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# 1 Strain Rate Effect on Interfacial Bond Behaviour between BFRP Sheets 2 and Steel Fibre Reinforced Concrete

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## 9 Abstract

10 Numerous studies have shown that using steel fibre reinforced concrete (SFRC) and  
11 retrofitting with Fibre-reinforced polymer (FRP) composites can improve the strength and  
12 ductility of RC structures against impact and explosive loadings. The interface between FRP  
13 and concrete has been identified as one of the weakest parts of the FRP strengthened  
14 structures subjected to dynamic loading, with debonding failure usually observed as the  
15 primary failure mode. In order to properly analysis and design of FRP strengthened  
16 reinforced concrete (RC) structures, it is important to understand the dynamic bonding  
17 strength between FRP and concrete. An experimental investigation regarding to the dynamic  
18 interfacial bond behaviour between basalt fibre (BFRP) sheets and SFRC is carried out in this  
19 study. Concrete prisms were made of short steel fibres with three volumetric fractions (i.e.  $V_f$   
20 = 0.5%, 1.0%, and 1.5%) to improve the tensile strengths. To achieve different strain rates,  
21 the loading velocities varied from 8.33E-6 m/s, 0.1 m/s, 1 m/s, 3 m/s, to 8 m/s. Experimental  
22 results show the bond strength and bond-slip were sensitive to strain rate. The loading rate  
23 changed the debonding failure modes from concrete substrate failure to interfacial debonding.  
24 In addition, the shear resistance of the interface increased with the fibre volume under both  
25 quasi-static and dynamic loadings. Based on the testing data, an empirical bond-slip model,

26 incorporating the volumetric fraction of steel fibre and strain rate, is established for FRP-  
27 strengthened SFRC structures.

28 **Keywords:** Dynamic loading; Strain rate; BFRP; SFRC; Interfacial bond behaviour.

## 29 **1. Introduction**

30 Using steel fibre reinforced concrete (SFRC) and fibre-reinforced polymer (FRP) is effective  
31 to improve the strength and ductility of reinforced concrete (RC) members. As reported by  
32 Mutalib and Hao [1], FRP strengthening is effective in enhancing RC slab's capacity to resist  
33 blast loads. Saatcioglu et al. [2] experimentally and numerically examined the responses of  
34 FRP-strengthened RC members and found that FRP strengthening was effective in enhancing  
35 blast resistance. Field blast tests on RC slabs and SFRC panels were conducted by Lan et al.  
36 [3] and found that adding fibres in concrete mix improved the damage resistance. Lee et al. [4]  
37 conducted blast tests on blast-damaged specimens retrofitted with steel fibres reinforced  
38 cementitious composite (SFRCC) as well as CFRP sheets and reported that the addition of  
39 steel fibres resulted in improved ductility and enhanced blast resistance. For the CFRP-  
40 strengthened specimens, the flexural capacity and ductility were enhanced and the debonding  
41 failure of CFRP was observed.

42 FRP debonding is a premature failure mode for FRP-strengthened RC structures when subject  
43 to different loading conditions [5-8]. Normally only 30% - 40% of FRP strength could be  
44 utilized due to the premature debonding failure. The FRP debonding cannot be easily  
45 prevented due to the localized cracks of concrete [9-11]. Steel fibres can be used to improve  
46 the interfacial bond behaviour since the addition of steel fibres can improve the cracking  
47 resistance. Compared with plain concrete, SFRC shows better ductility due to its enhanced  
48 tensile strength. Additionally, the mechanical properties of concrete were significantly  
49 influenced by the volume fraction and aspect ratio of fibres. [12, 13]. Due to the advantages

50 of SFRC and FRP, numerous studies investigated the FRP-strengthened fibres reinforced  
51 concrete (FRC) structures [14-17]. Experimental studies conducted by Li et al. [14] found  
52 that hybrid FRP-strengthened FRC beams with 0.9% short steel fibres and 0.1% polymer  
53 fibres yielded higher bending stiffness and crack resistance. GFRP debonding induced by the  
54 flexural cracks was observed in their tests. Experimental and numerical studies conducted by  
55 Yin and Wu [15] found that FRP-strengthened SFRC beams with four steel fibre volumetric  
56 fractions (i.e. 0, 0.25%, 0.5%, and 1%) exhibited a higher load bearing capacity, higher  
57 concrete toughness, and greater fracture energy. By conducting numerical studies o,  
58 Benvenuti and Orlando [18] found that the flexural capacity was significantly improved and  
59 the ductility of the post-peak branch was remarkably enhanced for FRP-strengthened SFRC  
60 beams. Gribniak et al. [17] reported that the ultimate deformation increased by 20% for FRP-  
61 strengthened SFRC beams ass compared to the control specimen.

62 FRC has been widely utilized to repair damaged RC elements while FRP composites have  
63 been used to strengthen defective structures. The efficiency of strengthening is primarily  
64 determined by the bonding performance. As FRP debonding has been observed in many tests,  
65 e.g., the field blast tests conducted by Lee et al. [4], it is necessary to quantitatively study  
66 dynamic interfacial bond behaviour between FRP and FRC at different strain rates. So far,  
67 very limited studies have been conducted to investigate the strain rate effect on the interfacial  
68 bond behaviour between FRP and concrete, and all these studies are limited to relatively low  
69 strain rates with the highest strain rate reached being around  $4.9 \text{ s}^{-1}$  [19-21]. This low strain  
70 rate does not necessarily reflect the true dynamic behaviour of FRP-retrofitted structures  
71 under high strain rates generated by high-speed impact and blast load, under which the strain  
72 rate of structural response can reach approximately up to a few hundred per second [22]. In  
73 addition, the study on the interfacial bond behaviour between FRP and SFRC is very limited.  
74 Yuan et al. [23] experimentally investigated the interfacial bond of BFRP-to-SFRC joint and

75 the found that the bond-slip relationship was sensitive to steel fibre volume under quasi-static  
 76 loading. However, studies of dynamic bonding behaviours between FRP and SFRC have not  
 77 been available in the literature yet.

78 To better understand the effect of steel fibre on the dynamic interfacial bond behaviour  
 79 between FRP and SFRC, different fibre volumetric fractions have been considered in the  
 80 experimental program. To achieve high strain rate, single-lap shear tests with various loading  
 81 speeds up to 8 m/s were carried out. Experimental results including strain distribution, bond  
 82 strength, and bond-slip response are presented and discussed in this paper. An empirical  
 83 dynamic bond-slip model incorporating the fibre volume and the strain rate is proposed and  
 84 validated.

## 85 2. Experimental program

### 86 2.1 Material properties

87 Concrete prisms with dimension of 150 x 150 x 300 mm were prepared for single-lap shear  
 88 tests. The 28-day mechanical properties of concrete including compressive and tensile  
 89 strengths are given in Table 1. Four volumetric fractions of steel fibres (i.e. 0%, 0.5%, 1.0%  
 90 and 1.5%) were used for the concrete with the design grade of 30 MPa. The short steel fibres  
 91 with the fibre-reinforcing index ( $V_f L_f / \phi_f$ ) in the range of 0 to 1.25 were used in the  
 92 experimental program. The Young's modulus, tensile strength, and density of steel fibres  
 93 provided by the supplier are 200 GPa, 2.5 GPa, and 7,800 kg/m<sup>3</sup>, respectively.

94 **Table 1.** Mechanical properties of SFRC

Specimen ID	Volume fraction $V_f$ (%)	Fibre-reinforcing index ( $V_f L_f / \phi_f$ )	Compressive strength $f'_c$ (MPa)	Splitting tensile strength $f'_t$ (MPa)
PC-1	0	0	29.48	2.71
PC-2			30.18	2.98
PC-3			28.74	2.86
Mean			29.47	2.85



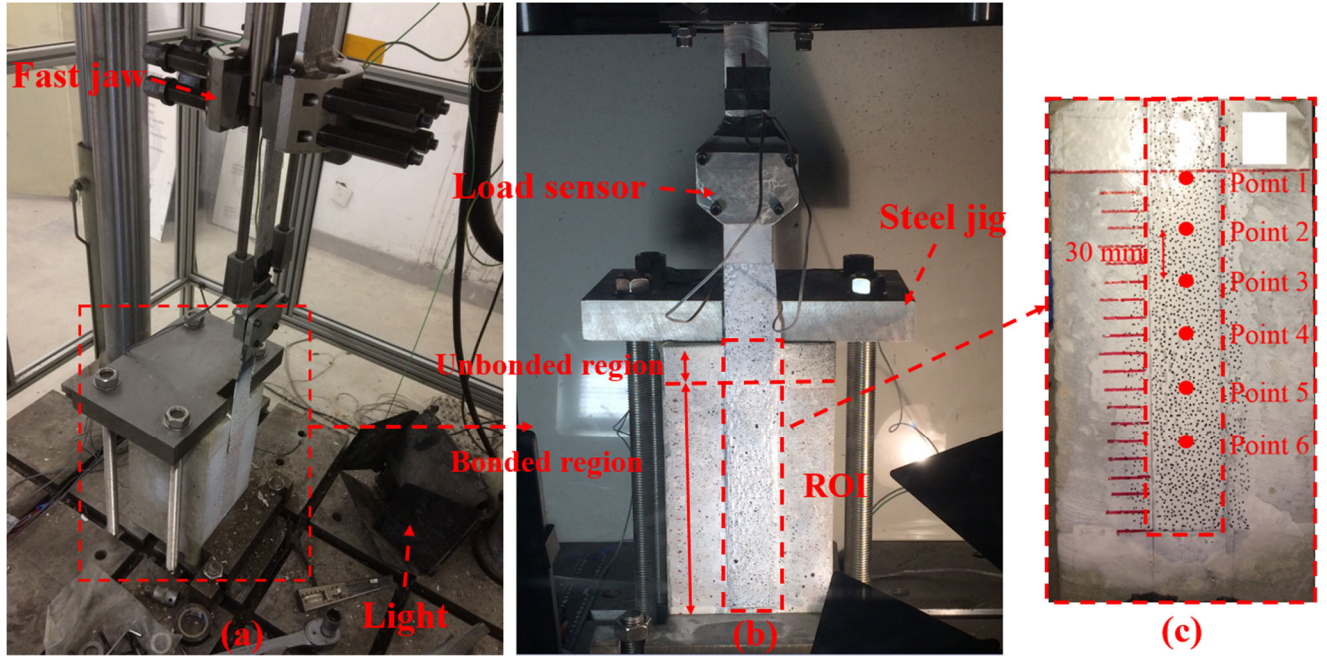
			(COV=0.02)	(COV=0.05)
SFRC-0.5-1			31.33	2.97
SFRC-0.5-2	0.50	0.417	33.05	3.16
SFRC-0.5-3			32.90	3.21
Mean			32.43	3.11
			(COV=0.03)	(COV=0.04)
SFRC-1.0-1			32.59	3.33
SFRC-1.0-2	1.00	0.833	34.09	3.58
SFRC-1.0-3			33.48	3.41
Mean			33.39	3.44
			(COV=0.02)	(COV=0.04)
SFRC-1.5-1			33.72	3.93
SFRC-1.5-2	1.50	1.250	34.24	3.86
SFRC-1.5-3			32.39	3.57
Mean			33.45	3.79
			(COV=0.03)	(COV=0.05)

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96 In this study, unidirectional BFRP sheets with an area density of 300 g/m<sup>2</sup> were prepared in  
97 this study. The tested rupture tensile strength, elastic modulus, and failure strain of the BFRP  
98 sheets were 1,333 MPa, 73 GPa, and 0.12%, respectively. The adhesive used to saturate the  
99 BFRP sheets was two-component epoxy resins at a ratio of 5:1. The ultimate tensile strength,  
100 elastic modulus, and rupture strain of the adhesive provided by the supplier were 50.5 MPa,  
101 2.8 GPa, and 4.5%, respectively [24].

## 102 2.2 Test matrix

103 Dynamic single-lap shear tests were carried out using an INSTRON<sup>®</sup> VHS 160-20 high speed  
104 servo hydraulic testing machine, as shown in Figure 1 (a). This machine can provide a  
105 constant loading velocity at the range of 0.1 m/s to 25 m/s. The fast jaw of this machine  
106 speeds up to a desired loading velocity and firmly grab the specimen then hold it at the  
107 desired velocity until the final debonding of the BFRP-to-concrete joints. A steel jig was  
108 designed to hold the concrete prisms in place to prevent the out-of-plane movement. As  
109 shown in Figure 1 (b), the bond length and width of BFRP sheets of all the specimens were  
110 200 mm and 40 mm, respectively. To prevent the edge effect of the concrete prisms, 50 mm  
111 unbonded region prior to the loaded end was reserved, as shown in Figure 1 (b).



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113 Note: *ROI* is the region of interest

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Figure 1. (a) Test setup; (b) Specimen detail; and (c) Tracking points

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A total of 56 single-lap shear specimens were prepared for this study. The GOM Correlate<sup>®</sup> 2D-DIC software was used in this study to conduct the DIC analysis. The successive digital images during testing were recorded first by using a high-speed camera and then processed in the DIC software to obtain the displacement and strain values. Six points were selected as the tracking points to determine the dynamic stress equilibrium and bond-slip curves, as shown in Figure 1 (c). Table 2 presents the specimen details and experimental results of the static and dynamic tests. The single-lap shear specimen ID was named as “*QSX-n*” and “*DX-m-n*”. “*QSX* or *DX*” refers to the quasi-static (QS) or dynamic (D) single-lap shear tests with steel fibre volumetric fraction of  $X\%$ . The letter “*m*” stands for the dynamic loading velocity. The letter “*n*” means the specimen number.

125 **Table 2.** Specimen details and experimental results

Specimen ID	Volume fraction $V_f(\%)$	$RI$ ( $V_f L_f / \phi_f$ )	Loading velocity (m/s)	Strain rate ( $s^{-1}$ )	$P_u$ (kN)	$\epsilon_m$ (%)	$\tau_m$ (MPa)	$s_o$ (mm)	$G_f$ (N/mm)	Failure mode
QS0-1	0	0	8.33E-6	2.50E-05	7.87	1.10	2.2	0.131	1.10	C
QS0-2	0	0	8.33E-6	2.50E-05	6.93	0.99	2.11	0.146	0.86	C
QS0.5-1	0.5	0.417	8.33E-6	2.50E-05	8.09	1.09	2.79	0.138	1.17	C

QS0.5-2	0.5	0.417	8.33E-6	2.50E-05	8.11	1.12	2.57	0.145	1.17	C
QS1-1	1.0	0.833	8.33E-6	2.50E-05	8.12	1.14	2.68	0.143	1.18	C
QS1-2	1.0	0.833	8.33E-6	2.50E-05	8.36	1.17	3.02	0.137	1.25	C
QS1.5-1	1.5	1.250	8.33E-6	2.50E-05	8.26	1.17	3.05	0.139	1.22	C
QS1.5-2	1.5	1.250	8.33E-6	2.50E-05	9.19	1.19	3.45	0.147	1.51	C
D0-0.1-1	0	0	0.1	4.51	8.07	1.18	3.25	0.13	1.16	C
D0-0.1-2	0	0	0.1	4.31	7.88	1.09	2.95	0.141	1.11	C
D0-0.1-3	0	0	0.1	4.21	7.67	1.08	2.68	0.135	1.05	C
D0-1-1	0	0	1.0	25.9	8.34	1.45	4.81	0.132	1.24	C
D0-1-2	0	0	1.0	-	-	-	-	-	-	-
D0-1-3	0	0	1.0	29.56	9.72	1.48	4.2	0.128	1.69	C
D0-3-1	0	0	3.0	65.12	10.51	1.65	5.34	0.124	1.97	C
D0-3-2	0	0	3.0	-	-	-	-	-	-	-
D0-3-3	0	0	3.0	60.75	11.18	1.69	6.31	0.121	2.23	C/CE
D0-8-1	0	0	8.0	173.55	12.01	1.82	9.44	0.107	2.57	C/CE
D0-8-2	0	0	8.0	155.55	11.89	1.78	9.05	0.098	2.52	C/CE
D0-8-3	0	0	8.0	150.75	13.5	1.83	9.82	0.112	3.25	C/CE
D0.5-0.1-1	0.5	0.417	0.1	2.11	9.14	1.44	4.67	0.135	1.49	C
D0.5-0.1-2	0.5	0.417	0.1	2.52	8.79	1.27	4.07	0.112	1.38	C
D0.5-0.1-3	0.5	0.417	0.1	1.62	8.34	1.20	4.16	0.153	1.24	C
D0.5-1-1	0.5	0.417	1.0	13.83	8.91	1.49	4.58	0.172	1.42	C
D0.5-1-2	0.5	0.417	1.0	16.06	9.53	1.51	5.73	0.111	1.62	C
D0.5-1-3	0.5	0.417	1.0	-	-	-	-	-	-	-
D0.5-3-1	0.5	0.417	3.0	76.55	11.34	1.70	7.75	0.167	2.29	C/CE
D0.5-3-2	0.5	0.417	3.0	64.93	10.42	1.71	8.49	0.166	1.94	C
D0.5-3-3	0.5	0.417	3.0	68.81	11.89	1.69	8.14	0.126	2.52	C/CE
D0.5-8-1	0.5	0.417	8.0	134.91	12.13	1.80	9.95	0.139	2.62	C/CE
D0.5-8-2	0.5	0.417	8.0	131.73	12.41	1.84	8.97	0.144	2.75	C/CE
D0.5-8-3	0.5	0.417	8.0	148.87	12.53	1.93	9.77	0.135	2.80	C/CE
D1-0.1-1	1.0	0.833	0.1	2.75	9.9	1.35	6.72	0.138	1.75	C
D1-0.1-2	1.0	0.833	0.1	2.07	9.12	1.34	5.47	0.129	1.48	C
D1-0.1-3	1.0	0.833	0.1	4.17	8.07	1.29	4.65	0.124	1.16	C
D1-1-1	1.0	0.833	1.0	28.09	9.32	1.46	6.35	0.125	1.55	C
D1-1-2	1.0	0.833	1.0	15.38	9.61	1.51	6.69	0.14	1.65	C
D1-1-3	1.0	0.833	1.0	27.93	9.87	1.53	7.23	0.146	1.74	C
D1-3-1	1.0	0.833	3.0	41.8	9.89	1.70	9.14	0.112	1.74	C
D1-3-2	1.0	0.833	3.0	43.95	12.25	1.72	8.16	0.126	2.68	C/CE
D1-3-3	1.0	0.833	3.0	61.49	11.69	1.71	8.84	0.13	2.44	C
D1-8-1	1.0	0.833	8.0	164.12	12.43	1.79	8.79	0.107	2.76	C/CE
D1-8-2	1.0	0.833	8.0	130.13	13.39	1.87	8.58	0.112	3.20	C/CE
D1-8-3	1.0	0.833	8.0	137.74	12.66	1.78	9.12	0.124	2.86	C/CE
D1.5-0.1-1	1.5	1.250	0.1	2.09	9.46	1.44	6.4	0.136	1.60	C
D1.5-0.1-2	1.5	1.250	0.1	2.16	9.49	1.45	5.98	0.12	1.61	C
D1.5-0.1-3	1.5	1.250	0.1	1.61	8.25	1.20	5.17	0.139	1.21	C
D1.5-1-1	1.5	1.250	1.0	29.44	12.01	1.63	8.85	0.141	2.57	C
D1.5-1-2	1.5	1.250	1.0	16.29	11.39	1.60	7.61	0.131	2.31	C
D1.5-1-3	1.5	1.250	1.0	23.03	11.25	1.51	8.09	0.132	2.26	C
D1.5-3-1	1.5	1.250	3.0	49.83	11.33	1.72	9.83	0.109	2.29	C
D1.5-3-2	1.5	1.250	3.0	38.21	11.66	1.73	9.78	0.11	2.43	C/CE
D1.5-3-3	1.5	1.250	3.0	42.28	12.86	1.78	9.98	0.117	2.95	C/CE
D1.5-8-1	1.5	1.250	8.0	167.54	13.3	1.97	8.58	0.102	3.16	C/CE
D1.5-8-2	1.5	1.250	8.0	129.46	12.97	1.87	8.76	0.112	3.00	C/CE
D1.5-8-3	1.5	1.250	8.0	160.61	12.32	1.80	9.34	0.108	2.71	C/CE

126 *Note: RI* represents the fibre-reinforcing index as indicated in Figure 1; *C* means debonding

127 in concrete layer; *CE* is the interface debonding between concrete and epoxy; and “-” means

128 unavailable data.

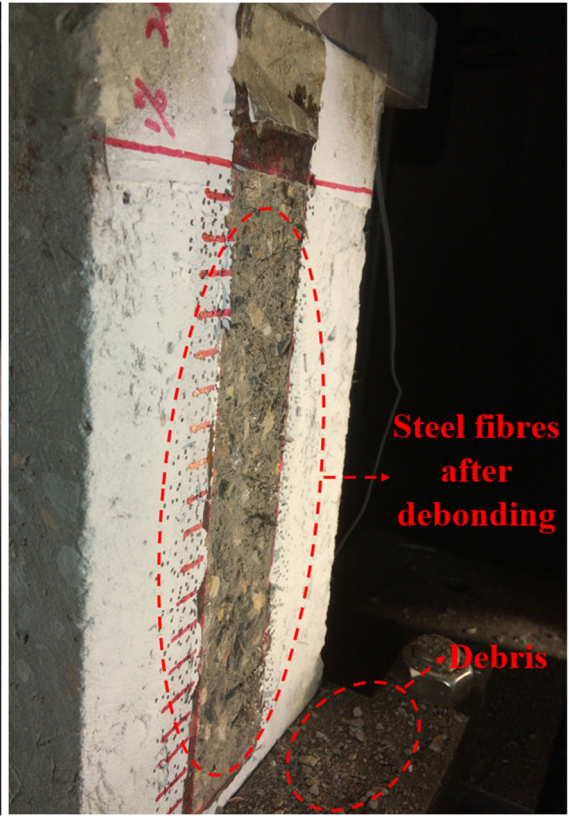
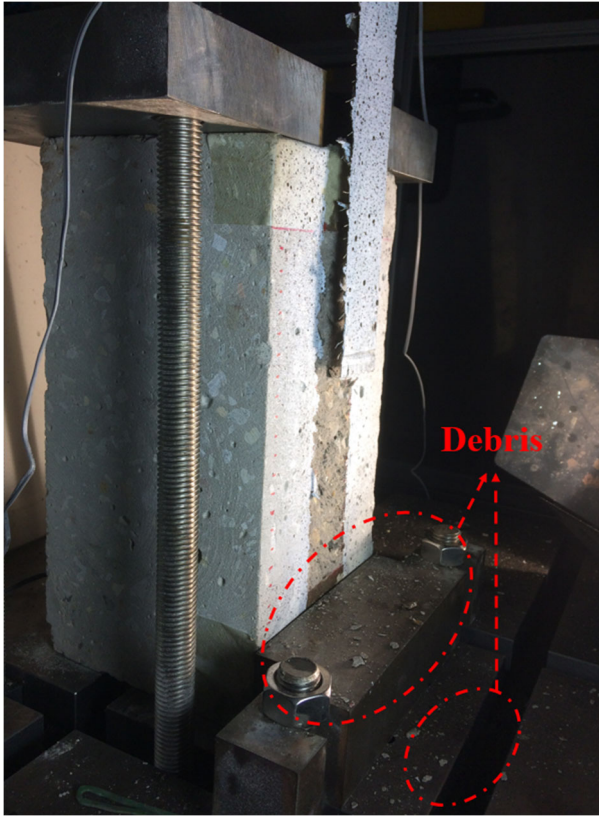
### 129 **3. Experimental results and discussions**

130 Experimental results from the impact single-lap shear tests are only valid when the  
131 equilibrium condition is achieved. The equilibrium condition was checked carefully in this  
132 study and only those results which satisfy this condition are included. Details of the analysis  
133 on the equilibrium and validity of the tests are presented in Section 3.2.

#### 134 **3.1 Failure modes and debonding load**

135 Debonding of BFRP sheets associated with concrete debris was observed in all the tested  
136 specimens under both quasi-static and dynamic loadings. For all the test specimens,  
137 debonding location changed from concrete layers to interface of concrete-epoxy with the  
138 increase of loading rates. During the process of debonding, debris of coarse aggregates,  
139 mortar and steel fibres with the detachment of FRP sheets can also be observed, as shown in  
140 Figure 2 (a), (b) , and (c). Additionally, with the volumetric fraction of steel fibres increasing,  
141 more steel fibres were pulled out from the matrix. The typical debonding failure modes of the  
142 tested specimens are shown in Figure 2 (d) and (e). It is observed that the additional steel  
143 fibres had a marginal effect on the debonding mechanism for the BFRP-SFRC interface.  
144 However, the debonding mechanism changed with the debonding location from the concrete  
145 layer (*C*) to the interface between concrete and epoxy (*CE*) with the loading rate increasing,  
146 as shown in Figure 2 (d) and (e). This might be because the tensile strength of FRC concrete  
147 is enhanced significantly with the rising strain rate while the strain rate has a marginal effect  
148 on the strength of epoxy resin [25, 26]. At a low loading rate, the specimen has enough time  
149 to initiate the internal defects and develop the cracks through the weak zone in the concrete  
150 substrate. However, at a high loading rate, the concrete strength is enhanced due to the strain  
151 rate effect, and at the same time the specimen has no enough time to extend the cracks  
152 through the concrete substrate. Therefore the failure extends along the concrete-adhesive  
153 interface for the single-lap shear test.

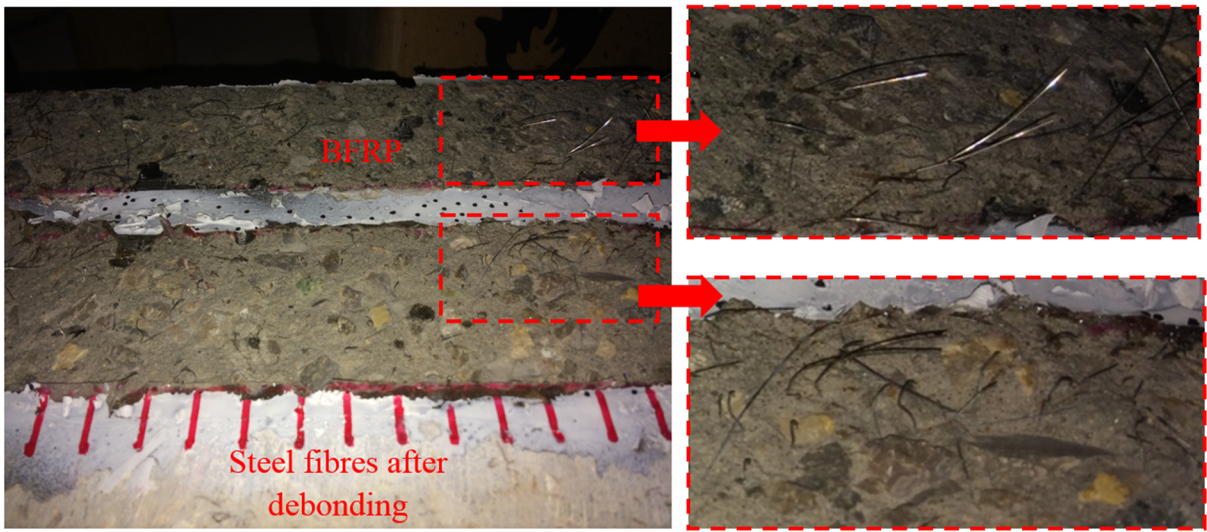




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155 (a) Plain concrete debris after testing (QS0-3-1)

(b) SFRC debris after testing (D1-3-1)



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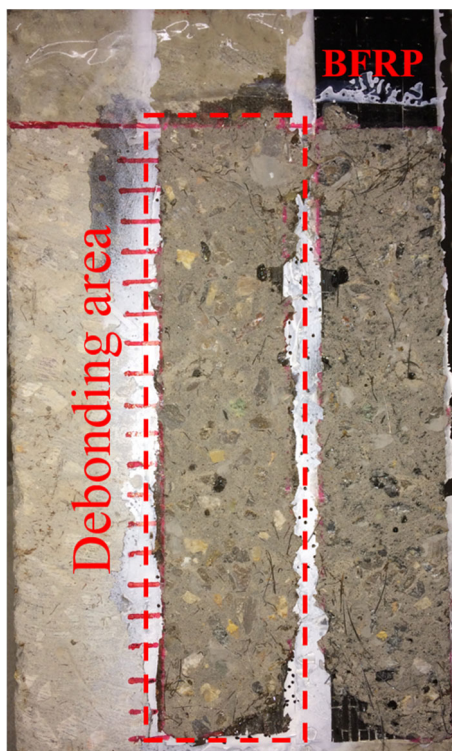
(c) Pull-out of steel fibres for D1-1-1 after testing





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(d) Failure mode of (L) QS0-1 and (R) D0-8-1

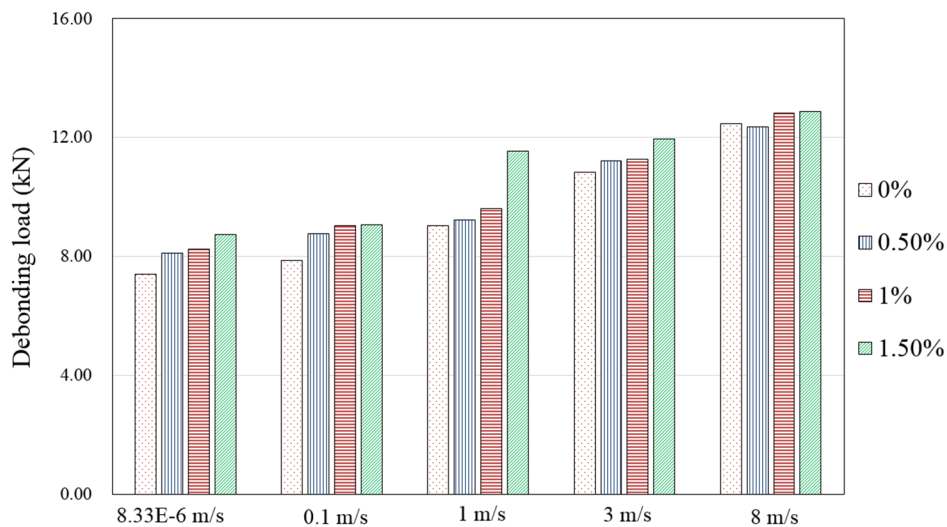


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(e) Failure mode of (L) QS1-1 and (R) D1-8-1

Figure 2. Photograph of failure modes

164 Figure 3 shows the impact of steel fibre volume on the debonding loads under different  
 165 loading rates. The general trend of the test results shows that the debonding load increased  
 166 with fibre volume as well as the loading speed. The increased debonding load is caused by  
 167 the enhanced tensile strength of concrete with the fibre volume increasing. For example as  
 168 the volume increased from 0% to 1.5%, the debonding load increased by 15.2 % from 7.87  
 169 kN to 9.07 kN at the loading speed of 0.1 m/s.



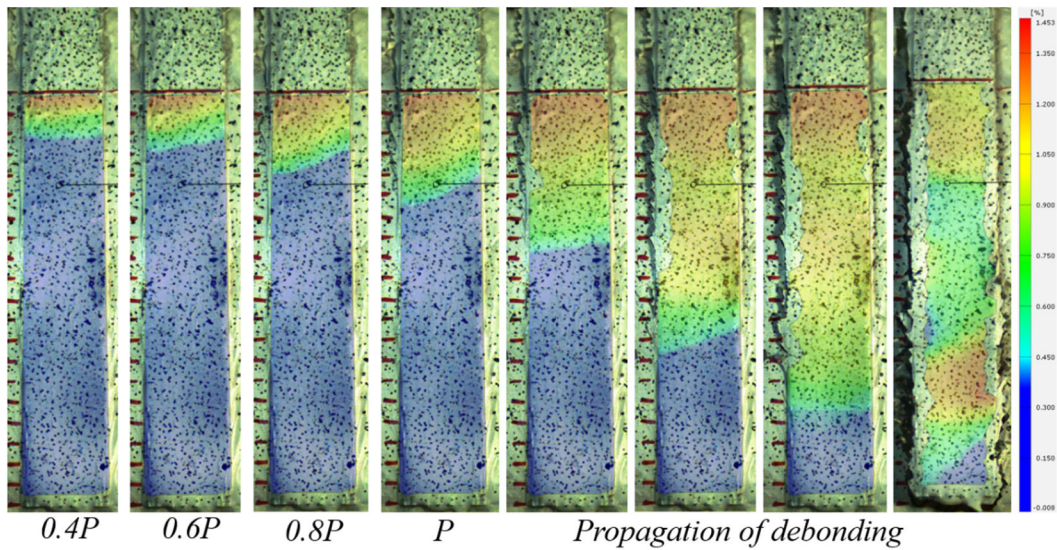
170  
 171 Figure 3. Debonding load under various loading rates

### 172 3.2 Strain time curves and stress equilibrium

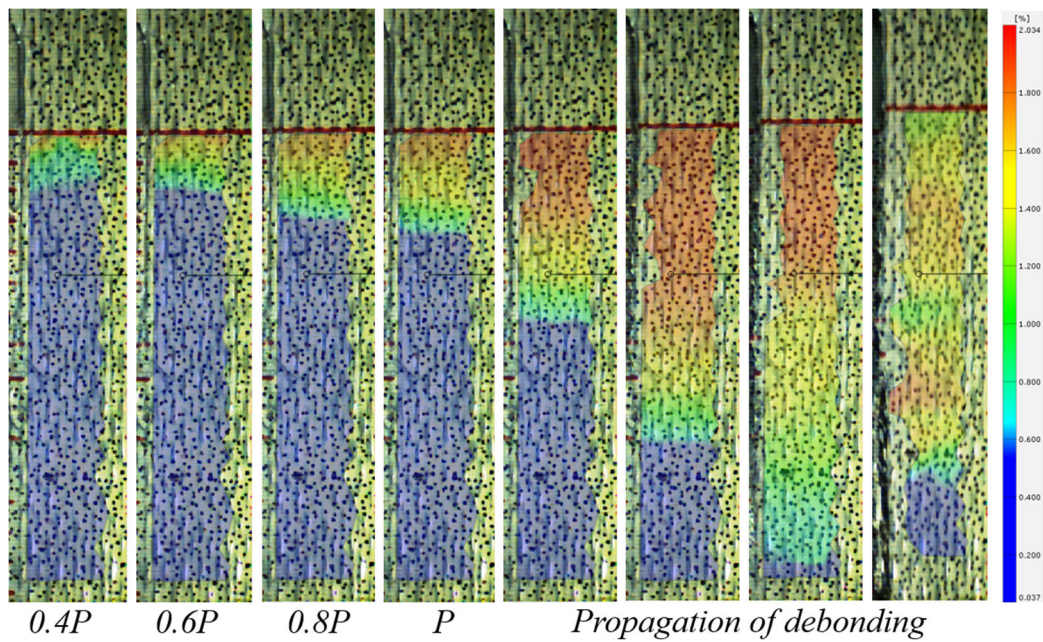
173 Figure 4 plots the strain contours at different loading rates. The strain contour consists of  
 174 different colours, red colour refers to the maximum strain while dark blue colour represents  
 175 the minimum strain. The strain contours show the strain distributions at different loading  
 176 stages under various loading velocities. At the initial stage of loading (i.e 0.4P), a large local  
 177 strain gradient in red colour was seen near the loaded end. With the tensile load increasing,  
 178 the localized zone in red colour continued to develop and propagated along the BFRP sheets  
 179 and a transition zone in colours of yellow and green formed. The distance of the strain  
 180 transition zone is known as the stress transfer zone, which increased slightly due to the added



181 steel fibres but decreased with the loading rate increasing. The added steel fibres and strain  
182 rate had a marginal impact on the pattern of strain distribution.



(a) D0.5-0.1-1



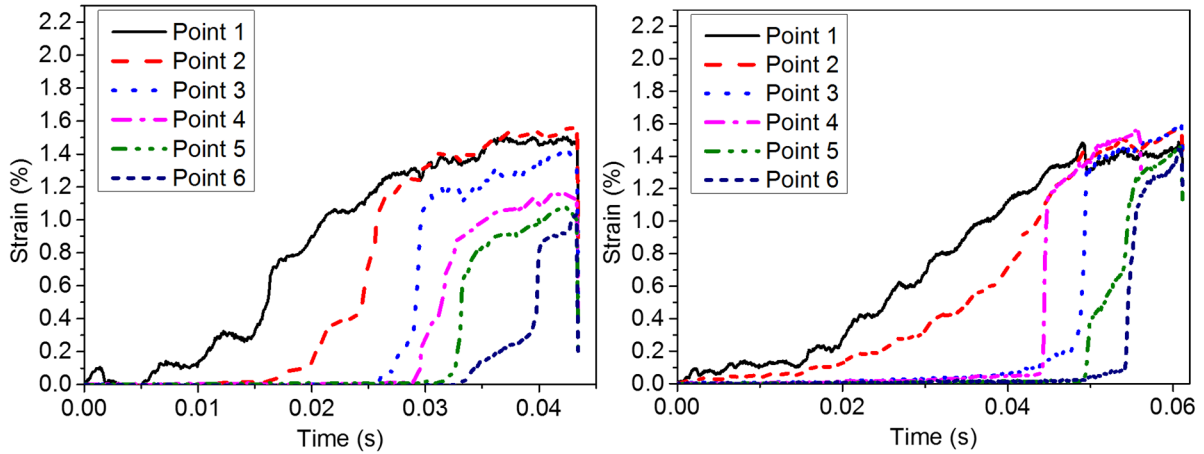
(b) D1.5-8-1

Figure 4. Strain contours at the loading velocities

188 Figure 5 illustrates the strain time histories of the tested specimens at the loading velocities of  
189 0.1 m/s and 8 m/s. Six points along the BFRP sheets in the bonded region were selected as  
190 the tracking points, as shown in Figure 1 (c). It is found that the strain vs. time curves are



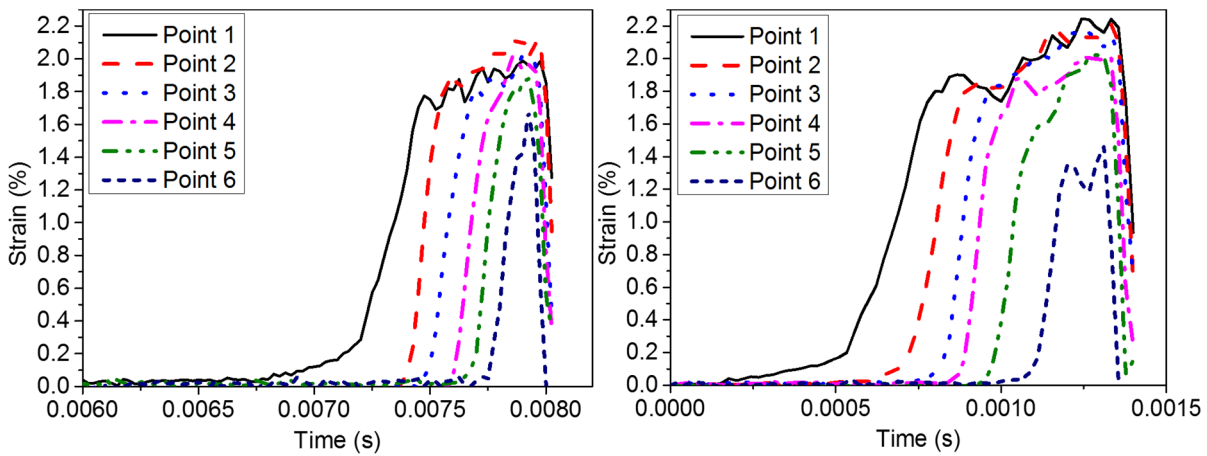
191 steeper under higher loading velocity than the case under lower loading velocity.  
 192 Additionally, the ultimate debonding strain increased with the steel fibre volume under both  
 193 the quasi-static and dynamic tests. The higher debonding strain of BFRP sheets was resulted  
 194 from the enhanced shear resistance of the BFRP-to-concrete interface.



195  
 196  
 197

(a) D0.5-0.1-1

(b) D1.5-0.1-1



198  
 199  
 200

(c) D0.5-8-1

(d) D1.5-8-1

Figure 5. Strain-time histories

201 To check the validity of the experimental results, the dynamic stress equilibrium must be  
 202 achieved in the dynamic test [27, 28]. For the quasi-static single shear tests, the loading rate  
 203 of 0.5 mm/min allows the stress wave to travel forth and back many times inside the interface  
 204 to obtain the stress equilibrium. To validate the dynamic stress equilibrium, six points along  
 205 the centreline of BFRP sheets in the bonded region were selected to compare the strain

206 distributions at different loading stages (Figure 1 (c)). As shown in Figure 5, the strain  
 207 distributions obtained from the six selected points show very similar shape and value. The  
 208 strain of BFRP sheets almost reached the plateau indicating the uniform strain distribution  
 209 and thus uniform stress or stress equilibrium condition was achieved. It should be noted that  
 210 Point 1 and Point 6 have slightly different strain distributions from other points. It is because  
 211 Point 1 is located at the boundary of unbonded and bonded regions where the stress  
 212 redistributes and Point 6 is close to the free end where the full debonding behaviour cannot  
 213 develop due to the brittle debonding process [29].

214 In addition, Figure 6 illustrates the strain rate distributions along the BFRP sheets at different  
 215 time instants. The strain rate was obtained by the differentiation of strain time history using

216  $\dot{\epsilon} = \frac{d\epsilon}{dt}$ . A bell-shape strain rate propagation along the BFRP sheets can be observed for all

217 the test specimens. The strain rate increased with the loading speed and the strain rate for D1-  
 218 1-1 was  $28.09 \text{ s}^{-1}$  at the loading velocity of 1 m/s and the strain rate for D1.5-8-1 was  $167.54$   
 219  $\text{s}^{-1}$  at the loading velocity of 8 m/s. All the tested specimens show the similar strain rate  
 220 distribution along the bonding length and the testing results are summarized Table 2.

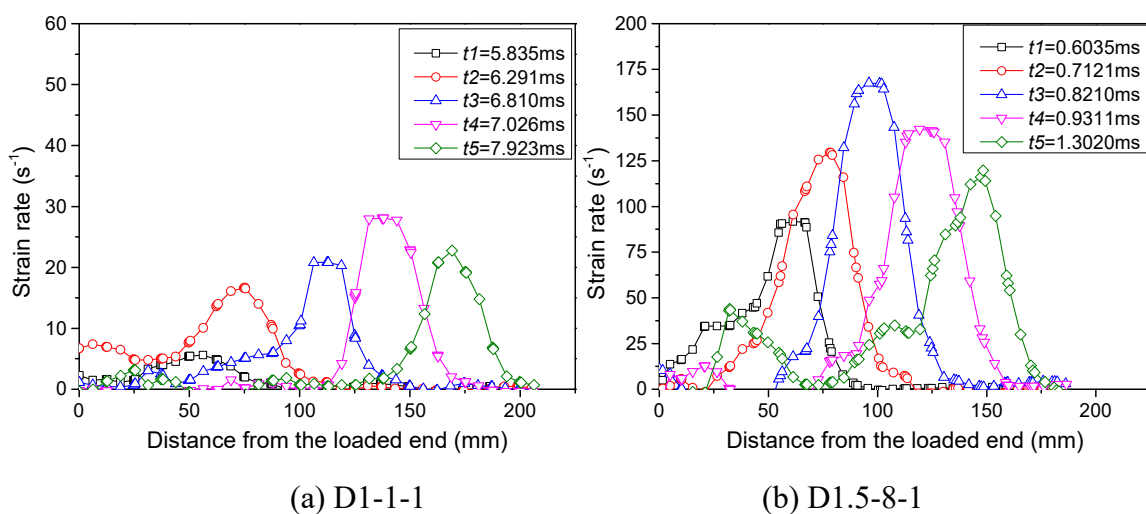
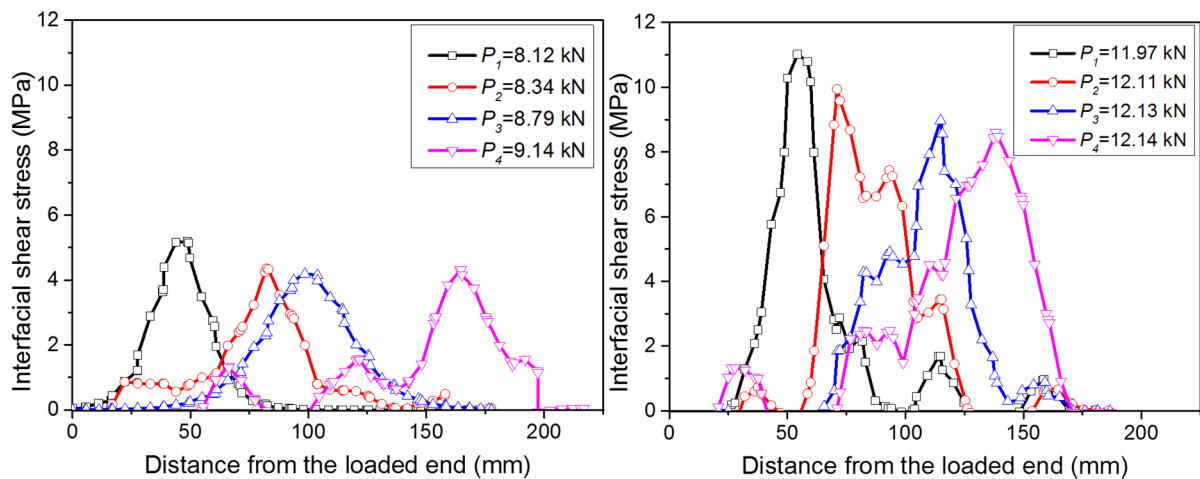


Figure 6. Strain rate distribution at different loading velocities

224 Figure 7 illustrates the local shear stress distribution. Four different loading levels after the  
 225 initial debonding load were selected to obtain a robust shear stress distribution. With the  
 226 applied load increasing, the peak value of the shear stress gradually propagated to the free  
 227 end. Due to the shear stress concentration near the loaded end, a relatively higher shear stress  
 228 was observed and then the shear stress maintained approximately constant with the  
 229 debonding propagation. The shear stress increased significantly with the strain rate but  
 230 increased slightly with the fibre volume. As compared to Specimen D0.5-0.1-1, the average  
 231 PSS of Specimen D0.5-8-1 increased by 113% when the strain rate increased from  $2.11 \text{ s}^{-1}$  to  
 232  $131.73 \text{ s}^{-1}$ . Compared to the strain rate effect, the effect of fibre volume on the PSS was  
 233 relatively small. There was a 37% increment in the PSS at the same loading speed of  $0.1 \text{ m/s}$   
 234 when the fibre volume increased from 0.5% to 1.5%.

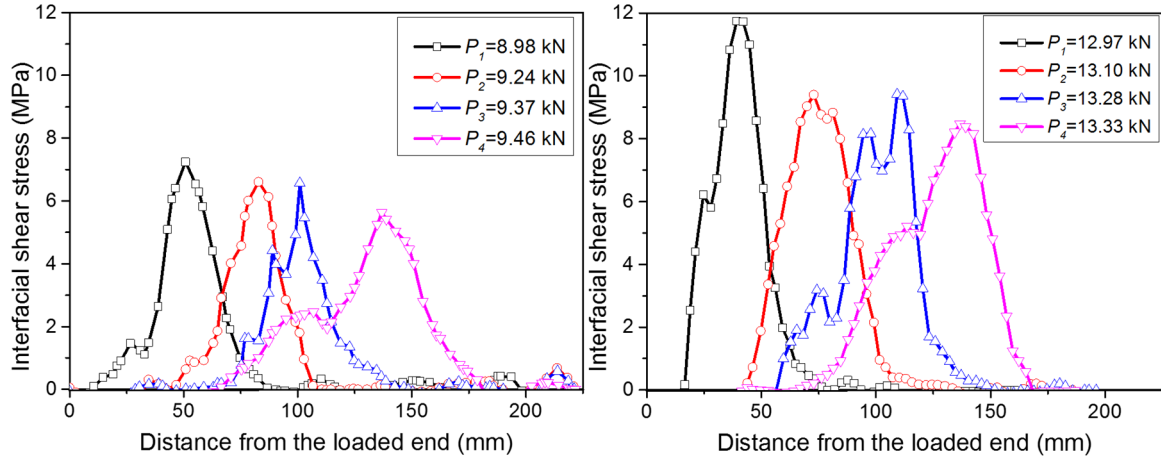


235

(a) D0.5-0.1-1

236

(b) D0.5-8-1



(c) D1.5-0.1-1

(d) D1.5-8-1

Figure 7. Local shear stress distribution

### 3.3 Experimental bond-slip curves

The DIC technique was used to measure the BFRP strain distributions and the relative slip, which can be used to obtain the interfacial bond-slip curves. The reliability of this technique as compared to readings from strain gauges was verified in the previous studies [23, 30]. Figure 8 and Figure 9 illustrate the typical bond-slip curves with different steel fibre volumes under various loading rates. The following equations can be used to obtain the interfacial shear stress and shear slip based on the measured strain distributions [31]:

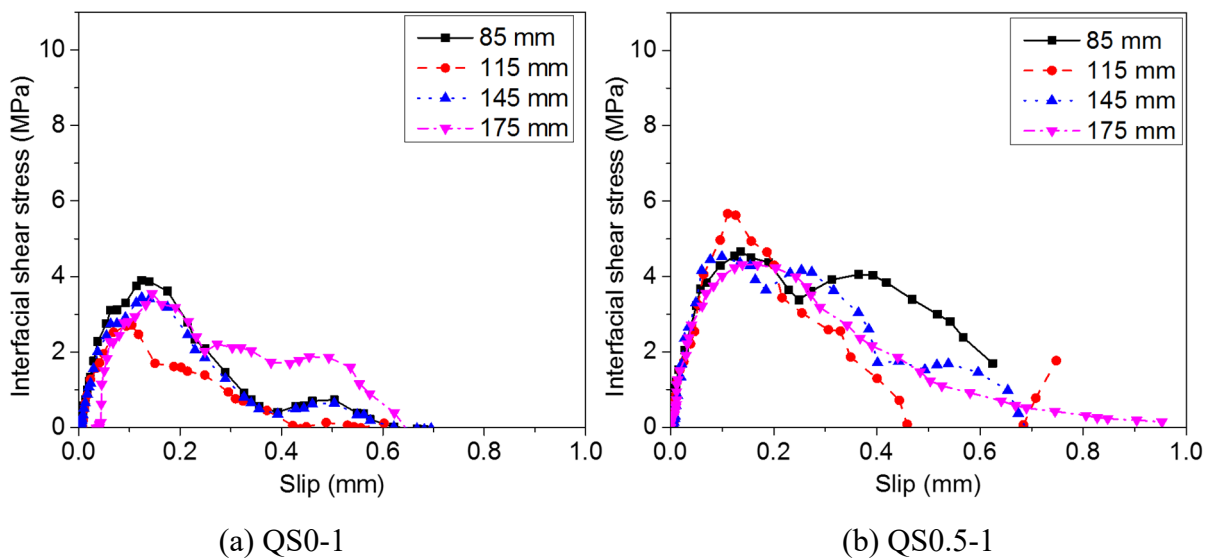
$$\tau(x) = E_f t_f \frac{d\varepsilon}{dx} \quad (1)$$

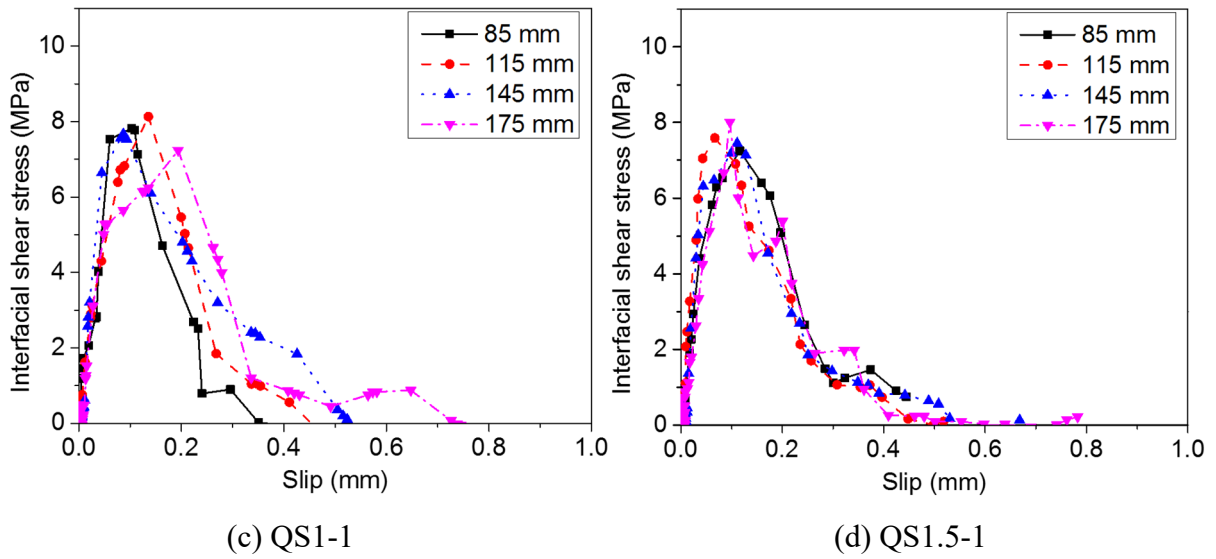
$$s(x) = \int \varepsilon dx \quad (2)$$

where  $\tau(x)$  is the interfacial shear stress,  $E_f$  is the elastic modulus,  $t_f$  is the thickness of BFRP sheet,  $d\varepsilon/dx$  is the strain gradient,  $s(x)$  is the shear slip along the BFRP sheets, and  $\varepsilon$  is the strain measured by the DIC technique.

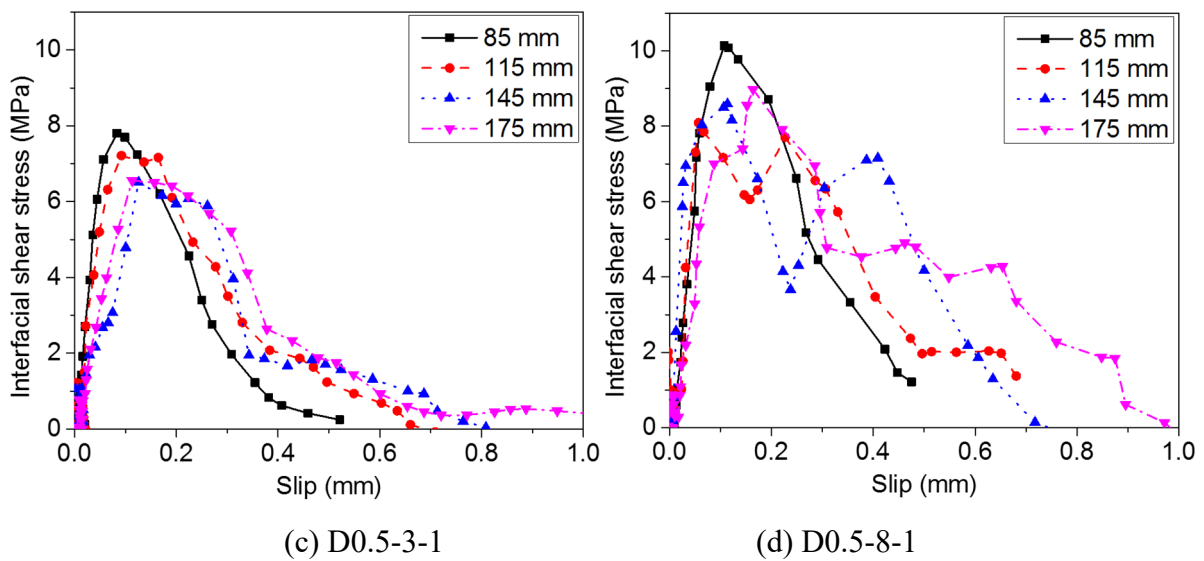
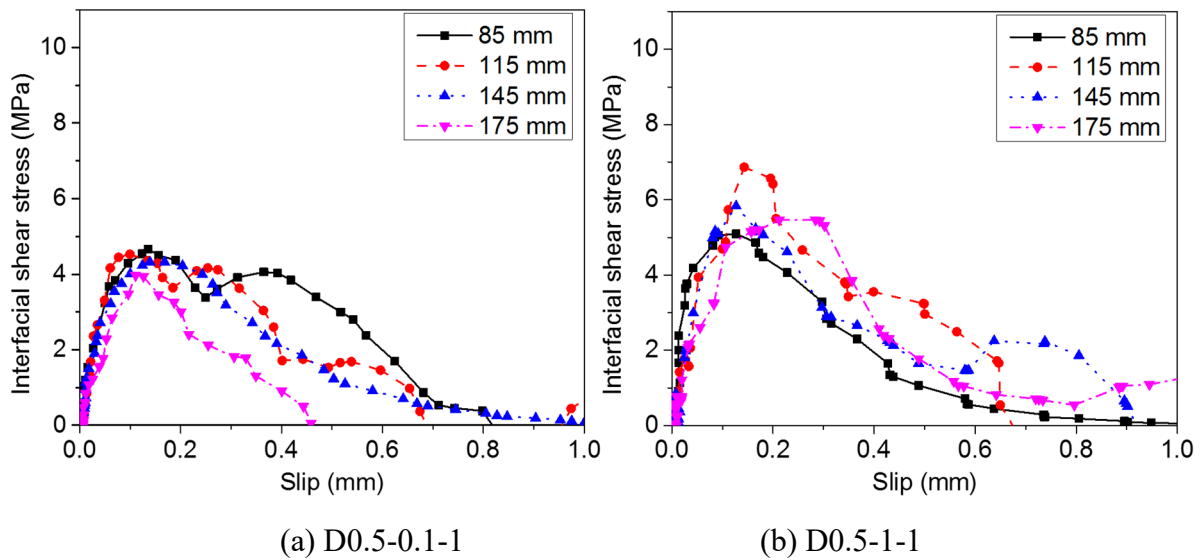
Figure 8 and Figure 9 illustrate the bond-slip relationships of each specimen under four loading levels and the peak shear stress (PSS) of each specimen is obtained from the mean

254 value at four different loading levels after the initial debonding load. The distance of 85 mm,  
 255 115 mm, 145 mm, and 175 mm shown in the legend refer to the range of strain distributing at  
 256 the four different loading levels after the initial debonding load. It is observed that the bond-  
 257 slip curves for PCs and SFRCs under quasi-static and dynamic loadings exhibit the similar  
 258 trend, i.e. non-linear ascending and descending branches [32]. With the shear slip increasing,  
 259 the reduction of shear stress was observed. Figure 8 illustrates the effect of steel fibre volume  
 260 on the bond-slip response under quasi-static loading and the results show that the interfacial  
 261 PSS increased with fibre volume. Figure 9 shows the effect of strain rate on the bond-slip  
 262 response for Specimen D0.5 under different loading rates. It is clear that the PSS increased  
 263 significantly with strain rate. Compared with the effect of fibre volume, the impact of strain  
 264 rate on the interfacial shear stress is more significant.





269 Figure 8. The relationship between peak shear stress and fibre volume under quasi-static  
 270 loading



276 Figure 9. The relationship between peak shear stress and loading speed under different  
277 dynamic loadings

278

### 279 **3.4 Effect of steel fibres on the interfacial bond**

280 Figure 10 illustrates the influence of steel fibre volumetric fraction on the BFRP-concrete  
281 interface bond behaviour. It is found that the average debonding load, the interfacial fracture  
282 energy (IFE), the ultimate debonding strain, and the PSS increased with the steel fibre  
283 volume. As compared to the control group (PC), the average debonding loads of the  
284 specimens with volumetric fraction of 0.5%, 1%, and 1.5% increased by 9.46%, 11.35%, and  
285 17.91% at quasi-static loading, and increased by 3.43%, 3.98%, and 10.19% at dynamic  
286 loading rate of 3 m/s, respectively. Due to the bridging action of fibres in the matrix, the  
287 fracture area of BFRP-to-SFRC is relatively larger than that of BFRP-to-PC. In this study, the  
288 tensile strength of concrete increased with the steel fibre volume, which is consistent with the  
289 previous study [33]. The increased tensile strength of concrete leads to the increased  
290 interfacial fracture energy. As compared to the quasi-static tests, the specimens with 0%,  
291 0.5%, 1% and 1.5% fibre volume at the dynamic loading speed of 8 m/s experienced the  
292 increment of average PSS by 338%, 257%, 210%, and 174 % and the average IFE increased  
293 by 184%, 133%, 142%, and 117%, respectively. It should be noted that the interfacial PSS  
294 increased with the rising strain rate in general while the PSS stopped rising over the loading  
295 speed of 3 m/s for the case of 1.5% fibre volume. It might be due to the strain fluctuation  
296 caused by the system ringing under relatively high loading speed (i.e. 8 m/s) because the  
297 shear stress was derived from the strain profile. For instance, the obtained shear stress was  
298 averaged from the shear stress at four different locations (i.e. 85 mm, 115 mm, 145 mm and  
299 175 mm), which show the variations of PSS as shown in Figure 9 (d).

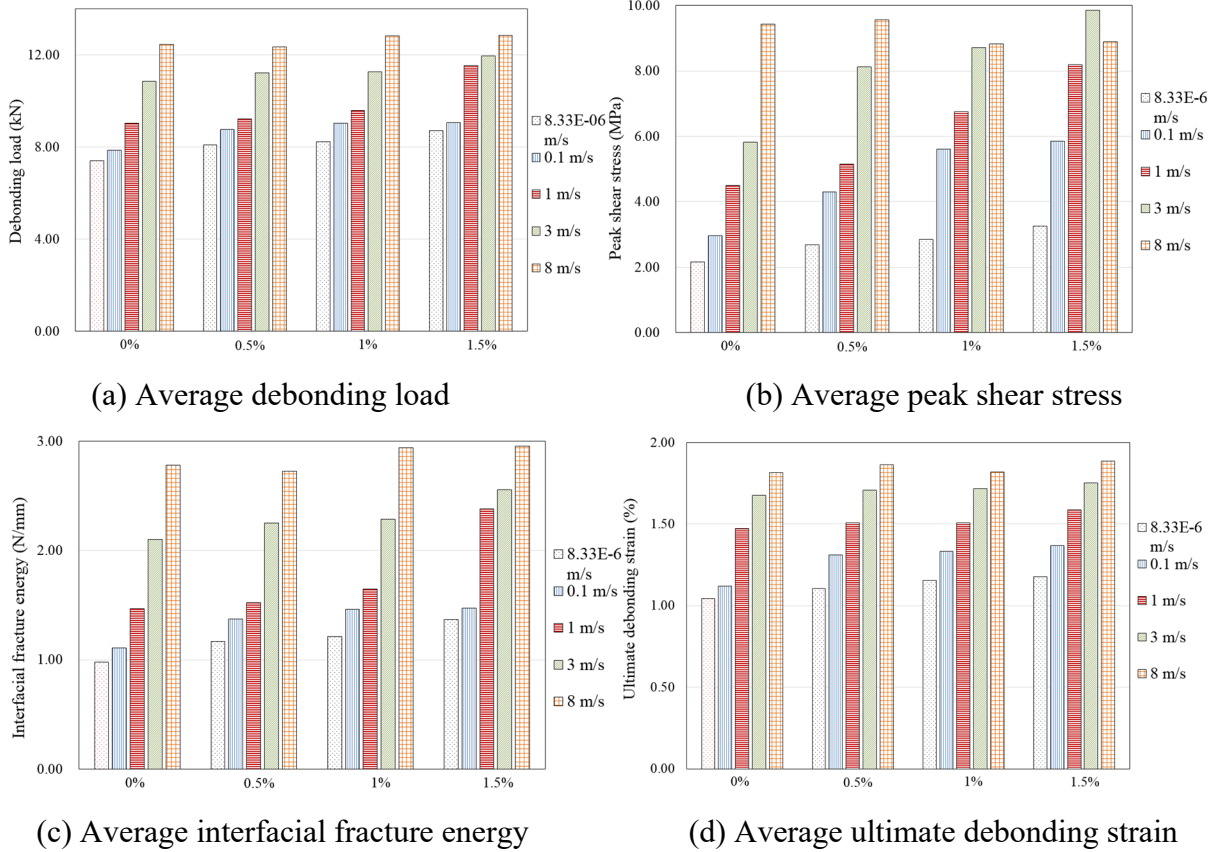
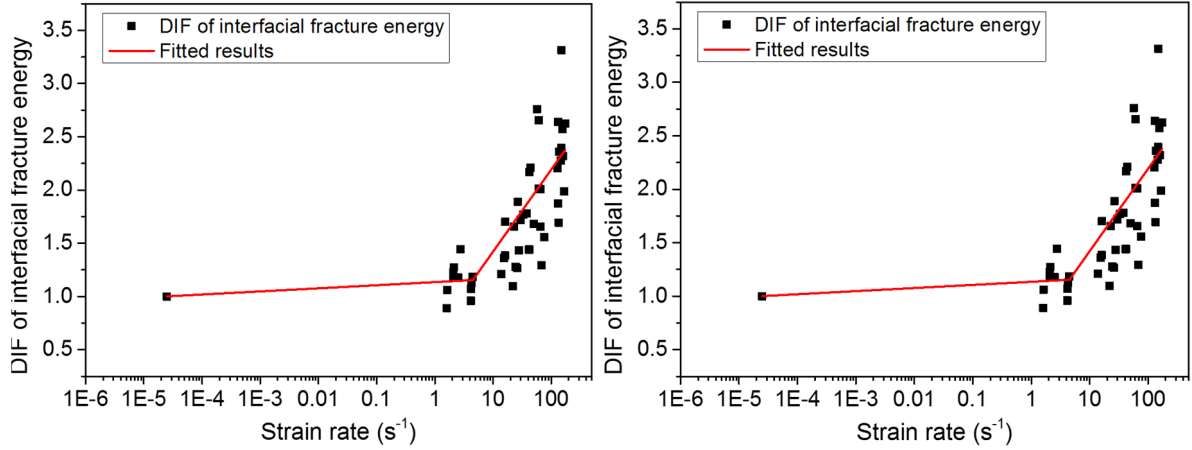


Figure 10. Effect of steel fibre volume under different loading rates

### 3.5 Effect of strain rate on the bond behaviour

As given in Table 2, the debonding load, the ultimate debonding strain, the IFE, and the PSS are strain rate dependent for both the BFRP-to-PC and BFRP-to-SFRC interfaces. For the modelling purpose in the following section, the dynamic increase factors (DIF) against the corresponding strain rate for the IFE ( $Gf$ ) and PSS ( $\tau_m$ ) are proposed and plotted in Figure 11. A bilinear relationship between the obtained DIF and strain rate is presented in logarithmic functions. It is observed that the increments of IFE and PSS are not significant when the strain rate is less than  $3 \text{ s}^{-1}$  while the increment becomes more apparent when the strain rate is great than  $3 \text{ s}^{-1}$ . This is because both the plain concrete (PC) and SFRC are strain rate dependent materials and the tensile strength increases with the strain rate, especially when the strain rate is higher than  $3 \text{ s}^{-1}$  [34, 35].





(a) Interfacial fracture energy

(b) Peak shear stress

Figure 11. DIF vs. strain rate

316

317

318

319 Based on the testing data, the following empirical equations are proposed for predicting the  
 320 dynamic values by substituting the obtained DIF into the proposed model of IFE and PSS.

321 For dynamic interfacial fracture energy:

$$322 \quad DIF_{G_f} = 0.0291 \log(\dot{\epsilon}) + 1.135, \text{ when } 2.5 \times 10^{-5} s^{-1} \leq \dot{\epsilon} \leq 3 s^{-1} \quad (3)$$

$$323 \quad DIF_{G_f} = 0.9001 \log(\dot{\epsilon}) + 0.358, \text{ when } 3 s^{-1} \leq \dot{\epsilon} \leq 173.55 s^{-1} \quad (4)$$

324 For dynamic interfacial PSS:

$$325 \quad DIF_{\tau_m} = 0.1257 \log(\dot{\epsilon}) + 1.629, \text{ when } 2.5 \times 10^{-5} s^{-1} \leq \dot{\epsilon} \leq 3 s^{-1} \quad (5)$$

$$326 \quad DIF_{\tau_m} = 1.2049 \log(\dot{\epsilon}) + 0.8, \text{ when } 3 s^{-1} \leq \dot{\epsilon} \leq 173.55 s^{-1} \quad (6)$$

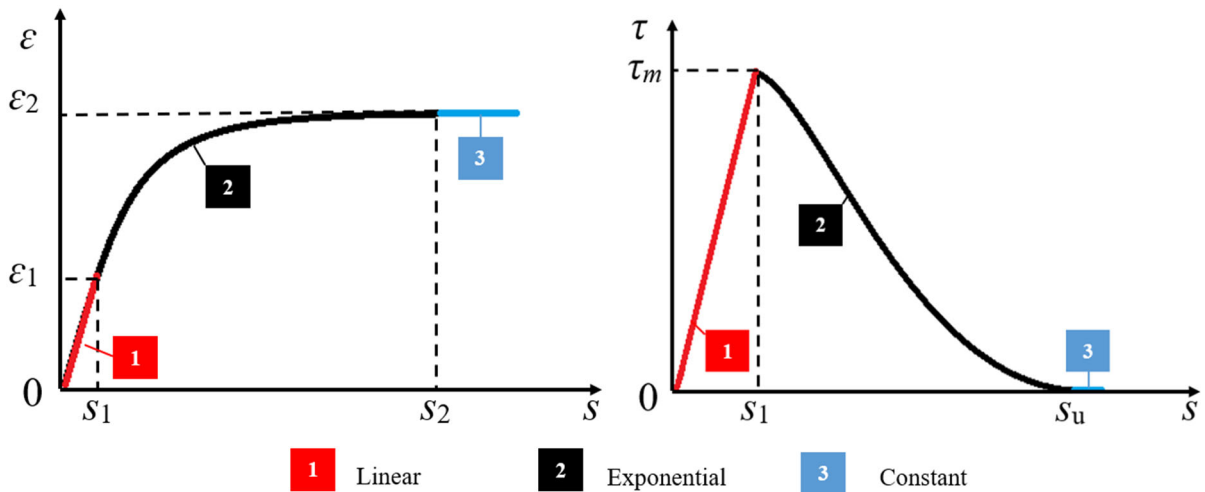
327 where  $DIF_{G_f}$  and  $DIF_{\tau_m}$  are respectively dynamic increase factor ( $DIF$ ) of IFE  $G_f$  and PSS  $\tau_m$ ,

328 and  $\dot{\epsilon}$  is strain rate.

## 329 4. Analytical investigation and the proposed model

### 330 4.1 Dynamic bond-slip relationship

331 Figure 12 (R) illustrates the typical bond-slip curves for the tested specimens. It is observed  
 332 that all the tested specimens exhibited an approximately triangular shape with a linear  
 333 ascending stage before the PSS, and after that a non-linear descending stage is observed until  
 334 the final debonding [36-38]. A linear equation can be used to depict the ascending stage, and  
 335 an exponential function can be used to describe the descending stage. As shown in Figure 12  
 336 (L), three stages can be defined in the strain-slip curves: (1) linear; (2) nonlinear; and (3)  
 337 constant [39, 40]. These three stages from the strain-slip curves can derive the corresponding  
 338 three parts in the local bond-slip curves as shown in Figure 12 (R).



339  
 340 Figure 12. Determination of the bond-slip curve (L) Strain-slip curve; (R) Bond-slip curve

341 Based on the determined shape of the bond-slip curve in Figure 12 (R), the shear stress can be  
 342 expressed as follows [29]:

$$343 \tau(s) = \begin{cases} \tau_m \left( \frac{s}{s_1} \right) & s \leq s_1 \\ \tau_m e^{-\omega(s-s_1)} & s_1 \leq s \leq s_u \\ 0 & s_u \leq s \end{cases} \quad (7)$$

344 where  $\tau(s)$  is the shear stress,  $\tau_m$  is the PSS,  $s_l$  is the maximum elastic slip, and  $s$  is the shear  
 345 slip.

346 The IFE  $G_f$  is defined as the enclosed area of the bond-slip curve for the FRP-to-concrete  
 347 interface, the following expression can be used to calculate the interfacial fracture energy:

$$348 \quad G_f = \int_0^{+\infty} \tau ds = \int_0^{s_l} \tau ds + \int_{s_l}^{+\infty} \tau ds \quad (8)$$

349 By integrating the shear stress and the slip, the IFE can be determined as follows:

$$350 \quad G_f = \frac{1}{2} \tau_m s_l + \int_{s_l}^{+\infty} \tau_m e^{-\omega(s-s_l)} ds = \frac{1}{2} \tau_m s_l + \frac{\tau_m}{\omega} \quad (9)$$

351 The coefficient  $\omega$  can be expressed by [41]:

$$352 \quad \omega = \frac{\tau_m}{G_f - \frac{1}{2} s_l \tau_m} \quad (10)$$

353 Therefore, the bond-slip model can be characterized by some key parameters (i.e.  $\tau_m$ ,  $s_l$ ,  $s_u$ ,  
 354 and  $\omega$ ). It can be found that these key parameters can be determined by the interfacial fracture  
 355 energy ( $G_f$ ). Once these key parameters are determined, the dynamic bond-slip relationship  
 356 can be obtained.

## 357 **4.2 Interfacial fracture energy**

358 The IFE ( $G_f$ ) is represented as the enclosed area of the bond-slip curve. However, due to the  
 359 fluctuation of the obtained bond-slip curves, inaccurate interfacial fracture energy might be  
 360 derived when using the bond-slip curves. Therefore, the IFE is obtained from the debonding  
 361 load in this study, as follows [42, 43]:

$$362 \quad G_f = \frac{P_u^2}{2b_f^2 t_f E_f} \quad (11)$$

363 The models to predict IFE have been proposed and adopted in numerous studies. It was  
 364 reported that the interfacial fracture energy increases with the higher tensile strength of  
 365 concrete. For SFRC, the splitting tensile strength increased with steel fibre volume, but the  
 366 added steel fibres had slight effect on the compressive strength. Thus, the formula to calculate  
 367 the tensile strength of SFRC by incorporating the fibre-reinforcing index ( $V_f L_f / \phi_f$ ) can be  
 368 expressed as follows [13]:

$$369 \quad f_t = 0.516(f'_{cu})^{0.5} + 0.101(f'_{cu})^{0.5} \left( \frac{V_f L_f}{\phi_f} \right) + 0.199 \left( \frac{V_f L_f}{\phi_f} \right) \quad (12)$$

370 For the BFRP-PC interface under quasi-static loading, it is found that the IFE correlates well  
 371 with the FRP-to-concrete width ratio ( $\beta_w$ ) and tensile strength of concrete ( $f_i$ ) [44]. In addition,  
 372 the debonding failure shifted from concrete layer to epoxy-concrete interface and fracture of  
 373 epoxy was also observed under high loading speed (i.e. 8 m/s). Thus, the contribution of  
 374 epoxy on the IFE should be taken into account [45]. The tensile strain energy of epoxy  $\frac{f_a^2}{2E_a}$ ,  
 375 which is represented as the area under the tensile stress-strain curves of the epoxy was  
 376 incorporated into the proposed model. The testing data from the existing studies [20, 46-49]  
 377 and the testing data from this study were employed to conduct the regression analysis. Table  
 378 3 summarizes the specimen details and the test results. Therefore, the empirical model based  
 379 on the best-fit coefficients can be obtained as follows:

$$380 \quad G_{f,s}(PC) = 0.55 \beta_w^2 \left( \frac{f_e^2}{2E_e} \right)^{0.42} \sqrt{f_t} \quad (13)$$

381 **Table 3.** Summary and comparison of testing data

Reference	Specimen ID	Test method	Adhesive			FRP		Concrete	$P_{u,exp}$ (kN)	
			$f_a$ (MPa)	$E_a$ (GPa)	$f_a^2/2E_a$ (N/mm <sup>2</sup> )	$E_f$ (GPa)	$t_f$ (mm)	$bf$ (mm)		$f_i$ (MPa)
Present study	QS1-1	Single shear	50.50	2.8	0.455	73	0.24	40	2.85	7.87

		QS1-2	50.50	2.8	0.455	73	0.24	40	2.85	6.93
Shen et al. [46]		1-1	45.80	2.6	0.403	105	0.121	50	2.62	11.40
		1-2	45.80	2.6	0.403	105	0.121	50	2.62	10.80
		1-3	45.80	2.6	0.403	105	0.121	50	2.62	13.60
Huo et al. [20]		C50-1-1	65	3.2	0.660	236	0.169	50	2.89	13.60
		C50-1-2	65	3.2	0.660	236	0.169	50	2.89	11.50
		C50-2-1	65	3.2	0.660	236	0.338	50	2.89	18.00
		C50-2-2	65	3.2	0.660	236	0.338	50	2.89	14.20
		C80-2-1	65	3.2	0.660	236	0.338	80	2.89	17.50
		C80-2-2	65	3.2	0.660	236	0.338	80	2.89	18.40
Toutanji et al. [47]		AA-1	23.6	4.1	0.068	110	0.495	50	2.73	7.56
		AA-2	23.6	4.1	0.068	110	0.66	50	2.73	9.29
		AA-3	23.6	4.1	0.068	110	0.825	50	2.73	11.64
		AA-4	23.6	4.1	0.068	110	0.99	50	2.73	12.86
		BB-1	23.6	4.1	0.068	110	0.495	50	2.73	12.55
		BB-2	23.6	4.1	0.068	110	0.66	50	2.73	14.25
		BB-3	23.6	4.1	0.068	110	0.825	50	2.73	17.72
		BB-4	23.6	4.1	0.068	110	0.99	50	2.73	18.86
		CC-1	23.6	4.1	0.068	110	0.495	50	2.73	13.24
		CC-2	23.6	4.1	0.068	110	0.66	50	2.73	15.17
		CC-3	23.6	4.1	0.068	110	0.825	50	2.73	18.86
		CC-4	23.6	4.1	0.068	110	0.99	50	2.73	19.03
Yun et al. [48]		M-EB	54	3.0	0.289	257	0.66	50	3.03	26.30
Yun and Wu [49]		N30-0-1	45	3.5	0.289	235	0.167	50	2.81	23.7
		N30-0-2	45	3.5	0.289	235	0.167	50	2.81	24.4
		N45-0-1	45	3.5	0.289	235	0.167	50	3.22	27.7
		N45-0-2	45	3.5	0.289	235	0.167	50	3.22	27.4

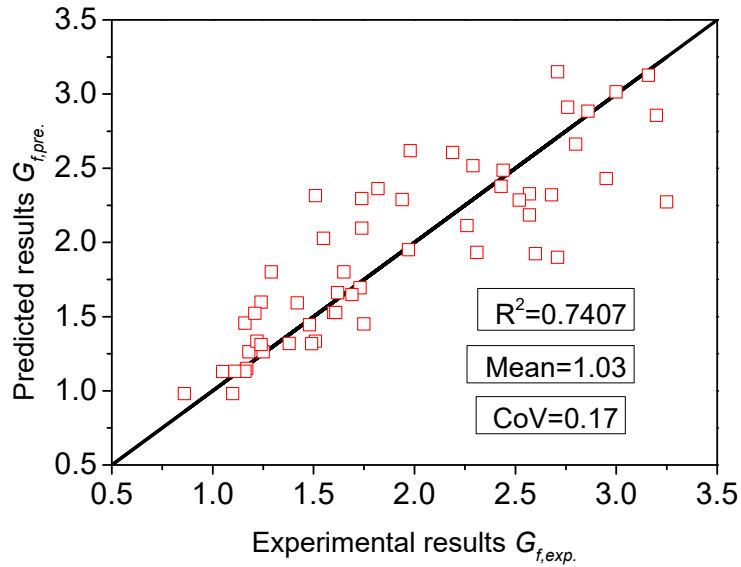
382

383 The IFE increased with the steel fibre volume. Therefore, the fibre-reinforcing index ( $V_f L_f / \phi_f$ )  
384 was set as a factor to determine the IFE of the BFRP-SFRC interface. Based on the best-fitted  
385 coefficients through regression analysis, the relationship between the IFE and fibre-  
386 reinforcing index can be expressed as follows:

$$387 \quad G_{f,s}(SFRC) = 1.321 \left( \frac{V_f L_f}{\phi_f} \right)^{0.135} G_{f,s}(PC) \quad (14)$$

388 The IFE increased with the strain rate. Therefore, by substituting the DIF in Equations  
389 (3) and (4) into Equation (14), the dynamic IFE can be obtained in Equation (15). Figure 13  
390 shows the comparison between the predicted and experimental results. The predicted results  
391 are consistent with the experimental data and the mean ratio of the predicted results to the test  
392 results is 0.7407 with the corresponding coefficient of variation (COV) of 0.17.

393  $G_{f,D}(SFRC) = DIF_{G_f} G_{f,S}(SFRC)$  (15)

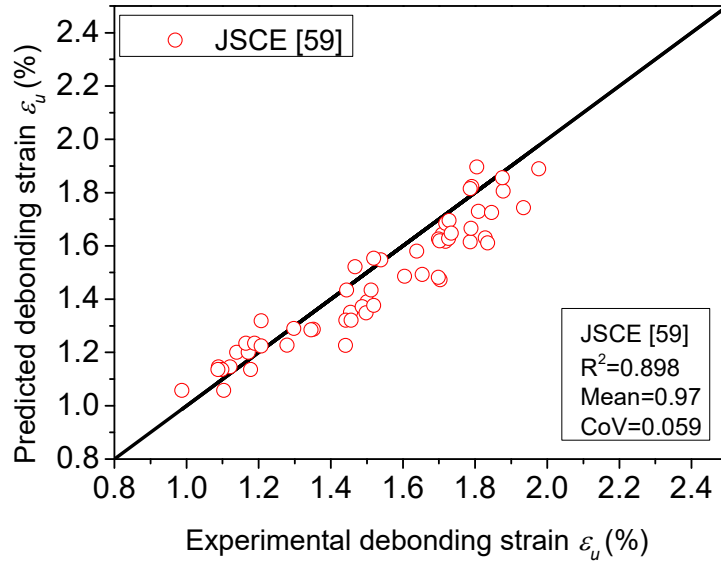


394  
395 Figure 13. Experimental vs predicted interfacial fracture energy

396 **4.3 Dynamic debonding strain**

397 The single-lap shear test is used to simulate the intermediate crack (IC) induced interfacial  
 398 debonding in the FRP-strengthened concrete structures. Due to the FRP debonding, only  
 399 30%-40% of FRP strength is utilized [50]. Numerous debonding strain models have been  
 400 proposed for design purpose [51]. However, there is no debonding strain model available  
 401 considering FRP-strengthened SFRC elements and strain rate effect. Therefore, an empirical  
 402 debonding strain model by incorporating steel fibre volume and strain rate is proposed in this  
 403 study. Using the model proposed by JSCE [52], the proposed IFE by incorporating the steel  
 404 fibre volume and strain rate expressed in Equation (15) can be used to obtain the ultimate  
 405 debonding strain in Equation (16). The predicted results are in good agreement with the  
 406 experimental data, as shown in Figure 14. The mean ratio of the predicted results to the  
 407 experimental results was 0.97, and the corresponding coefficient of variation (COV) was  
 408 0.059.

$$409 \quad \varepsilon_{u,D} = \sqrt{\frac{2G_{f,D}}{E_f t_f}} \quad (16)$$



410

411

Figure 14. Experimental vs predicted debonding strain

#### 412 4.4 Dynamic peak shear stress and slip

413 The interfacial PSS is obtained from the strain distributions. Based on the test results of the  
 414 present study, the PSS increased slightly with steel fibre volume and increased significantly  
 415 with strain rate. There is a consistent finding that the interfacial shear stress is determined by  
 416  $f_t$  and  $\beta_w$  [53, 54]. Therefore, the formula to predict the static PSS can be expressed as follows:

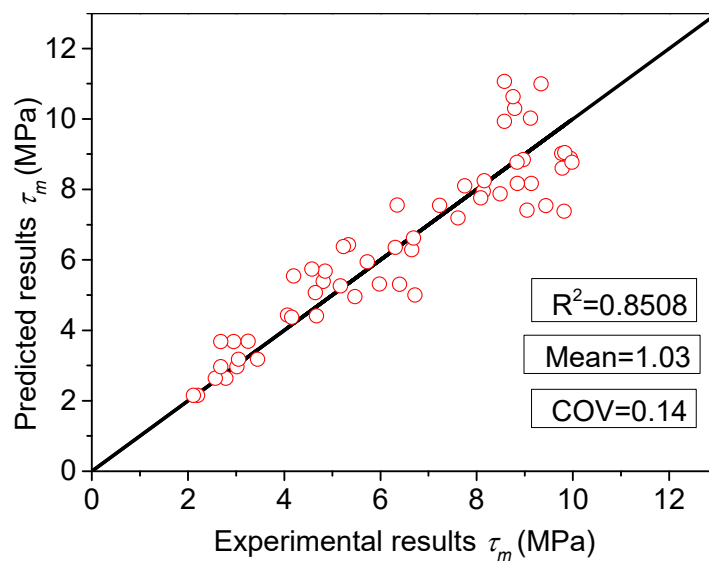
$$417 \quad \tau_{m,s}(PC) = 0.646\beta_w\sqrt{f_t} \quad (17)$$

418 The interfacial PSS increased with the steel fibre volume. Therefore, the fibre-reinforcing  
 419 index ( $V_f L_f / \phi_f$ ) should be a factor determining the PSS of the BFRP-SFRC interface. Based on  
 420 the best-fit coefficients from regression analysis, the interfacial PSS can be expressed by the  
 421 fibre-reinforcing index in the following way:

$$422 \quad \tau_{m,s}(SFRC) = 1.421 \left( \frac{V_f L_f}{\phi_f} \right)^{0.17} \tau_{m,s}(PC) \quad (18)$$

423 The interfacial PSS increased with the rising strain rate. Therefore, by substituting the DIF in  
 424 Equations (5) and (6) into Equation (18), the dynamic interfacial PSS in Equation (19) can be  
 425 obtained. Figure 15 shows the comparison between the predicted and experimental results.  
 426 The predicted results are in good agreement with the test data as the ratio between the  
 427 predicted and test results is 1.03 and the corresponding coefficient of variation (COV) is 0.14.

$$428 \quad \tau_{m,D}(SFRC) = DIF_{\tau_{m,s}} \tau_{m,s}(SFRC) \quad (19)$$



429  
 430 Figure 15. Experimental vs predicted interfacial peak shear stress

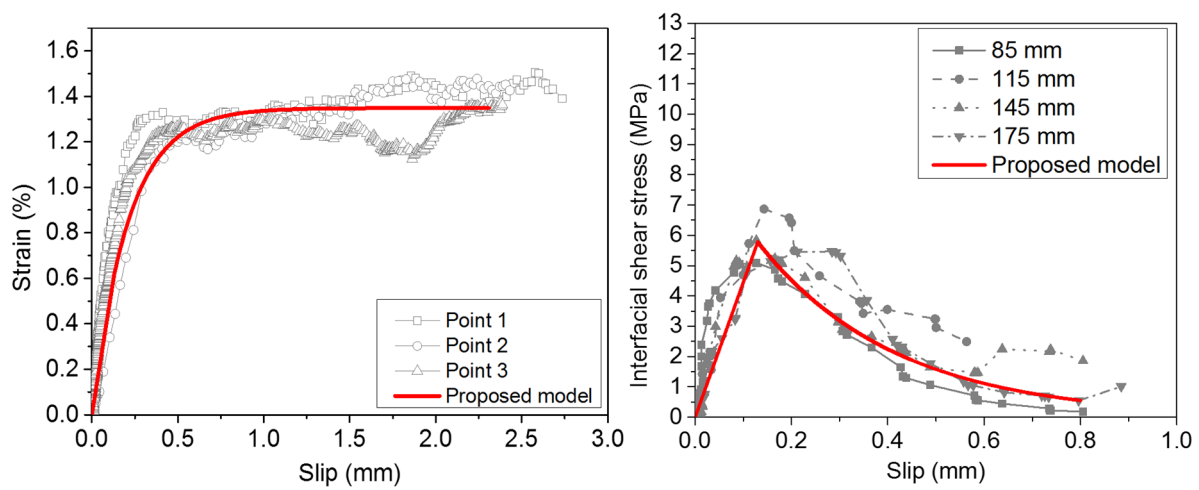
431 The maximum elastic slip  $s_l$  is the maximum slip corresponding to the elastic stage of the  
 432 bond-slip curves. The elastic slip is mainly resulted from the shear deformation within the  
 433 bonded region. The elastic slip slightly decreased with the increasing strain rate, but results  
 434 were less consistent and presented higher scatter. As a result, the elastic shear slip was set as  
 435 a constant of 0.13 mm for simplicity.

#### 436 4.5 Analysis and validation of the dynamic bond-slip model

437 Figure 16 shows the comparisons between the model predictions based on Equations  
 438 (7) to (19) and the directly measured experimental results for the strain-slip response and  
 439 bond-slip response. Based on the obtained parameters  $\tau_m$ ,  $s_l$ , and  $\omega$ , the predicted strain-slip



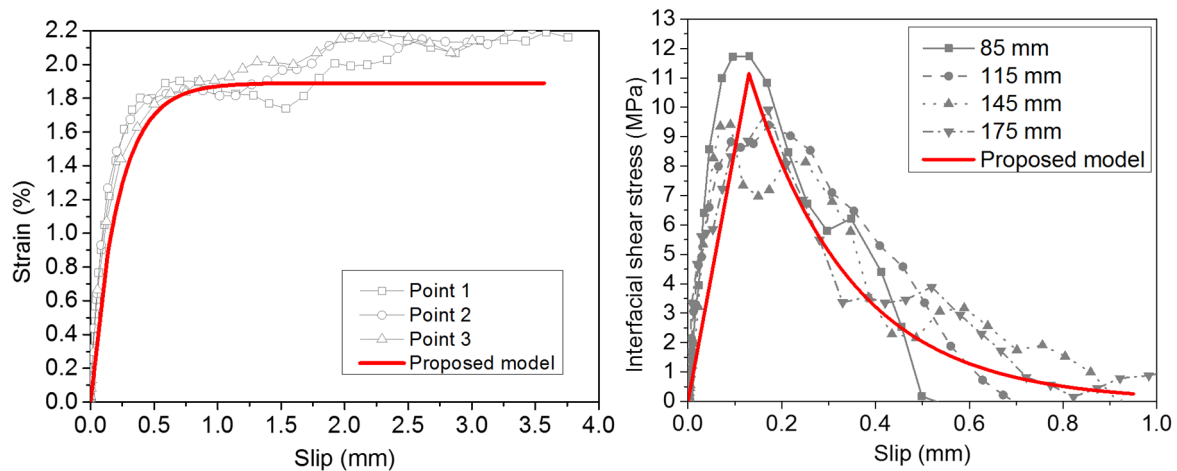
440 and bond-slip relationships are in good agreement with the test data. This comparison  
 441 demonstrates that the proposed bond-slip models can accurately predict the dynamic  
 442 interfacial bond-slip of BFRP-to-SFRC interface. Figure 17 illustrates the comparison  
 443 between the experimental and tested debonding load. The debonding load can be obtained by  
 444 a widely accepted formula  $P_u = b_f \sqrt{2E_f t_f G_f}$  [55] with the strain rate effect included in the  
 445 corresponding dynamic interfacial fracture energy. As shown the predictions agree well with  
 446 the test data, with a mean value of 1.013 and a *COV* of 0.08.



447

448 (a) Strain-slip response of D0.5-1-1

(b) Bond-slip response of D0.5-1-1

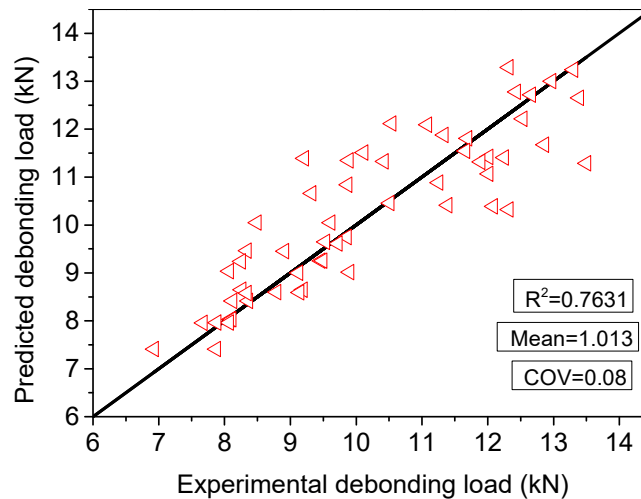


449

450 (c) Strain-slip response of D1.5-8-1

(d) Bond-slip response of D1.5-8-1

451 Figure 16. Comparisons of analytical predictions and tests data of strain-slip curve and  
 452 slip curve



453

454

Figure 17. Experimental vs predicted debonding load

## 455 5. Conclusions

456 This study investigated the dynamic interfacial bond behaviour of BFRP-to-SFRC interface.

457 The single-lap shear test method was used to evaluate the bond strength and bond-slip  
 458 relationships. The following conclusions can be drawn:

459 (1) Strain rate had a significant effect on the debonding failure modes. With the increasing  
 460 strain rate, the damage mode shifted the debonding area from concrete layer to the  
 461 concrete-epoxy interface. When the damage mode changed to concrete-epoxy interface,  
 462 adding steel fibres had only limited improvement on the debonding load.

463 (2) The addition of steel fibres increased the debonding load due to the improved  
 464 microcracking resistant capacity of SFRC substrate. Additionally, the strain rate had more  
 465 significant effect on the debonding load than the enhanced tensile strength of SFRC by  
 466 adding steel fibre.

467 (3) The addition of steel fibres resulted in higher IFE as the large fracture area dissipated  
 468 more fracture energy. In addition, the IFE increased with strain rate as the shear resistance  
 469 was enhanced under high loading rate.

470 (4) The addition of steel fibres resulted in higher interfacial shear stress due to the enhanced  
471 bond strength. In addition, strain rate had significant effect on the PSS as the ultimate  
472 debonding strain of BFRP increased with strain rate.

473 (5) The addition of steel fibres and strain rate had nearly no effect on the pattern of bond-slip  
474 relationship, i.e. ascending and descending branches, which were similar to the control  
475 specimen. However, the IFE increased with increase of steel fibres and the rising strain  
476 rate.

477 (6) Empirical bond-slip model was proposed by incorporating the strain rate effect. The  
478 proposed model gave good predictions of the experimental results.

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