

452 applicable for the strain rate ranging between $2.5 \times 10^{-5} \text{ s}^{-1}$ and 155.10 s^{-1} .





454

455

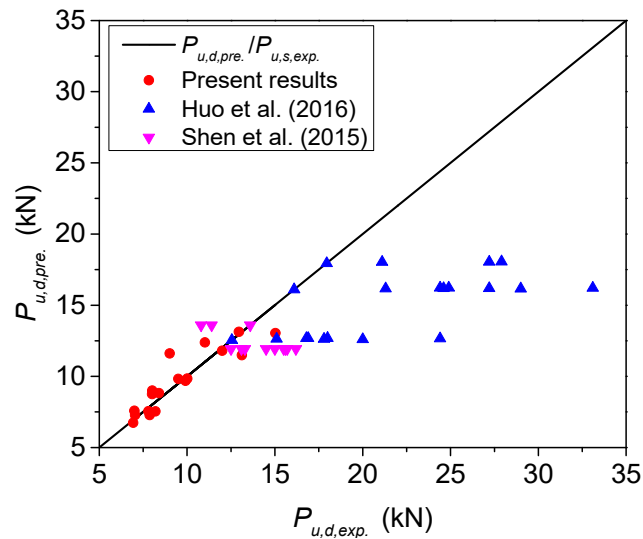
456

Figure 19. Predicted vs. tested bond-slip curves

457 **4.4 Validation of the proposed dynamic models**

458 The proposed dynamic bond-slip model can be used to determine the debonding load, the PSS,
 459 the BFRP strain distribution and the bond-slip curve. Testing results can directly provide the
 460 debonding load and FRP strain distribution. In this section, the present and previous testing
 461 data were collected to compare with the predicted results. As there were limited experimental
 462 studies in the literature regarding the dynamic interfacial bond of FRP-to-concrete interface,
 463 two studies by Huo et al. [33] and Shen et al. [32] are selected to validate the predictions. Figure
 464 20 shows the comparisons of the predicted and tested results. The experimental results from
 465 the present study and the study of Shen et al. [32] match well with the predicted results.
 466 However, the experimental results by Huo et al. [33] is overestimated by the proposed model.
 467 The discrepancies might be due to different testing methods. Huo et al. [33] used the testing
 468 method of three-point impact tests on beams bonded by FRP for dynamic bonding test and

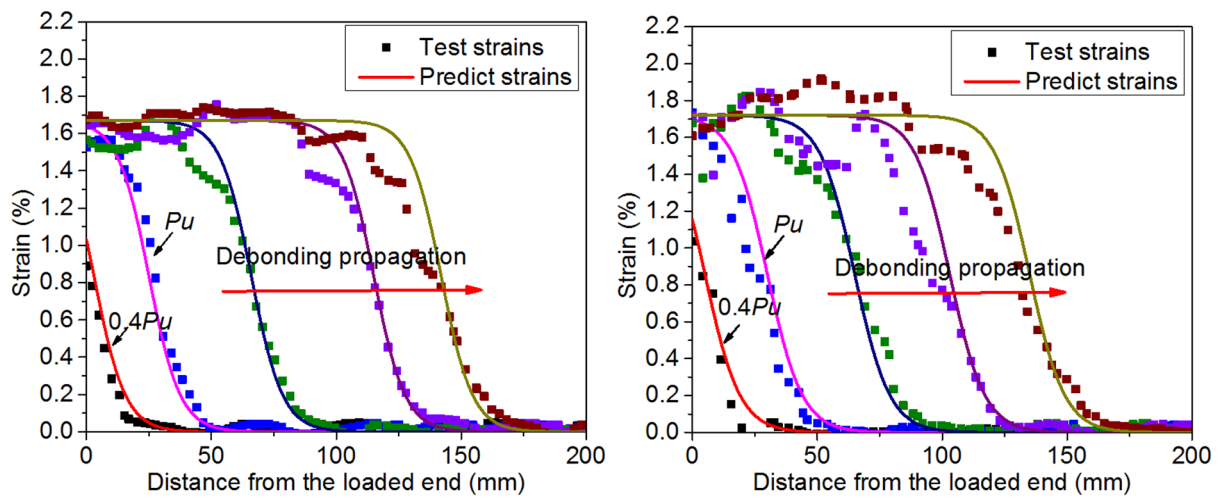
469 consequently the additional bending moment and normal stress complicated the debonding
 470 process. However, Shen et al. [32] employed double-lap shear test method and the present
 471 study used single-lap shear test method to investigate dynamic bonding behaviours.



472
 473 Figure 20. Experimental results vs. predicted results

474 The FRP strain distributions along the bonded length can be obtained by the proposed bond-
 475 slip model based on the studies from Zhou et al. [10] and Yuan et al. [15]. Analytical studies
 476 were carried out by Zhou et al. [10] and Yuan et al. [15] on the full debonding process of FRP-
 477 to-concrete joints, and consequently the strain distributions at various loading levels were
 478 predicted based on the proposed models. Figure 21 illustrates the comparison between the
 479 tested and predicted FRP strain distributions of four specimens. The Specimen D4_5MPS_1
 480 and D5_8MPS_1) are selected from the present study, and it is noted that the BFRP strains
 481 were measured by the DIC method. Other two specimens (i.e. L200-D3-2 and L200-D2-1)
 482 were tested by Shen et al. [32], and the BFRP strains were measured by the strain gauges.
 483 Comparisons show that the predicted strain distributions match well with the tested results at
 484 different dynamic loading stages. The proposed model can properly predict the pre-debonding
 485 stage and post-debonding stage, and the predicted strain profile remained the same shape to

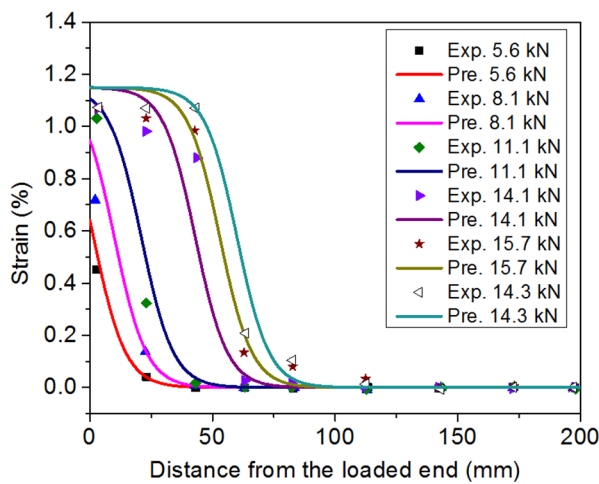
486 propagate the debonding process. The experimental strain distributions of Huo et al. [33] were
 487 not compared herein due to different testing method and different FRP materials.



488

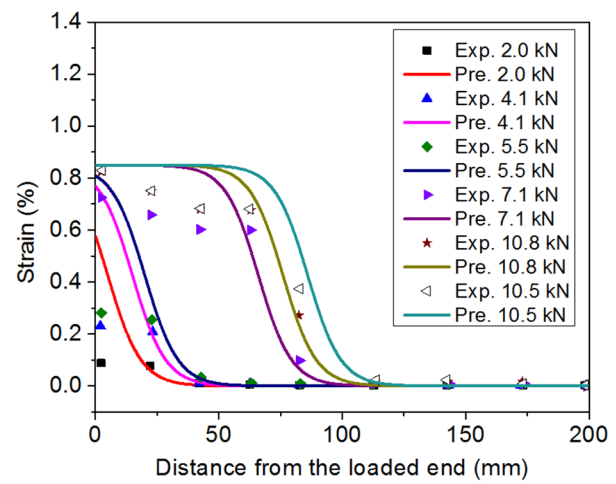
489 (a) Specimen D4_5MPS_1 (present study)

(b) Specimen D5_8MPS_1 (present study)



490

491 (c) Specimen L200-D3-2 (Shen et al. 2015)



492 (d) Specimen L200-D2-1 (Shen et al. 2015)

Figure 21. Comparison between the tested and predicted strain distributions

493 5 Conclusions

494 This study experimentally investigates the strain rate effect on the failure modes, strain
 495 distributions, interfacial fracture energy, strain-slip response, debonding load, and bond-slip
 496 response by implementing SST. The following conclusions can be drawn:

- 497 (1) Strain rate changed the failure modes of the BFRP-to-concrete interface. Two debonding
 498 failure modes of the BFRP-to-concrete interface under dynamic loadings can be observed,

499 i.e. debonding in concrete failure (C) and debonding in the interface of concrete-epoxy
500 (CE).

501 (2) The single-lap shear specimens under dynamic loadings exhibited more ductile behaviour
502 due to the increased ultimate slip. The shear slip increased by 13.89%, 32.61%, 34.97%,
503 52.06%, and 58.48% with the rising strain rate from $2.5 \times 10^{-5} \text{ s}^{-1}$ to 4.27 s^{-1} , 29.47 s^{-1} , 51.47
504 s^{-1} , 103.17 s^{-1} , and 155.10 s^{-1} , respectively. The increased slippages at the interface
505 improved the interfacial fracture energy and consequently the bond strength of the interface.

506 (3) The strain distributions in BFRP sheets were significantly affected by the dynamic loadings.
507 The strain distribution gradient in the BFRP sheets under higher loading speeds was steeper
508 than those obtained with lower loading speed. By changing the BFRP sheets from two
509 layers to four layers, the debonding strain of BFRP sheets reduced due to the increased FRP
510 thickness. Reducing the bonding width of BFRP sheets from 40 mm to 25 mm had little
511 effect on the interfacial stiffness while the ultimate debonding strain increased under
512 dynamic loadings.

513 (4) The dynamic effective bond length (EBL) decreased with the increasing strain rate, but the
514 effect of strain rate on the EBL became less prominent when subjected to relatively higher
515 loading rate, such as 5 m/s and 8 m/s.

516 (5) By comparing the predicted results with the testing data, the validated proposed dynamic
517 bond-slip model by incorporating the strain rate can accurately predict the dynamic bond
518 behaviour of BFRP-to-concrete interface.

519 **Acknowledgements**

520 The authors thank Australian Research Council Linkage Project (ARC LP150100259) for
521 the financial support.

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