

Citation

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1 **Experimental Investigation on Lightweight Rubberized Concrete Beams** 2 **Strengthened with BFRP Sheets Subjected to Impact Loads**

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4 **Abstract**

5 This study experimentally investigates the impact behaviour of rubberized concrete beams
6 strengthened with basalt fiber reinforced polymer (BFRP). Twelve reinforced concrete
7 beams, which consisted of different rubber contents (0%, 15%, and 30%), were tested under
8 impact loads. Various wrapping schemes were considered to determine the most effective
9 strengthening schemes for impact resistance performance of both the conventional and
10 rubberized concrete beams. The experimental results have shown that rubberized concrete
11 had 10-18% higher imparted energy per unit weight than that of normal concrete. The
12 rubberized concrete beams localized the damage at the impact area and slowed down the
13 stress wave velocity. Although rubberized concrete beams possessed lower compressive
14 strength (50.3 MPa, 25.4 MPa and 14.7 MPa for beams with 0%, 15% and 30% rubber
15 content, respectively), they yielded less displacement as compared to the reference beams
16 under the same impact velocity. The rubberized concrete beams experienced a lower peak
17 impact force. Meanwhile, the use of U-shape BFRP wraps concentrating at the impact area

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18 showed similar performance as those with BFRP wraps uniformly distributed along the entire
19 beam, therefore, this proposed strengthening scheme provides a cheaper solution for
20 strengthening concrete structures.

21 **Keywords:** Rubberized concrete; Fiber Reinforced Polymer (FRP); Impact loading; Energy
22 absorption; Impact resistance.

23 **Introduction**

24 Rubberized concrete has compositions, which are similar to conventional concrete except a
25 portion of normal aggregates is replaced by recycled rubber aggregates. There are many
26 studies on rubberized concrete and they proved its many advantages comparing to
27 conventional concrete, e.g., lightweight, green, and energy-absorption capacity [1-5]. When
28 considering a light-weight material, rubberized concrete mixed with chipped rubber has a
29 lower density than concrete mixed with crumb rubber and conventional concrete [6]. The
30 density of rubber is significantly lower than conventional coarse/fine aggregates and sand so
31 that more rubber content leads to more reduction in the self-weight of rubberized concrete.
32 According to Elchalakani [2], the density of the rubberized concrete reduced from 2450
33 kg/m^3 for 0% rubber content to 1950 kg/m^3 for 40% rubber content.

34 In addition, rubberized concrete showed excellent performance in resisting impact loads. The
35 excellent energy absorption of rubberized concrete was proven by previous studies [7, 8]. The
36 rubberized concrete with excellent characteristic of good energy dissipation capacity is
37 suitable for the applications when the energy dissipation capacity is of more importance than
38 strength, i.e. pedestrian blocks [9], rock-fall barriers [10-14] and roadside barriers [2, 7, 15].
39 It was reported that the roadside barriers made of rubberized concrete had good performance
40 and energy absorption capacity against impact loads [2, 7, 15]. It is noted that an innovative
41 design of a cushion layer can significantly improve the impact resistance [10-14]. For the
42 rock-fall barriers, studies on the impact-resistance behaviors of the RC barriers without
43 cushion layers have been conducted [13, 14] and the effect of cushioning on the barriers with
44 various cushion layers such as granular materials and gabion [10-12] has been also
45 investigated. It was reported that using cushion layers placed in front of the barrier is
46 effective in attenuating impact force, reducing transmitted loads to the barrier and dissipating

47 impact energy from boulder impacts. The effectiveness of mitigation can be quantified by the
48 cushioning efficiency i.e. load-reduction factor. The impact forces and transmitted loads to
49 the barrier can be reduced by 25% and 50%, respectively when using cushion layer [11]. The
50 inertial resistance of the barrier also contributes to its impact resistance. Meanwhile, the
51 quasi-static mechanical properties and structural performance of rubberized concrete are
52 relatively better understood than their dynamic counterparts. Many studies have been
53 conducted on the quasi-static properties of rubberized concrete [16]. However, very limited
54 studies have been conducted on the dynamic properties of rubberized concrete [17]. Pham et
55 al. [18] experimentally investigated the lateral impact performance of the columns made of
56 rubberized concrete. The findings from that study have shown that the energy absorption
57 capacity of the column increased significantly by using rubberized concrete under impact
58 loading. For instance, the impact energy absorption capacity of the column was increased by
59 58% and 63% when the rubber content increased from 0% to 15% and 30%, respectively.
60 The rubberized concrete columns experienced nearly double displacements than the reference
61 column prior to failure. The displacement response is even larger when they were confined
62 with basalt fiber-reinforced polymer (BFRP).

63 The rubberized concrete was tested by using different axial impact rigs to study its energy
64 absorption capacity. Gupta et al. [19] reported the impact resistance capacity of rubberized
65 concrete with 25% rubber fiber replaced by using drop-weight rig. It was reported that the
66 energy absorption improved considerably with the increase of rubber content. Donga et al.
67 [20] also carried out tests on rubberized concrete to examine its impact resistance and
68 reported that the impact resistance capacity of concrete can be increased by up to 60%
69 through adding rubber. Atahan and Yücel [21] carried out impact tests by using Instron
70 machine. This machine can monitor energy absorption, impact velocity, and impact force.
71 The testing results exhibited that the rubberized concrete can effectively reduce peak impact

72 forces and increase impact duration. Moreover, Liu et al. [17] conducted SHPB test on
73 rubberized concrete to examine its dynamic properties . It was found that rubberized concrete
74 had lower increment of dynamic increase factor (DIF) of strength as compared to traditional
75 concrete. With the higher rubber content (within 10%), the rubberized concrete exhibited the
76 increased energy absorption capability. However, when the rubber content is over 10%, the
77 rubberized concrete showed decreasing energy absorption capacity with the increase of
78 rubber replacement.

79 To further examine the impact performance of rubberized concrete, experimental tests were
80 carried out on a structural scale, i.e. Sukontasukkul et al. [22] proposed a cushion layer made
81 of rubberized concrete, which can be used for the bulletproof panels. The panels consist of
82 two layers i.e. soft rubberized concrete layer and steel fiber reinforced concrete layer. The
83 softer layer worked as a sacrificed layer in protective structures and less impact energy is
84 transferred to the harder layer. Atahan and Sevim [7] carried out impact tests on full-scaled
85 rubberized concrete roadside barriers by using a real vehicle with a 500 kg total mass. It was
86 also reported that the concrete with higher rubber content had higher energy absorption
87 capacity. Additionally, the acceleration and impact force induced in an impact event can be
88 significantly reduced owing to the hardness of rubberized concrete, which can mitigate injury
89 risk. Pham et al. [18] found that rubberized concrete columns could be used to effectively
90 minimize the peak impact force up to 40% for tested specimens with 30% rubber content
91 after comparing with the reference concrete specimen. In the latter study, the columns made
92 of rubberized concrete with different rubber contents were subjected to lateral impact loads.
93 Pham et al. [23] also conducted axial tests on rubberized concrete by using instrumented
94 drop-weight impact test apparatus. The main concern of that study was the impact energy
95 absorption and the impact force. The authors also found that the peak impact force can be
96 mitigated up to 50% and the impact duration can be considerably extended by using

97 rubberized concrete. As a result, they recommended that the possible use of rubberized
98 concrete for roadside barriers might reduce injury risk to drivers and passengers of the
99 colliding vehicle.

100 As can be seen from the above review, the vast majority of previous studies on rubberized
101 concrete focused on the material scale with only a few studies that investigated the
102 performance of beams and columns made of rubberized concrete having been reported. None
103 study has been carried out to investigate the flexural behavior of rubberized concrete beams
104 against impact loads. Therefore, the impact behavior of rubberized concrete beams is
105 investigated in this study by using the drop-weight tests. It is noted that rubberized concrete
106 provides high-energy absorption capability but it has lower strength as compared to normal
107 concrete. Accordingly, these rubberized concrete beams were strengthened by using fiber-
108 reinforced polymer (FRP) to enhance their load-carrying capacity for better design of beams
109 to reduce impact force through drop-weight and beam interaction, enhance energy absorption
110 capacity, and possess sufficient load-carrying capacities.

111 **Impact mechanism of concrete beams under impact loads**

112 Since the impact behaviour of rubberized concrete beams has not been investigated and
113 reported in the literature, the impact behaviour of normal concrete beams is reviewed instead
114 to provide a general view of its dynamic response. There were a few studies on the
115 performance of reinforced concrete (RC) beams or FRP strengthened RC beams under impact
116 loads [24-30]. The behaviour of RC beams under impact loads was completely different from
117 that under static loads. The different behavior of RC beams under impact loads can be
118 explained by two phenomena, namely the localized/global responses of the beams and shear-
119 dominant failure mechanism. The localized/global response causes differences in the negative

120 bending moment and reaction force while the shear-dominant mechanism relates to the
121 inertial resistance of the beams.

122 Under static loading, a simply supported RC beam subjected to three-points bending shows
123 positive moment at midspan and the whole beam contributes to resist the applied load.
124 However, a simply supported RC beam under dynamic loading experiences positive bending
125 moment at the midspan and negative bending moment close to the supports [28, 31, 32]. The
126 beam also experiences negative reaction forces at the supports, which definitely do not appear
127 under static loads. The existence of negative bending moment and reaction forces was
128 discussed in the previous studies [28, 31, 32]. The negative reaction forces were observed in
129 all the simply supported beams under impact tests in the previous study [28]. Pham and Hao
130 [28] reported this interesting phenomenon, which was also confirmed by other studies [33,
131 34], and explained this phenomenon by the stress wave theory. The authors mentioned that
132 the stress wave propagations caused this phenomenon. Therefore it is a stress wave
133 propagation problem rather than a structural mechanics or a structural dynamics problem.
134 The surface Rayleigh wave, which accounts for 67% impact energy, may cause this
135 phenomenon. Meanwhile, the negative bending moment in the simply supported beams under
136 impact loads was observed experimentally in the tests and numerically simulated in the
137 previous study by Pham et al. [35]. The experimental tests clearly showed some vertical
138 cracks on top of the beam at the negative bending moment region. Accordingly, similar
139 damage and cracks at the negative bending moment region were seen in the numerical
140 simulation. The authors explained the formation of the negative bending moment was caused
141 by the local response of the beam. When a simply supported beam is impacted by a projectile,
142 only a portion at the midspan of the beam responds [35, 36] during the early stage of the
143 impact. The two beam ends and boundary conditions do not affect the responses at the initial
144 stage of the impact. Accordingly, the negative bending moment only occurs in a relatively

145 long beam while short beams do not show this phenomenon as clarified in the previous study
146 by Pham and Hao [32].

147 Unlike static behaviour, the impact behaviour of RC beams includes two phases including the
148 impact loading phase and the free-vibration phase. In the impact loading phase, which
149 happens in a very short period of about a few milliseconds, the impact force at the impact
150 point quickly reaches to the peak value associated with localized damage at the impact area
151 and inclined shear cracks. The beams may fail with shear dominant failure mechanism even
152 though they would have failed in a flexural mode and a ductile manner under static loads. For
153 instance, Pham et al. [35] tested two identical RC beams, in which Beam 1 failed with a pure
154 flexural manner under static load with only vertical cracks and Beam 2 was damaged with a
155 mixed shear-flexure mode when subjected to impact load. It is noted that the two tested
156 beams were designed to have the shear capacity four times the flexural capacity so that it
157 would experience pure flexural failure as also observed in the static tests. Interestingly, the
158 shear failure was observed for the beam under impact loads. This phenomenon was identified
159 as the shear-dominant mechanism of RC beams under impact loads as mentioned in the
160 previous studies [28, 37]. The previous studies also examined and explained the shear
161 mechanism of structures subjected impact loads, which is the most common failure mode
162 [37-39].

163 In general, the impact behaviour is governed by many parameters in which the peak impact
164 force plays an essential role as shown in the previous study by Do et al. [40]. The authors
165 demonstrated that under vehicle-column collision, the peak impact force might change the
166 column failure mode even though the impact force time histories of various scenarios are
167 almost similar (except the peak impact force). The impact force is influenced by the contact
168 stiffness between the projectile and the beam at which the hardness and modulus of the

169 material and contact quality are critical parameters as discussed in the previous study by
170 Pham et al. [35]. The rubberized concrete has lower modulus so that it results in lower peak
171 impact force under similar impact energy [23]. Accordingly, the inertia resistance will be
172 lower and thus the impact behaviour of the rubberized concrete is distinguished from that of
173 normal concrete. These variations are experimentally investigated in this study.

174 **Experimental program**

175 *Specimen design and material properties*

176 Twelve rubberized reinforced concrete (RuC) beams were cast and they had dimension of
177 2200 mm in length by 250 mm in height by 150 mm in width. These beams included 6
178 reference beams without rubber, 3 beams with 15% rubber content, and 3 beams with 30%
179 rubber content (Table 1). Among these beams, nine beams were wrapped with different
180 schemes as shown in Fig. 1. The beams (B_{xy_zm}) are labelled based on their rubber contents,
181 strengthening scheme, and drop height. For example, Beam B15A_2m means this beam was
182 made of 15% rubberized concrete, strengthened with scheme A, and tested under 2 m drop
183 height. The rubber content indicates the amount of rubber aggregates used to replace 15% or
184 30% of the total volume of the aggregate. N10 and N12 steel rebars were used as longitudinal
185 reinforcements with a length of 2160 mm. Steel stirrups had a dimension of 10 mm in
186 diameter and a spacing of 115 mm.

187 The rubber aggregates included crumb rubber (7-10 mm) and chip rubber (2-5 mm), which
188 was pre-treated by 10% of NaOH solution. This is a crucial procedure as it significantly
189 improves the bonding between rubber aggregates and the cement matrix. The treatment
190 process was carried out as follows: (1) thoroughly washed the rubber aggregates to remove
191 all the impurities and dust which might weaken the bonding strength between rubber
192 aggregates and the cement matrix, (2) prepared 10% of NaOH aqueous solution and used it to

193 soak rubber particles for a minimum duration of 24 hours, (3) drained the NaOH solution and
194 the rubber aggregates were rinsed with water to achieve a pH of 7, (4) dried the rubber
195 aggregates under the sun before the actual use.

196 The unidirectional BFRP sheets used in this experiment had the dimensions of 100 mm in
197 width and 0.12 mm in thickness and a density of 300 g/m². It has the properties of 2100 MPa
198 in tensile strength, 77.9 GPa in elastic modulus, and 2.1% in tensile elongation as reported in
199 the previous study [41]. Prior to bonding BFRP, surface preparation was carefully conducted
200 by removing weak concrete. Air gun was used to blow the concrete surface and remove all
201 dust and weak concrete. More details about the surface preparation can be found in previous
202 studies [28, 29]. Epoxy resin including two parts with a mixing ratio at 5:1 was used [42].
203 The tensile strength, modulus, and elongation of the epoxy resin were 54 MPa, 2.8 GPa, and
204 3.4%, respectively. These beams are divided into three groups based on their BFRP bonding
205 schemes. The first group will be the reference beams with no BFRP strengthening. The
206 second group will have beams with four longitudinal BFRP strips as illustrated in design A in
207 Figure 1, while the third group will have beams with four longitudinal BFRP strips and one
208 45° inclined U-shape wraps as shown in design B in Figure 1. The classification of each
209 beam specimen and their respective tests are summarized into the test matrix as shown in
210 Table 1. Strain gauges (SG) were bonded to BFRP wraps to monitor their strain in the
211 longitudinal and transverse directions. There were two SGs on the longitudinal BFRP sheets
212 including one at the midspan and another one offset 250 mm from the beam end. Another
213 strain gauge was attached to the middle of the 45° inclined U-shaped layer close to the
214 midspan.

215 ***Impact Testing Procedure***

216 All the beams were tested under 2 m drop height for the first drop. If the beams did not fail,
217 they were tested again under 2.5 m and then repeated until failure. An instrumented drop-
218 weight test system, which releases a weight from a designated height onto the midspan of the
219 beams, was used for all the impact tests as shown in Fig. 2. The drop weight weighs 208.8 kg.
220 The shape of the impactor had a smooth spherical bottom (50 mm radius). The impactor
221 vertically drops to specimens by using a plastic tube. The boundary condition was carefully
222 designed to achieve the simply supported beams, in which the supports were restrained in the
223 vertical direction to prevent rebounding of the beams. Two upper and lower load cells with
224 the capacity of 25 ton each were fixed to two sides of the beam supports as shown in Fig. 3,
225 which were used to record the positive and negative reaction forces. The effective span of
226 these beams was 1900 mm, which was created by steel rollers. A steel load adaptor (100 x
227 100 x 20 mm) was fixed on the top surface of the beams at the centre and the impact load
228 cell (180 ton) was bolted to the load adaptor. A high-speed camera was used to monitor the
229 failure processes of these beams and it was set as 20,000 frames per second. The data
230 acquisition system was utilized to record the signals of the FRP sheets and load cells from
231 strain gauges. The sampling rate of data acquisition system was set as 100 kHz. Signals of the
232 impact forces were filtered by FFT low-pass with a cutoff frequency of 10 Hz.

233 **Experimental results and discussions**

234 *Crack development and failure modes*

235 All the beams were tested under a drop height of 2 m for the first hit. The drop height
236 increased to 2.5 m for the second hit if the beam did not fail under the first impact. Damage at
237 the impact area is larger than the load distributor and this is similar to the damage of the front
238 face of a concrete panel subjected to projectile impact [43]. The longitudinal compressive
239 stress waves generated by the impact spherically propagated into the beams. The spalling of

240 concrete at the two sides of the beam, close to the impact area, was observed as shown in Fig.
241 4. The spalled concrete debris was still intact after failure. The tensile spalling of concrete at
242 the two sides of the beams was also reported in previous studies [28, 29]. When the stress
243 wave arrived at the free surface of the beams at the side, it was reflected as a tensile stress
244 wave. The original compressive stress wave interacted with the reflected tensile stress wave
245 resulted in a decreasing compressive wave but increasing tensile wave amplitude. The
246 increasing tensile stress wave might exceed the dynamic tensile strength of concrete, which
247 might generate cracks in the beam as shown in Fig. 5. The tensile stress wave propagated to
248 the free surfaces of the beams and reflected back as a compressive stress wave. This process
249 was repeated and might have caused further damage to the beams until the resultant stress
250 waves were lower than the dynamic tensile strength of concrete.

251 Failure modes were associated with the shear dominant mechanism as can be seen from the
252 shear plug at the impact area, in which the shear plug indicates a trapezium concrete region
253 underneath the impact point. The reference beam without rubber content showed distributed
254 flexural and shear crack along the beam axis. Meanwhile, the rubberized concrete beams
255 showed more localized damage because of the shear dominant mechanism under impact tests,
256 which was explained clearly in previous studies [28, 37]. The shear resistance of the beams
257 becomes more critical under impact tests at which the rubberized concrete beams had much
258 lower shear resistance so that they failed in a shear-govern mechanism. This phenomenon
259 was clearly observed in beam B30_2m at which cracks only appeared within the shear plug
260 under the impact area. The BFRP strengthened beams showed similar crack map regarding
261 the corresponding unstrengthened specimens with a combination of flexural and shear cracks.
262 However, BFRP sheets prevented crack development in the strengthened beams so that they
263 failed under higher impact energy with rupture of the longitudinal BFRP sheets and partial
264 debonding of vertical/inclined U-shaped BFRP strips as shown in Fig. 5.

265 In addition, the flexural cracks induced by negative bending moments were observed in these
266 tests as shown in Fig. 5. Under static tests, it is obvious that the simply-supported beam under
267 point load only generates positive bending moment along the beam. However, a simply
268 supported beam may induce a negative bending moment on the beam top close to the
269 supports. The formation of the negative bending moment was reported and discussed in the
270 previous studies [31, 32, 34]. This negative bending moment caused flexural cracks in the
271 upper surface as shown in Fig. 5. The cracks at the negative bending moment area were
272 caused by the inertial resistance of the beams. The higher impact velocity leads to high
273 acceleration of the beams and thus causes higher inertia resistance, which leads to a higher
274 negative bending moment and thus more cracks at the negative bending area. This
275 phenomenon is shown in Fig. 5 where the beams under 2.5 m drops yielded more cracks at
276 the negative bending moment area. This observation again confirmed the existence of the
277 negative bending moment and its consequences so that it needs to be taken into consideration
278 when designing concrete beams against impact loads.

279 *Dynamic response*

280 The impact response of the tested beams included two continuous stages, which are the
281 impact force transient phase and the free vibration phase. The impact force phase occurred in
282 about 10 ms in which the peak impact force last for approximately 1 ms while the reaction
283 force last much longer up to 10 ms. Afterward, the beams exhibited a free vibration phase in
284 which the beams freely vibrated and damped after more than 100 ms. The time histories of
285 the impact force and midspan displacement are presented and discussed in the following
286 sections. The time histories of the impact force and the reaction force of the unstrengthened
287 beams are shown in Fig. 6. The use of rubberized concrete reduced the peak impact forces
288 and reaction force. Unfortunately, the impact force time histories of Beam B30_2m was not

289 recorded due to a malfunction in the data acquisition system. When the rubber content
290 increased, the reduction of the impact forces and reaction forces under the same impact
291 energy was observed as shown in Fig. 7. The maximum impact forces of Beams B0A_2m
292 and B30A_2m were 1800 kN and 1500 kN, respectively. The maximum reaction forces of
293 these two beams were 52 kN and 40 kN, respectively. These figures clearly demonstrate that
294 using rubberized concrete can considerably reduce the impact forces and reaction forces in
295 the beams. The reduction of the impact forces was also observed for other BFRP
296 strengthened rubberized concrete beams as compared to the conventional concrete beams.
297 Meanwhile, the duration of the peak impact forces of the rubberized concrete beams was
298 longer than that of the conventional concrete beams, for example the duration of the peak
299 impact forces of Beam B0A_2m and B30A_2m was 0.6 ms and 1 ms, respectively.

300 In the meantime, another unique phenomenon associated with the impact behaviour of a
301 simply supported beam, which is the existence of the negative reaction force earlier than the
302 positive one, was also observed in the tests as shown in Figs. 6-8. This phenomenon was
303 reported in previous studies [28, 33, 34]. Pham and Hao [32] attempted to explain this
304 interesting phenomenon by using the theory of stress wave propagation. Upon an impact
305 event on a solid surface, P-wave, shear wave and surface Rayleigh wave dissipated 7%, 26%
306 and 67% of the impact energy, respectively [44]. Both the P-wave and shear wave propagate
307 faster than Rayleigh wave and diminish at a faster rate because the former ones have higher-
308 frequency contents. In these concrete beams, P-wave arrives the supports first and then shear
309 wave while Rayleigh wave comes last. Shear wave and P-wave cause the longitudinal and
310 transverse vibrations of the beam, respectively. Since vibrations in the horizontal directions,
311 caused by both P-wave and shear wave, do not generate vertical loads so that these two
312 waves cannot be monitored by the load cells fixed in the vertical direction. Therefore, the
313 reaction force in the negative direction was likely caused by the arrival of Rayleigh wave. All

314 the beams in this study showed the magnitude of the negative reaction force was about a half
315 the corresponding positive ones (20-25 kN vs 40-50 kN).

316 Additionally, the time histories of displacement are traced from the high-speed camera videos
317 and shown in Fig. 9. It is interesting that the displacement of Beams B15 and B30 was lower
318 than that of conventional concrete beam B0, the rubberized concrete beams deformed slightly
319 less (43.5 mm vs 45.5 mm, 4.4% reduction) than that of the reference beam under impact
320 loads. Meanwhile, the displacement at maximum static loads can be reasonably estimated by
321 using the software Response 2000 [45], such as the displacement at maximum static loads of
322 Beams B0, B15 and B30 is 16.8 mm, 19.2 mm, and 21.6 mm, which shows an increase of
323 14.3% and 28.6%, respectively. This observation demonstrates that the rubberized concrete
324 beams possess an excellent performance under impact loads. In addition, the maximum
325 displacement of Beam B30 was slightly higher (44.5 mm vs 43.5 mm) than that of Beam B15
326 so that it suggests that the optimized rubber content is close to 15%. This observation is valid
327 for all other strengthening schemes since the beams with 15% rubber content always showed
328 lower maximum displacement as compared to other corresponding beams as shown in Fig. 9.
329 In addition, replacing normal aggregates by rubber aggregates did not considerably change
330 the vibration characteristics of the beams. Fig. 9 shows that the natural vibration period of
331 Beams B0, B15 and B30 was 24.9, 24.2, and 23.6 ms, respectively. To verify the measured
332 natural vibration period, the predicted natural vibration period was estimated based on the
333 material properties and the beams' dimensions. The mix design of the rubberized concrete in
334 this studies was adopted from the previous studies [6, 18]. The Young's modulus of RuC
335 with the rubber contents of 15% and 30% were estimated as 19 GPa and 15 GPa, respectively
336 [2]. The natural circular frequency of the beams is estimated as follows [46]:

$$337 \quad \omega = \sqrt{\frac{k}{m^*}} \quad (1)$$

338 where k and m^* are respectively the stiffness and effective mass of the beam, taken as
339 $0.493m$. It is noted that m is the mass of the beam within the effective length, L_e , and k is
340 estimated as follows:

$$341 \quad k = \frac{48EI}{L_e^3} \quad (2)$$

342 where E is the elastic modulus and I is the moment of inertia of the beam which considers
343 cracked section. The natural period of vibration T is estimated as follows:

$$344 \quad T = \frac{2\pi}{\omega} \quad (3)$$

345 In the impact force transient phase, only a portion of the beam responds to the impact.
346 However, the entire beam vibrates to the impact in the free vibration stage. Therefore, the
347 effective length is considered as the whole length in this analysis. For an approximation, the
348 moment of inertia of RC beams associated with a cracked section is about 35% of the
349 uncracked section [47]. The estimated natural period of vibration of the beams with 15% and
350 30% rubber content is 19 ms and 21 ms, respectively. The measured period of vibration of
351 these beams was 24.2 and 23.36 ms, respectively. This variation is reasonable since the
352 modulus and the stiffness of the crack section was approximately estimated for the rubberized
353 concrete beams. This verification indicates the reliability of the testing results. Meanwhile,
354 from the displacement time histories of all the tested beams, it can be seen that the damping
355 ratio of the strengthened beam was much higher than that of the unstrengthened beams. The
356 vibration of the first ones vanished after only one or two cycles while the later ones damped
357 after more than 4 cycles.

358 ***Time lag and stress wave velocity***

359 The impact force time histories from the tested beams show that there was a delay in the
360 arrival time between the impact force at the midspan and the reaction force at the supports,

361 called time lag. It might be estimated from the initiation of the impact force as well as the
362 reaction force [28], which is affected by the stress wave velocity. The time lag between
363 impact and reaction forces of the tested beam shown in Fig. 10 indicates the time lag was
364 affected by the rubber content and damage of concrete. Under the first impact of 2 m, there
365 were no existing cracks in these beams. The time lag for beams with 0%, 15%, and 30%
366 rubber content was 0.52 ms, 0.55 ms, and 0.70 ms, respectively. This time lag is related to the
367 required time for stress waves propagate from the impact point at midspan toward the two
368 supports. In this study, the stress wave velocity of these beams was 1827 m/s, 1727 m/s, and
369 1357 m/s, respectively. It is evident that increasing the rubber content from 0% to 15% only
370 slightly reduced the stress wave velocity by 5% while increasing the rubber content to 30%
371 significantly decreased the stress wave velocity by 26%. These stress wave velocities can be
372 theoretically estimated from the velocity of P-wave ($c=\sqrt{E/\rho}$), which are 3290 m/s, 2887
373 m/s, and 2630 m/s. From both the measured and estimated values, the stress wave velocity
374 decreases with an increase of the rubber replacement. However, the measured stress wave
375 velocity was almost half of the estimated ones. These variations were stated in previous
376 studies [28, 34, 48]. Pham and Hao [32] suggested that the measured stress wave from the
377 impact point toward the boundaries, which is located on the surface of the beams, should be
378 the velocity of R-wave as discussed previously. Rhazi et al. [44] reported the velocity of R-
379 wave in concrete is approximately 2100-2500 m/s. The theoretical value of R-wave velocity
380 is still slightly higher than the measured velocity. The reason for this difference was clarified
381 in the previous study [28], i.e. the load cells and steel plates in the test setup make the actual
382 travel distance of the stress wave greater than 0.95 m. The actual stress wave velocity in the
383 concrete should be higher than the measured values but it is close to the theoretical value for
384 R-wave.

385 In addition, Fig. 10 also shows the time lag of the tested beams under different drop heights.
386 If a beam survives under 2m-drop, it was tested again under 2.5m-drop. As a result, these
387 beams had some pre-cracks before being tested under 2.5 m. Concrete in these pre-cracked
388 beams obviously had a lower modulus and thus lower stress wave velocity. The measured
389 time lag of the beams with 0%, 15% and 30% rubber content under second impact was 0.82
390 ms, 0.86 ms, and 1.00 ms, respectively. These values correspond to the wave velocity of 1158
391 m/s, 1104 m/s, and 950 m/s, respectively. Repeatedly, the stress wave velocity reduces with
392 an increase in the damage to the tested beams. The level of reduction was also dependent on
393 the rubber contents. However, increasing the rubber content from 0% to 15% only leads to a
394 minor change (<5%) in the stress wave velocity while the stress wave velocity in beams with
395 30% rubber showed a reduction of 18% in the second drop, less than the 26% reduction
396 during the first drop, compared to the reference beam.

397 *Effectiveness of longitudinal and U-wrap BFRP*

398 The rubberized concrete beams reduced the peak impact forces and had more pronounced
399 localized damage at the impact area as shown in Fig. 5. To improve the load carrying
400 capacity of these beams, longitudinal and transverse BFRP strips were used. As shown in
401 Table 2 and Fig. 9, the use of BFRP strengthening significantly reduced both the maximum
402 and residual displacements. For example, the maximum and residual displacements of Beam
403 B0_2m were 45.6 mm and 32.9 mm. These values for beams B0A_2m and B0B_2m were
404 33.4 mm, 33.4 mm, 16.1 mm, and 12.2 mm, respectively. The use of BFRP strengthening
405 reduced the maximum and residual displacement approximately by 27% and 56%,
406 respectively. As expected, strengthening scheme B with the combination of longitudinal
407 BFRP sheets and transverse BFRP sheets yielded better results. The effectiveness of using
408 BFRP strengthening for the rubberized concrete beams was similar to that of the conventional

409 concrete beams as given in Table 2. Therefore, it can be concluded that the BFRP
410 strengthening efficiency was similar for both conventional and rubberized concrete beams.

411 Even though the use of BFRP strengthening greatly reduced the displacement of the beams, it
412 exhibited a minor effect on the maximum impact force and impact force duration as given in
413 Table 2. An increase of about 10% was observed in the maximum impact force when
414 comparing the peak impact force of the strengthened beams with the corresponding
415 unstrengthened ones. Meanwhile, the substantial reduction in the maximum and residual
416 displacement of the strengthened beams indicated that these beams had higher global stiffness
417 than the unstrengthened beams. This phenomenon shows that the increase in the global
418 stiffness marginally affected the impact force. This observation was theoretically and
419 numerically explained in the previous study by Pham and Hao [36], which concluded that the
420 local stiffness governs the peak impact force while the global stiffness controls the maximum
421 displacement.

422 As mentioned previously that the shear dominant mechanism affects the impact force and the
423 dynamic resistance capacity of the tested beams. Therefore, using U-shape BFRP strips to
424 locally improve the shear resistance capacity at the impact region may be a good design
425 rather than uniformly distributing the U-shape BFRP strips along the beams. Fig. 11 shows
426 the impact force time histories of the four beams with 0% rubber content and different
427 strengthening schemes (A, B, C, and D). Beam B0A_2m exhibited the lowest maximum
428 reaction force (51.7 kN) while the corresponding values of Beams B0B_2m, B0C_2m, and
429 B0D_2m were 60.3 kN, 66.8 kN, 55.3 kN, respectively. In terms of reaction forces, these
430 beams with U-shape BFRP strips showed higher reaction forces to that of Beam B0A_2m,
431 which only had longitudinal BFRP strips. As can be seen from Fig. 11, Beam B0C_2m which
432 had only a half number of U-shape BFRP strips compared to that of Beam B0B_2m but the
433 former one even shows slightly higher impact force and reaction force. However, this

434 difference is minor and can be considered as variation in testing. From this observation, it can
435 be concluded that locally strengthening a beam in shear with U-shape BFRP yields similar
436 impact resistance as beams which had uniformly distributed U-shape BFRP strips. This
437 phenomenon is different from the static case when the beam with uniformly distributed BFRP
438 U-shape wraps resisted higher loads and deformed at a much higher displacement as reported
439 by Chen et al. [41]. To further investigate the impact response of these beams, the
440 displacement time histories of these beams are shown in Fig. 12. It is seen that the
441 displacement time history of Beam C is similar to Beams B and D. The maximum and
442 residual displacements of these beams were in the range of 31-33 mm and 11-16 mm,
443 respectively. This observation suggests that strengthening beams at the impact region by
444 using vertical wraps is very effective and can provide a cost-saving solution.

445 *Imparted Energy*

446 The impact energy is reversed back into the rebound in an ideally elastic impact while a
447 portion of the impact energy is imparted in elastic deformation and another part of the impact
448 energy is consumed in the plastic deformation and failure in real impacts [49]. The energy-
449 balanced method can be used to equate the input kinetic energy and the component energies
450 in a beam. The energy-balanced equation can be expressed as follows:

$$451 \quad \frac{1}{2} M (V_1^2 - V_2^2) = E_b + E_s + E_m + E_c + E_k \quad (4)$$

452 where M is the projectile weight, V_1 and V_2 are the initial impact velocity and residual
453 velocity of the projectile, respectively, E_b , E_m , E_s , E_c represent the energy in the form of
454 bending deformation, membrane component, shear deformation, and indentation effect when
455 the projectile rebounds from the beam, respectively, and E_k is the kinetic energy of the beam.
456 After separating from the projectile, the beam further deforms and reaches its maximum

457 displacement when the kinetic energy in the beam equals zero. From the energy conservation
458 law, the energies in the beam can be equated as follows:

$$459 \quad \frac{1}{2}M(V_1^2 - V_2^2) = E_b^* + E_s^* + E_m^* + E_c \quad (5)$$

460 where E_s^* , E_b^* , and E_m^* are energies representing the shear deformation, bending
461 deformation, and membrane component when the beam reaches the maximum displacement,
462 respectively. It is noted that the energy caused the local indentation does not change and the
463 kinetic energy of the beam vanishes at the maximum displacement. Since the stretching effect
464 is small and can be ignored in the beam behavior, the energy for the membrane effect can be
465 excluded [50].

466 The energy-balanced method was discussed and adopted to predict the impact response and
467 impact forces in previous studies [50-54]. Predictions from the proposed models in these
468 studies matched the experimental results quite well. The models were derived based on two
469 assumptions, which need to be carefully justified. Firstly, structures were assumed to behave
470 in a quasi-static manner, at which the structures reach their maximum displacement when the
471 beam velocity becomes zero [51, 53]. Secondly, the energies are derived based on the load-
472 displacement under quasi-static loads [50, 54]. Zhou and Stronge [54] recommended their
473 model was based on the static behavior, thus, it is only meaningful in the case of a heavy
474 projectile impacting a light plate. The two assumptions are not necessarily correct in the
475 impact tests in this study. In all the impact force time histories in this study, the impact forces
476 ceased at about 1-2 ms while the beams reached the maximum displacements at
477 approximately 20 ms. As a result, the separation between the projectile and the beam
478 occurred before the beams reached the maximum displacement. In addition, estimating the
479 energies by using the bending and shear stiffness of the beams usually adopts the global
480 stiffness for the whole impact duration. However, it has been proven in previous studies that

481 only a portion of a beam reacts to the impact force in the force phase (for the case of impact
482 tests on concrete beams) and the effective span of the beam is shorter than its actual span [31,
483 32, 34, 36, 48, 55]. This observation is because the beam locally responds to the impact loads,
484 instead of globally deforms as in a static case. In the previous study, Abrate [51] concluded
485 that using the energy absorption from the assumption of a static case is inappropriate in this
486 case because the impact force vanishes when the beam deflection has not reached its
487 maximum value. To distinguish whether the local response or global response governs the
488 beam behavior, the ratio between the impact loading duration, t_d , and the structural vibration
489 period, T , was used.

490 There is an alternative way to quantify the energy imparted into the beams by using the
491 variation of the kinetic energy of the projectile as presented in Eqs. 4-5. The imparted energy
492 of the tested beams is given in Table 2. For unstrengthened beams, the imparted energy of the
493 rubberized concrete beams was slightly less than that of the reference beams with a reduction
494 of 1.9% and 8.1% for Beams B15_2m and B30_2m, respectively. However, these beams
495 have different masses so that it is more useful if the imparted energy per unit weight is
496 examined (Table 2). The imparted impact energy per unit weight of the rubberized concrete
497 was significantly higher than that of the reference beam (B0_2m) with an increase of 10.3% and
498 17.8% for Beams B15_2m and B30_2m, respectively. Meanwhile, strengthening the beams
499 with BFRP sheets did not increase the energy imparted to the beams as shown in Fig. 13.
500 Meanwhile, when higher impact energy is applied to the beams, more impact energy
501 imparted to the beams. Strengthening schemes A and B did not show a difference in the
502 imparted energy in the conventional concrete beams. However, strengthening scheme B
503 clearly show higher imparted energy than that of strengthening scheme A for the rubberized
504 concrete beams, particularly under 2.5-m drops. In general, the imparted energy of the
505 strengthened rubberized concrete beams was almost similar to the corresponding

506 conventional concrete beams under 2 m drops but they exhibited higher imparted energy than
507 the reference beams under 2.5 m drops.

508 **Strain and failure of BFRP**

509 BFRP strain in the longitudinal direction at the midspan was measured by strain gauges and
510 plotted in Figs. 14-15. Fig. 14 shows BFRP strain of the tested beams under 2 m drop, in
511 which the maximum BFRP strain was about 1% which was comparable to the results under
512 static tests reported in previous studies [56, 57]. BFRP strain quickly increased to the peak
513 values and then reduced to the plateau value of 0.5-0.6% for all the beams, except for Beam
514 B30B_2m. Unfortunately, BFRP strain of some beams was lost due to a malfunction in the
515 data acquisition system. All the beams did not show debonding of longitudinal BFRP sheets
516 under 2 m drops. These beams were then tested and failed under 2.5 m drop height. The
517 beams strengthened with scheme A failed by intermediate crack induced debonding of the
518 bottom BFRP sheets close to the midspan and then propagated toward the supports. The two
519 major shear cracks under the impact region developed at a very early stage and initiated the
520 debonding. Meanwhile, the rupture of BFRP sheets lead to failure of the strengthened beams
521 with scheme B (Fig. 16). As a result, the maximum BFRP strain of beams type B was greater
522 than that of beams type A, for instance, the maximum BFRP strain of Beams B15B_2.5m and
523 B30B_2.5m was 0.6% and 0.65%, respectively, while the corresponding numbers of Beams
524 B15A_2.5m and B30A_2.5m were 0.46% and 0.45%, respectively (Fig. 15). It is worth
525 mentioning that the BFRP strain under the second impact of 2.5m was measured on the top of
526 the residual BFRP strain as shown in Fig. 14 so that the actual BFRP strain at failure should
527 be a sum of these values. The relatively high values of BFRP strain prove that it can be
528 effectively used to strengthen concrete structures against impact without losing its
529 effectiveness as reported in previous studies. The cohesive debonding of BFRP in beams type

530 A, associated with a thin layer of concrete, exhibited sufficient bond strength between BFRP
531 and concrete (Fig. 16), which implies good workmanship.

532 **Conclusions**

533 This study experimentally examines the impact behaviour of RuC beams strengthened with
534 BFRP. The experimental results clearly show that the rubberized concrete beam deformed
535 less than the conventional concrete beam under the same impact energy even though they had
536 lower compressive strength of concrete and static strength. The findings can be summarized
537 as follows:

- 538 1. Rubberized concrete had 10-18% higher imparted energy per unit weight than that of
539 normal concrete.
- 540 2. Under the same impact energy, rubberized concrete reduces the maximum impact force
541 while providing slightly less deformation relative to conventional concrete.
- 542 3. BFRP strengthening sufficiently improves the impact resistance of the beams made of
543 both conventional and rubberized concrete. The BFRP strengthened beams damped the
544 impact force at a faster rate than the corresponding unstrengthened ones.
- 545 4. Locally strengthening the beams with U-shape BFRP wraps at the impact points
546 generates the same impact performance as compared to using U-shape BFRP wraps for
547 the entire beams but with a cheaper cost.
- 548 5. The debonding strain of BFRP wraps under impact tests was similar to that under static
549 tests so that it can be used efficiently to strengthened RC beams against impact loads.

550 Finally, rubberized concrete is a green and lightweight material. With a much lower
551 compressive strength, its impact performance is slightly better than conventional concrete
552 with lower maximum impact force and displacement and similar imparted energy.

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706 Table 1. Test matrix

Beam	Wrapping scheme	Longitudinal BFRP layers	U-shape FRP layers	Rubber content (%)	Concrete strength (MPa)	U-shape fiber orientation
B0_2m	-	-	-	0	50.3	-
B0A_2m	A	4	-	0	50.3	-
B0B_2m	B	4	2	0	50.3	90 ⁰
B0C_2m	C	4	2	0	50.3	90 ⁰
B0D_2m	D	4	2	0	50.3	45 ⁰
B15_2m	-	-	-	15	25.4	-
B15A_2m	A	4	-	15	25.4	-
B15B_2m	B	4	2	15	25.4	90 ⁰
B30_2m	-	-	-	30	14.7	-
B30A_2m	A	4	-	30	14.7	-
B30B_2m	B	4	2	30	14.7	90 ⁰

707 - Not applicable

708 Table 2. Experimental results of the impact tests

Rubber content (%)	Beam	Max Impact force (kN)	Impact force duration (ms)	Max reaction force (kN)	Max disp. (mm)	Residual disp. (mm)	Impact velocity (m/s)	*Residual velocity (m/s)	Imparted energy (J)	Dimensionless Imparted energy (J/kg)
0%	B0_2m	1475	0.69	54.8	45.6	32.9	6.25	-1.79	3744	
	B0A_2m	1815	0.54	51.7	33.4	16.1	6.23	-1.55	3801	
	B0A_2.5m	-	-	-	47.5	32.9	6.92	-1.54	4752	
	B0B_2m	1614	0.7	60.3	33.4	12.2	6.22	-1.55	3788	
	B0B_2.5m	1209	0.79	48.1	41.2	19.8	6.98	-1.55	4836	
15%	B15_2m	1412	0.58	45	43.4	29.8	6.19	-1.77	3673	
	B15A_2m	-	-	-	33.8	15.4	6.33	-2.11	3718	
	B15A_2.5m	1558	1.05	45.4	41.2	18.1	6.99	-2.10	4641	
	B15B_2m	-	-	-	31.4	10.7	6.30	-2.11	3679	
	B15B_2.5m	1173	0.98	54.4	43.1	25.7	7.24	-1.45	5253	
30%	B30_2m	-	-	-	44.8	31.3	5.99	-1.71	3441	
	B30A_2m	1552	0.65	39.8	36.6	-	6.29	-1.40	3926	
	B30A_2.5m	1351	1.00	42.9	46.9	19.5	7.04	-2.11	4709	
	B30B_2m	-	-	-	33.4	11.8	6.30	-2.19	3643	
	B30B_2.5m	1446	0.90	47.8	47.4	30.4	7.03	-1.41	4952	
0%	B0C_2m	1811	0.60	66.8	33.5	16.5	6.40	-2.40	3675	
	B0C_2.5m	1307	1.07	-	51.2	34.6	6.92	-0.77	4937	
	B0D_2m	1586	0.73	55.3	31.1	12.8	6.21	-2.33	3459	
	B0D_2.5m	1349	0.77	-	45.4	32.4	7.09	-1.57	4991	

709 - Not applicable

* Negative sign indicates the travel direction upward