





LETTER TO THE EDITOR

Rapid evolution of the recurrence time in the repeating partial tidal disruption event eRASSt J045650.3–203750

Zhu Liu¹, Taeho Ryu² , A. J. Goodwin³, A. Rau¹, D. Homan⁴, M. Krumpe⁴, A. Merloni¹, I. Grotova¹ ,
G. E. Anderson³, A. Malyali¹ , and J. C. A. Miller-Jones³ 

¹ Max-Planck-Institut für extraterrestrische Physik, Gießenbachstraße 1, 85748 Garching, Germany
e-mail: liuzhu@mpe.mpg.de

² Max-Planck-Institut für Astrophysik, Karl-Schwarzschild-Str. 1, 85748 Garching, Germany

³ International Centre for Radio Astronomy Research, Curtin University, GPO Box U1987, Perth, WA 6845, Australia

⁴ Leibniz-Institut für Astrophysik Potsdam, An der Sternwarte 16, 14482 Potsdam, Germany

Received 21 November 2023 / Accepted 28 February 2024

ABSTRACT

In this letter, we present the results from subsequent X-ray and UV observations of the nuclear transient eRASSt J045650.3–203750 (hereafter, J0456–20). We detected five repeating X-ray and UV flares from J0456–20, marking it as one of the most promising repeating partial tidal disruption event (*p*TDE) candidates. More importantly, we also found rapid changes in the recurrence time, T_{recur} , of the X-ray flares by modelling the long-term X-ray light curve of J0456–20. We found that T_{recur} first decreased rapidly from about 300 days to around 230 days. It continued to decrease to around 190 days with an indication of a constant T_{recur} , as evidenced by the latest three cycles. Our hydrodynamic simulations suggest that, in the repeating *p*TDE scenario, such a rapid evolution of T_{recur} could be reproduced if the original star is a $1 M_{\odot}$ main sequence star near the terminal age, losing nearly 80–90% of its mass during the initial encounter with a supermassive black hole (SMBH) of a mass around $10^5 M_{\odot}$. The inferred mass loss of $0.8\text{--}0.9 M_{\odot}$ is higher than the estimated value of around $0.13 M_{\odot}$ drawn from observations, which could be explained if the radiation efficiency is low (i.e. $\ll 0.1$). Our results indicate that repeating *p*TDEs could be effective tools for exploring the dynamics around SMBHs beyond our own Galaxy.

Key words. accretion, accretion disks – black hole physics – galaxies: nuclei – X-rays: individuals:: eRASSt J045650.3–203750

1. Introduction

Tidal disruption events (TDEs) are typically considered one-off events where a star is completely destroyed by a supermassive black hole (SMBH) at the first pericentre passage. However, theoretical calculations and numerical simulations have shown that a partial TDE (*p*TDE) can also occur (e.g. Guillochon & Ramirez-Ruiz 2013; Ryu et al. 2020). In a *p*TDE, the star loses only a fraction of its mass and survives its first encounter with the SMBH. If the star is initially in a bound orbit with low eccentricity, it is expected to generate repeating flares (e.g. Hayasaki et al. 2013; Ryu et al. 2020; Nixon & Coughlin 2022; Cufari et al. 2022, 2023; Melchor et al. 2024). Because the encounter cross-sections of *p*TDEs are generally larger than or comparable to those of full TDEs, the rate of *p*TDEs is expected to be larger or comparable to full TDEs (Krolik et al. 2020; Bortolas et al. 2023). Repeating *p*TDEs are particularly interesting as they may be effective probes to explore stellar dynamics around SMBHs beyond our own Galaxy and may also serve as ideal laboratories for studying the accretion processes in SMBHs.

Only a few repeating *p*TDE candidates have been reported so far (e.g. ASASSN-14ko, Payne et al. 2021; HLX-1¹, Webb et al. 2023; eRASSt J045650.3–203750, here-

after J0456–20, Liu et al. 2023; RX J133157.6–324319.7, Malyali et al. 2023; AT2018fyk, Wevers et al. 2023). Among these, J0456–20 is one of the best-studied repeating nuclear transients discovered in a quiescent galaxy ($z = 0.077$). Liu et al. (2023) reported the detection of three repeated X-ray and UV flares from J0456–20. In particular, the profiles of the X-ray flares are similar and can be characterised by four distinctive phases: an X-ray rising phase ($P_{X,\text{rise}}$) leading into an X-ray plateau phase ($P_{X,\text{plat}}$), which is terminated by a rapid X-ray drop phase ($P_{X,\text{drop}}$) and followed by an X-ray faint state ($P_{X,\text{faint}}$). These results provide strong evidence that J0456–20 is a repeating nuclear transient, making J0456–20 one of the most promising *p*TDE candidates.

Quasi-period eruptions (QPEs) are a class of recurring X-ray flares found in galactic nuclei, with periods of less than one day (Miniutti et al. 2019; Giustini et al. 2020; Arcodia et al. 2021). Their origin remains elusive, though recent studies indicate a potential link to *p*TDEs (e.g. GSN 069, Miniutti et al. 2023; RX J133157.6–324319.7, Malyali et al. 2023). The discovery of Swift J0230, which exhibits QPE-like behaviours with a period of around 22 days (Evans et al. 2023; Guolo et al. 2024), further strengthens the link between repeating *p*TDEs and QPEs. It is thus interesting to study the evolution of T_{recur} of the flares for repeating *p*TDEs. However, any substantial evolution in T_{recur} has only been reported in ASASSN-14ko and HLX-1. A period derivative of -0.0026 ± 0.0006 , with a period of $115.2_{-1.2}^{+1.3}$ days,

¹ Note that HLX-1 is believed to be an intermediate mass black hole (IMBH) with mass of $\sim 10^{4-5} M_{\odot}$ (Davis et al. 2011; Webb et al. 2012).

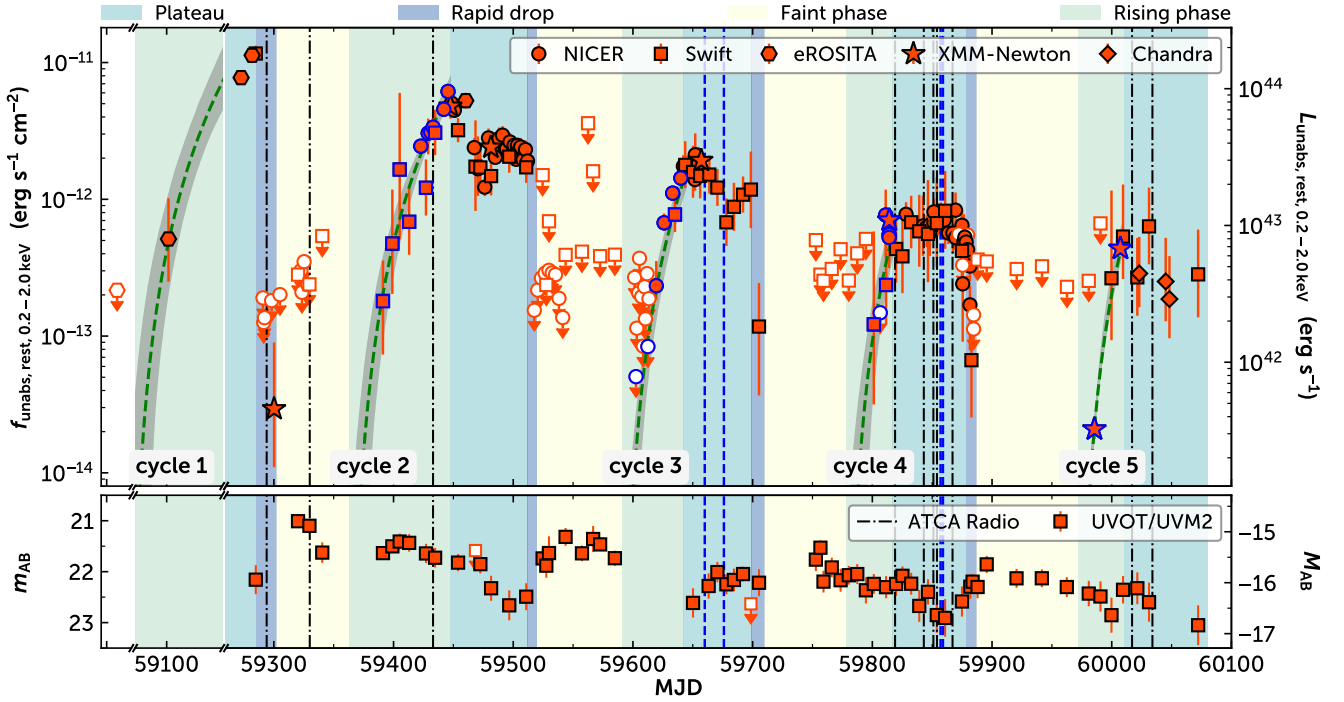


Fig. 1. Long-term X-ray and UV light curves for J0456–20. The coloured regions represent the four phases: the plateau phase ($P_{X,\text{plat}}$, light cyan), the rapid drop phase ($P_{X,\text{drop}}$, light blue), the faint phase ($P_{X,\text{faint}}$, light yellow), and the rising phase ($P_{X,\text{rise}}$, light green). *Upper panel:* red points with error bars are the unabsorbed rest-frame 0.2–2.0 keV X-ray light curve from eROSITA (hexagons), *Swift*/XRT (squares), NICER (circles), *XMM-Newton* (stars), and *Chandra* (diamonds). The error bars indicate 90% uncertainties. The points with downward arrows represent the 3σ flux and luminosity upper limits. The points with blue colour are the data used to model the profiles of the $P_{X,\text{rise}}$ phase. The green dashed lines show the best-fitting power-law model for the five X-ray rising phases. The grey shaded regions mark the 1σ uncertainty of the model. *Bottom panel:* UV light curve from *Swift*/UVOT UVM2 (red squares). The error bars mark the 1σ uncertainties. Squares with downward arrows indicate 3σ upper limits. The vertical lines mark the dates of the ATCA radio observations (black dashed-dotted: non-detections; blue dashed: detections).

has been reported for ASASSN-14ko (Payne et al. 2022). HLX-1 initially shows quasi-periodic X-ray outbursts spaced by about 1 yr between 2009 and 2012. Then, T_{recur} started to increase until 2018, with no X-ray outbursts detected afterwards (Godet et al. 2014; Webb et al. 2023). Long-term multi-wavelength observations on a larger sample of repeating p TDEs are required to fully understand the evolution of T_{recur} in these objects and potentially provide further evidence to confirm the connection between repeating p TDEs and QPEs.

In this letter, we report the discovery of the rapid evolution of T_{recur} in J0456–20. A detailed analysis of the latest X-ray and UV data has revealed five X-ray and UV flares in J0456–20 (marked as cycle 1–5 in Fig. 1). These results confirm that J0456–20 is indeed a repeating nuclear transient and also suggest an initially rapid decrease in T_{recur} by more than two months between cycles 1 and 2, slowing to around 40 days between cycles 2 and 3. Afterwards, T_{recur} reaches an almost constant value of around 190 days in the latest three cycles.

This paper is structured as follows. In Sect. 2, we present the multi-wavelength data reduction. X-ray spectral and light curve modelling are presented in Sect. 3. Finally, we discuss and summarise our results in Sects. 4 and 5. Throughout this paper, we adopt a flat Λ CDM cosmology with $H_0 = 67.7 \text{ km s}^{-1} \text{ Mpc}^{-1}$ and $\Omega_m = 0.308$ (Planck Collaboration VI 2020). Therefore $z = 0.077$ corresponds to a luminosity distance of $D_{\text{ld}} = 360 \text{ Mpc}$. All magnitudes will be reported in the AB system (not corrected for Galactic extinction). All the quoted uncertainties correspond to the 90% confidence level, unless specified otherwise.

2. Observations and data reduction

In this paper, we analysed all observations after MJD 59720. We refer to Liu et al. (2023) for more details on the data analysis prior to this date.

2.1. XMM-Newton

A pre-approved *XMM-Newton* target of opportunity (ToO) observation was performed on 2022 Aug. 23 (hereafter X5). In addition, two *XMM-Newton* Director’s Discretionary Time (DDT) observations were performed on 2023 Feb. 10 and Mar. 4 (hereafter X6 and X7, respectively). J0456–20 was detected in all new *XMM-Newton* observations.

The Observation Data Files (ODFs) for each observation were reduced using the *XMM-Newton* Science Analysis System software (SAS, version 19.1, Gabriel et al. 2004), with the latest calibration files. For each observation, the SAS tasks `emchain` and `epchain` tasks were used to generate the event lists for the European Photon Imaging Camera (EPIC) MOS (Turner et al. 2001) and pn (Strüder et al. 2001) detectors, respectively. High background flaring periods were identified and filtered from the event lists. For all the EPIC images, a circular region with a radius of 30, 20, 25” was chosen as the source region for X5, X6, and X7, respectively. A source-free annulus region with an inner radius of 50” and an outer radius of 100” was chosen as the background region for all MOS observations. The background for the pn camera was extracted from a circular region with a radius of 60” centred at the same CCD read-out column as the source position for all observations. X-ray events with pattern

≤ 12 for MOS and ≤ 4 for pn were selected to extract the X-ray spectra. We used the tasks `rmfgen` and `arfgen` to generate the response matrix and ancillary files, respectively. The X-ray spectra were rebinned to have at least one count per bin.

2.2. Swift observations

The XRT online data analysis tool² (Evans et al. 2009) was used to check whether the source was detected for each observation. It was also used to generate the X-ray spectra for observations where J0456–20 was detected and to calculate the 3σ count rate upper limits for non-detections. The X-ray spectra were rebinned to have at least one count in each bin.

The *Swift*/UVOT data were reduced using the UVOT analysis pipeline provided in HEASOFT (version 6.31) with UVOT calibration version 20201215. Source counts were extracted from a circular region with a radius of $5''$ centred at the source position. A $20''$ radius circle from a source-free region close to the position of J0456–20 was chosen as the background region. The task `uvotsource` was used to extract the photometry.

2.3. NICER observations

The NICER data were analysed using HEASOFT with the NICER data analysis software (version 10) and calibration files (version 20221001). The `nicer12` task is used to generate cleaned X-ray events. Events with overshoot higher than 1.5 or undershoot larger than 300 were removed. The `nicer13-spec` task was then used to generate the X-ray spectra for each NICER observation. The X-ray spectra were then rebinned to have at least one count per bin. We adopted the SCORPEON model to generate background models for each observation. The `nicerarf` and `nicerrmf` tasks were used to generate the response matrix and ancillary file for each observation, respectively. The same procedures were also adopted to re-analyse the NICER observations taken during the first two X-ray rising phases (i.e. observation carried out during MJD 59418–59448 and 59600–59641).

2.4. Chandra observations

We requested *Chandra* DDT observations of J0456–20, which were performed on 2023 Mar. 18, Apr. 11, and April 14 with the Advanced CCD Imaging Spectrometer (ACIS). We used the CIAO (Fruscione et al. 2006, version 4.15) software package to reduce the *Chandra* data with calibration files CALDB version 4.10.4. We reprocessed the *Chandra* data using the CIAO script `chandra_repro`. The CIAO task `dmextract` was used to extract the source and background spectra. We extracted the source spectra using a circular region with a radius of $2''$. The background spectra were extracted using an annulus (concentric with the source) region with an inner and outer radius of $6''$ and $20''$, respectively. The response files were generated using the `mkacisrmf` and `mkarf` tasks. The position of the X-ray flare measured from *Chandra* is (RA, Dec) = (04:56:49.81, $-20^{\circ}37'47.98''$) with a 2σ uncertainty of $0.54''$ (Appendix A), consistent with the centre of the host galaxy.

2.5. ATCA radio observations

We observed the coordinates of J0456–20 nine times with the Australia Telescope Compact Array (ATCA) between 2022 Aug.

² http://www.swift.ac.uk/user_objects

and 2023 Mar., in addition to the five observations between 2021 Mar. and 2022 Apr. reported in Liu et al. (2023). We observed the target during the X-ray outburst phase as this was previously when radio emission had been detected and therefore observed the target with the array in various configurations. In each observation, we used the dual 5.5 GHz and 9 GHz receiver, placing the 2×2 GHz of bandwidth split into 2048×1 MHz channels at a central frequency of 5.5 GHz and 9 GHz. Data were reduced in the Common Astronomy Software Application (CASA, version 5.6.3, CASA Team 2022) using standard procedures, including flux and bandpass calibration with PKS 1934–638 and phase calibration with PKS 0454–234. Additionally, we carried out one round of phase-only self-calibration of the target field at both 5.5 and 9 GHz, with a typical solution interval of two minutes, to produce a good quality image due to a bright AGN in the field. Images of the target field were created with the CASA task `tclean` and in cases where a source was visible at the location of J0456–20, the flux density was extracted with the CASA task `imfit` by fitting a Gaussian the size of the synthesised beam.

3. Data analysis and results

3.1. X-ray spectral modelling

The XSPEC software (version 12.13.0, Arnaud 1996) was used to fit all X-ray spectra using the Cash statistic (Cash 1979, Cstat in XSPEC). As mentioned in Liu et al. (2023), a power-law model (i.e. `TBabs*zashift*cflux*powerlaw`, hereafter M_{pl}) is preferred for observations taken at relatively high X-ray flux (i.e. the rest-frame unabsorbed 0.2–2.0 keV flux, $f_{X,soft}$, $\geq 5 \times 10^{-13}$ erg cm $^{-2}$ s $^{-1}$). We first fit all the new X-ray spectra with the M_{pl} model. The Galactic column density is fixed at 3.3×10^{20} cm $^{-2}$.

For NICER data, we first fit the total X-ray spectra over the 0.25–10.0 keV range with the backgrounds model generated using SCORPEON. We then re-fit the data by adding the M_{pl} model. A 3σ upper limit for $f_{X,soft}$ was estimated for observations in which the fit did not improve significantly (i.e. $\Delta C_{stat} < 11.8$) after adding the M_{pl} model. A strong oxygen $K\alpha$ line is presented in some of the NICER data. The `niscorpv22_swcxok_norm` parameter in the background model was thus left free to properly model the oxygen $K\alpha$ line in those observations. We fit the background subtracted spectra with the M_{pl} model for the data from the other missions. The *Swift*/XRT X-ray spectra were fitted over the 0.3–5.0 keV energy range, while the 0.5–5.0 keV energy band was used for *Chandra* observations. For *XMM-Newton* data, we jointly fit the data from the three EPIC cameras over the 0.2–5.0 keV energy range for X5 and X7 (0.2–2.0 keV for X6). The best-fit values and the 90% uncertainties were calculated for the $f_{X,soft}$ and photon index parameters. In addition, the 68% uncertainties for the $f_{X,soft}$ were also estimated for observations taken during the $P_{X,rise}$ phase. The 3σ upper limits of $f_{X,soft}$ were calculated for non-detections using either the M_{pl} or a disk model (see below). The details of the fitting results are listed in Table C.2.

Liu et al. (2023) noticed that the UV-to-X-ray SEDs of J0456–20 can be described by a multi-colour disk model (`TBabs*zashift*cflux*diskbb`, hereafter M_{mcd}) when the X-ray flux is low. Thus, the M_{mcd} model was also used to fit the X-ray spectra at the early stage of the $P_{X,rise}$ phase, namely, observations taken between MJD 59600 and 59620 in cycle 3 and X6 in cycle 5. J0456–20 was detected only on MJD 59619 (NICER, ObsID: 4595020126, hereafter N26) and on MJD 59999 (X6). The best-fitting T_{in} and

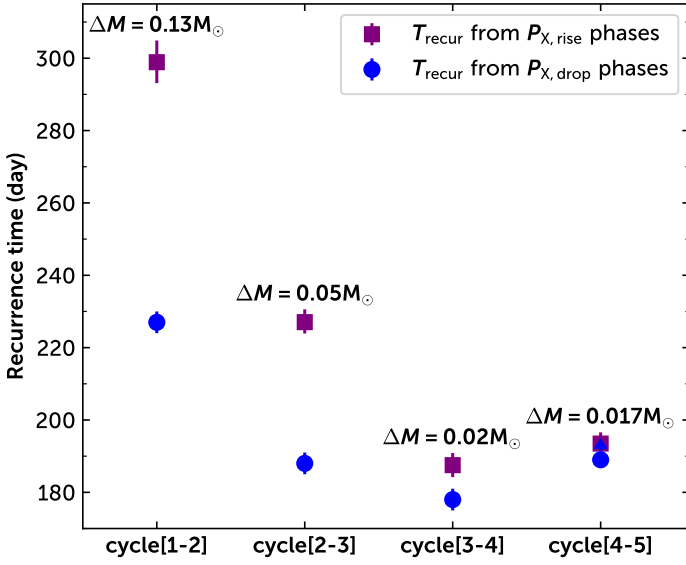


Fig. 2. Evolution of the recurrence time. The purple square (blue circle) points represent T_{recur} measured from the $P_{X,\text{rise}}$ ($P_{X,\text{drop}}$) phases. The error bars mark the 1σ uncertainties. The upward arrow indicates the 3σ lower limit. The estimated total mass loss from the star is also marked.

$f_{X,\text{soft}}$ are 193^{+43}_{-25} (78^{+24}_{-18}) eV and $2.0^{+0.5}_{-0.3} \times 10^{-14}$ ($2.3^{+1.2}_{-0.5} \times 10^{-13}$) $\text{erg cm}^{-2} \text{s}^{-1}$ for X6 (N26), respectively. The M_{pl} model resulted in a higher $f_{X,\text{soft}}$ of $3.3^{+1.0}_{-0.6} \times 10^{-14}$ ($4.6^{+1.1}_{-1.6} \times 10^{-13}$) $\text{erg cm}^{-2} \text{s}^{-1}$ with photon index of $3.3^{+0.3}_{-0.4}$ ($5.3^{+0.7}_{-0.8}$) for X6 (N26). Both the M_{mcd} and the M_{pl} model fit the X6 and N26 spectra well, although the M_{pl} model gives a slightly better fit ($C_{\text{stat}}/\text{d.o.f.} = 136/144$, compared to $152/144$) for X6.

In this work, we used the results from the M_{mcd} model for X6 and N26. The best-fitting T_{in} of N26 is comparable to that obtained from the eRASS2 and *Swift* observations (in the range of ~ 50 – 100 eV, Liu et al. 2023) at similar $f_{X,\text{soft}}$ (i.e. $\approx 4 \times 10^{-13}$ $\text{erg cm}^{-2} \text{s}^{-1}$), while T_{in} is much higher during the X6 observation when J0456–20 was in a historically low X-ray flux. This suggests a potential change in T_{in} during the $P_{X,\text{rise}}$ phase. For this reason, different values of T_{in} (listed in Table C.2) were used to calculate the 3σ flux upper limits for NICER observations before N26 during cycle 3.

3.2. Modelling the X-ray rising phase

The $P_{X,\text{rise}}$ phases during cycles 2, 3, 4, and 5 were captured by our follow-up observations. We also assumed that J0456–20 is in the $P_{X,\text{rise}}$ phase of cycle1 during the eRASS2 observations. This is justified by the duration of the $P_{X,\text{drop}}$ phase being much shorter than the $P_{X,\text{rise}}$ phase and by the spectral property of eRASS2 (i.e. best described by the M_{mcd} model) being similar to that at the early stage of the $P_{X,\text{rise}}$ phase.

We jointly fit the five $P_{X,\text{rise}}$ phases with a power-law function $f_{\text{rs},i}(t) = A * (t - t_i)^\beta$, where $i = 1, 2, 3, 4, 5$. We assumed that the normalisation, A , and power law index, β , were the same for all the five $P_{X,\text{rise}}$ phases. The `lmfit` package is adopted to fit the data with the least-squares method. To take into account upper limits and to estimate the uncertainties of the parameters in the model, we generated 10^5 realisations of $f_{X,\text{soft}}$ in the five $P_{X,\text{rise}}$ phases from Gaussian distributions for observations where J0456–20 has been detected as well as uniform distributions with a lower limit of zero (excluded) for non-detections. The best-fitting $f_{X,\text{soft}}$ and the 1σ uncertainties obtained from X-ray

Table 1. Results of the X-ray rising phase modelling and estimations of T_{recur} .

Parameters	Cycles [1, 2, 5] MJD	All cycles MJD	T_{recur} days	$T_{\text{recur, drop}}$ days
t_1	59070^{+7}_{-8}	59065^{+8}_{-9}	299^{+6}_{-6}	227 ± 3
t_2	59367^{+5}_{-5}	59363^{+6}_{-6}	227^{+4}_{-3}	188 ± 3
t_3	–	59591^{+6}_{-5}	188^{+3}_{-3}	178 ± 3
t_4	–	59778^{+7}_{-7}	193^{+3}_{-3}	>189
t_5	59976^{+3}_{-4}	59972^{+4}_{-5}		
$\log A$	$-16.2^{+0.6}_{-0.8}$	$-17.2^{+1.0}_{-1.2}$		
β	$2.6^{+0.4}_{-0.3}$	$3.1^{+0.6}_{-0.5}$		

Notes. *Parameters*: name of the parameter in the power-law model; *Cycles [1,2,5]*: results from jointly fitting the $P_{X,\text{rise}}$ phases of cycles 1, 2, and 5; *All cycles*: results by jointly fitting the $P_{X,\text{rise}}$ of all the five cycles; T_{recur} and $T_{\text{recur, drop}}$ are the recurrence time estimated using the $P_{X,\text{rise}}$ and $P_{X,\text{drop}}$ phases, respectively.

spectral modelling of each observation are used as the means and standard deviations of the Gaussian distributions, respectively. The 3σ $f_{X,\text{soft}}$ upper limits for non-detections are used as the upper limits for the uniform distributions. We obtained 10^5 values for each parameter in the model by fitting the 10^5 datasets using the least squares method. We estimated the best-fitting values using the median values for each parameter and estimated the 1σ confidence intervals using the 16th and 84th percentiles of the fitting results. Similarly, the recurrence time T_{recur} for cycle i and $i + 1$, and the lower and the upper intervals of the 1σ confidence intervals are estimated using the median, the 16th, and 84th percentiles of a sample calculated using $t_{i+1} - t_i$. To test whether the results could be affected by the inclusion of flux upper limits, we applied the same procedures to cycles 1, 2, and 5 only (i.e. cycles without upper limits in the $P_{X,\text{rise}}$ phases). We found the results to be consistent within 1σ uncertainties (see Table 1). The fitting results and the estimated T_{recur} are listed in Table 1. We also calculated the recurrence time using the $P_{X,\text{drop}}$ phase (Appendix B). The estimated values of T_{recur} are also listed in Table 1. It is clear from Fig. 2 that the T_{recur} of the X-ray flares in J0456–20 show rapid changes. The mass loss for each cycle marked in Fig. 2 are calculated using the method outlined in Sect. 3.3.

3.3. Estimation of the mass loss

Following Liu et al. (2023), a cycle is defined as the time between the start of two consecutive $P_{X,\text{rise}}$ phases. The total energy released in each cycle was estimated by

$$E_{\text{tot}} = L_{\text{fa}} \Delta t_{\text{fa}} + L_{\text{pl}} \Delta t_{\text{pl}} + \int_0^{\Delta t_{\text{rs}}} L_{\text{rs}}(t) dt, \quad (1)$$

where L_{rs} is the bolometric luminosity during the $P_{X,\text{rise}}$ phase, which is calculated using the best-fitting power law (see Sect. 3.2), that is, $L_{\text{rs}}(t) = \kappa 4\pi D_{\text{ld}}^2 f_{\text{rs}}(t)$, where $\kappa = L_{\text{bol}}/L_{X,\text{res}0.2-2.0\text{keV}}$ is the bolometric correction factor and D_{ld} is

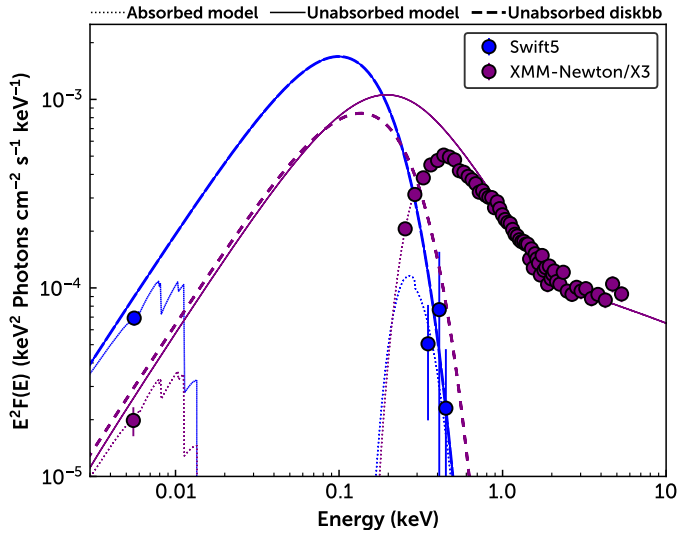


Fig. 3. UV to X-ray SEDs at different X-ray flux levels. The solid circles are the unfolded spectra for Swift5 (blue) and *XMM-Newton/X3* (purple). The dotted lines are the absorbed models. The solid and dashed lines represent the unabsorbed intrinsic model and the diskbb component, respectively.

the luminosity distance. Then, L_{pl} and L_{fa} are the average bolometric luminosity during each of the $P_{X,\text{plat}}$ and $P_{X,\text{faint}}$ phases, respectively, while Δt_{fa} , Δt_{pl} , and Δt_{rs} are the duration of the $P_{X,\text{faint}}$, $P_{X,\text{plat}}$, and $P_{X,\text{rise}}$ phases, respectively. The $P_{X,\text{faint}}$ phase in cycle 5 was not covered by our follow-up observations. In this work, we assumed $\Delta t_{\text{fa}} = 70$ days for cycle 5. Liu et al. (2023) estimated the κ to be in the range of 3–20 during the $P_{X,\text{rise}}$ phase, calculated by modelling the UV to X-ray data using either the M_{mcd} (when J0456–20 is X-ray faint) or Comptonized M_{mcd} model. The T_{in} of the M_{mcd} model is around 40–60 eV and does not change significantly (see also Fig. 10 in Liu et al. 2023). Following Liu et al. (2023), we adopted a value of $\kappa = 15$ to calculate L_{rs} during the $P_{X,\text{rise}}$ phases. The high quality X-ray and UV data taken during the $P_{X,\text{plat}}$ phase of cycle 2 (the third *XMM-Newton* observation, hereafter X3) can be optimally fitted with a multi-coloured disk (with T_{in} around 60 eV) Comptonized by two coronae (*XMM-Newton/X3* in Fig. 3; see also Table 3 in Liu et al. 2023 for the best-fitting results for X3). We estimated a value of $\kappa \sim 3$ using this model. Both the X-ray and UV only show mild variability during the $P_{X,\text{plat}}$ phases, indicating that κ will not change significantly. We thus calculated L_{pl} assuming $\kappa = 3$ for the $P_{X,\text{plat}}$ phases. L_{fa} is poorly constrained. We thus estimated L_{fa} using the M_{mcd} model ($T_{\text{in}} \sim 45$ eV) obtained by modelling the UV and X-ray emission from the first Swift observation in cycle 2 (Swift5 in Fig. 3). This model resulted in a bolometric luminosity of $L_{\text{bol,sw}} = 9.0 \times 10^{43}$ erg s $^{-1}$. Considering that the peak UV magnitude in $P_{X,\text{faint}}$ phases is $\lesssim 0.6$ mag brighter than that during the $P_{X,\text{rise}}$ phases, we thus conservatively estimated L_{fa} by multiplying $L_{\text{bol,sw}}$ by a factor of 1.8, which leads to a value of 1.6×10^{44} erg s $^{-1}$.

The values of the parameters used to calculate E_{tot} for each cycle can be found in Table 2. To calculate the total mass loss in each cycle, we assumed that half of the tidally disrupted debris returns to the SMBH and that the radiation efficiency is 0.1. We estimated a total released energy (mass loss) of 1.12 (0.13), 0.46 (0.05), 0.18 (0.02), 0.15 (0.017), and $\gtrsim 0.12 \times 10^{52}$ erg ($\gtrsim 0.014 M_{\odot}$) for cycles 1, 2, 3, 4, and 5, respectively. A lower limit is given for cycle 5 as the $P_{X,\text{plat}}$ phase could be longer than the value quoted in Table 2.

Table 2. Values of the parameters used to calculate the total release energy (E_{tot}) and mass loss (ΔM) in each cycle.

	cycle 1	cycle 2	cycle 3	cycle 4	cycle 5
t_s (MJD)	59065	59363	59591	59778	59972
Δt_{rs} (day)	100	84	51	39	38
Δt_{pl} (day)	120	65	57	61	$\gtrsim 70$
Δt_{fa} (day)	61	71	68	85	70
L_{pl} (10^{44} erg s $^{-1}$)	4.6	1.1	0.70	0.27	0.13
E_{tot} (10^{52} erg)	1.12	0.46	0.18	0.15	$\gtrsim 0.12$
ΔM (M_{\odot})	0.13	0.05	0.02	0.017	$\gtrsim 0.014$

Notes. t_s is the start date of the cycle. Δt_{rs} , Δt_{pl} , and Δt_{fa} are the duration for the $P_{X,\text{rise}}$, $P_{X,\text{plat}}$, and $P_{X,\text{faint}}$ phases, respectively. The estimated values for E_{tot} and ΔM are also listed.

3.4. Radio variability

J0456–20 was mostly undetected after 2022 Aug., with a detection at 9 GHz on 2022 Oct. 05 and at 5.5 GHz on 2022 Oct. 07 during the $P_{X,\text{plat}}$ phase of cycle 4 (see Fig. 1) with a significance of 7 and 9 σ , respectively. In order to improve the sensitivity, we additionally stacked the observations from October 2–7 and detected a faint point source at the coordinates of J0456–20. The radio observations reported here indicate that the transient radio source associated with the X-ray outbursts in 2022 Mar. and Apr. has also been fading, consistent with the decrease in the peak X-ray flux of each cycle (see Fig. 1). A summary of the ATCA radio observations of J0456–20 is given in Table C.1. The long-term radio light curve is shown in Fig. C.1.

4. Discussion

We detected five repeating X-ray flares in J0456–20 using the latest data. In addition, repeating transient radio emission has also been detected in J0456–20. These results provide further evidence that J0456–20 is a repeating nuclear transient, making it one of the most promising repeating p TDE candidates. More importantly, our results also revealed rapid evolution of the recurrence time T_{recur} , measured from the $P_{X,\text{rise}}$ phases, of the X-ray flares. Specifically, T_{recur} decreased by more than two months between cycles 1 and 2. It continued to decrease by roughly 40 days between cycles 2 and 3. Such a rapid change is likely to have ceased, as suggested by an almost constant T_{recur} (~ 190 days) measured from the latest three cycles. Evidence for the evolution of T_{recur} has also been found using the values measured from the $P_{X,\text{drop}}$ phases (Appendix B and Table 1). However, the changes in T_{recur} are less dramatic than those measured from the $P_{X,\text{rise}}$ phases, which may be attributed to the changes in the duration of the other phases (see Table 2). In this work, T_{recur} values derived from the $P_{X,\text{rise}}$ phase were used.

The evolution of T_{recur} has been reported only in a few repeating p TDE candidates. For instance, ASASSN-14ko showed a decrease in the periods with a period derivative of around -0.0026 (Payne et al. 2022; Huang et al. 2023), which is much shorter than that found in J0456–20 ($\lesssim -0.2$). The X-ray flares in HLX-1 initially showed a quasi-periodic T_{recur} of around 1 yr. Then, T_{recur} increased by about one month in 2013 (Godet et al. 2014) and continued to increase until 2018, after which no X-ray outbursts were detected (Webb et al. 2023). Unlike the case of HLX-1, we found no evidence for an increase in T_{recur} in J0456–20 as of now. As suggested by Godet et al. (2014), the evolution of T_{recur} can put strong constraints on the initial mass, the mass loss, and the orbital parameters of the star.

A repeating p TDE is favoured to explain the long-term multi-wavelength light curve of J0456–20 (Liu et al. 2023). We thus performed simulations to test if the changes in T_{recur} , ΔP , can be explained by p TDEs. We made a grid of hydrodynamics simulations, using the moving-mesh code AREPO (Springel 2010; Weinberger et al. 2020; Pakmor et al. 2016), to examine the change in the orbital period of remnants produced in p TDEs of main-sequence stars by BHs with a mass of $M_{\text{BH}} = 10^5 M_{\odot}$. We considered solar-metallicity main sequence stars with masses of $M_{\star} = 1, 2, \text{ and } 3 M_{\odot}$, and a core hydrogen mass fraction of 0.01 (terminal age) and 0.3 (middle age), evolved using the 1D stellar evolution code MESA (Paxton et al. 2013, 2015, 2019, 2011), imported into AREPO with $0.5M$ cells³. We also considered a wide range of the pericentre distance of r_p , $0.1 \lesssim r_p/r_t \lesssim 1.2$ (tidal radius $r_t = (M_{\text{BH}}/M_{\star})^{1/3}R_{\star}$), encompassing scenarios from the full disruption to no mass loss. We varied the pericentre distance for a given M_{\star} . Meanwhile, we fixed the orbital period of the original orbit to be 300 days, so that the stellar orbit in each simulation would have a different eccentricity ($e \gtrsim 0.99$). The initial separation between the black hole and the star is $5 r_t$. We followed the evolution of the remnant after the first pericentre passage of the original star, using the Helmholtz equation of state (Timmes & Swesty 2000) until the post-disruption orbital parameters do not evolve, which occurred when the separation between the black hole and the remnant is $\gtrsim 5r_t$. We verified that the total energy in all simulations was conserved within a fractional error of $\lesssim 10^{-5}$. We note that a rapid decrease in T_{recur} requires a BH mass of around $10^5 M_{\odot}$ in our simulations, which were run with a limited range of parameter space. Our simulations with a higher BH mass of $10^6 M_{\odot}$ cannot reproduce T_{recur} observed in J0456–20. The required BH mass of $10^5 M_{\odot}$ is much smaller than the value quoted in Liu et al. (2023), which is around $10^7 M_{\odot}$. However, as cautioned in Liu et al. (2023), the values of M_{BH} measured from the $M_{\text{BH}} - \sigma_{\star}$ relation and the $\sigma_{\text{rms}}^2 - M_{\text{BH}}$ relation exhibit notable differences and have large uncertainties. Thus, a M_{BH} on the order of $10^5 M_{\odot}$ could still be possible for J0456–20.

Figure 4 depicts ΔP as a function of the original stellar mass, M_{\star} , and the fractional mass loss, $\Delta M/M_{\star}$. The general trend indicates that ΔP decreases as $\Delta M/M_{\star}$ increases until the fractional mass loss exceeds a critical value Δm_c , roughly $\approx 0.7\text{--}0.8$. Above the critical mass loss, ΔP starts to increase with $\Delta M/M_{\star}$. This trend was observed for parabolic p TDEs in Ryu et al. (2020). However, the values of ΔP strongly depend on the internal structure of the star (i.e. mass and age). For p TDEs of middle age stars, ΔP is negative (positive) when $\Delta M/M_{\star}$ is below (above) Δm_c , meaning the remnants become more (less) bound than that of the original star before the TDE. For this case, ΔP is at most ≈ -10 days. However, ΔP is negative across a wider range of $\Delta M/M_{\star}$ and can be as large as -90 days for p TDEs of terminal age stars. Most notably, the large ΔP (i.e. ~ -70 days) observed in J0456–20 between cycles 1 and 2 can be reproduced if the original star is a $1 M_{\odot}$ terminal age star and loses nearly 80–90% of its mass. Although we have not explored the entire parameter space of p TDEs, our simulations suggest that the observed decrease in T_{recur} may be explained by a severe p TDE of a main sequence star near the terminal age. The inferred mass loss ($0.8\text{--}0.9 M_{\odot}$) is much higher than that estimated for cycle 1 ($\sim 0.13 M_{\odot}$, Sect. 3.3 and Table 2) of J0456–20. We note that this discrepancy can be alleviated if the radiation efficiency in J0456–20 is much lower than the

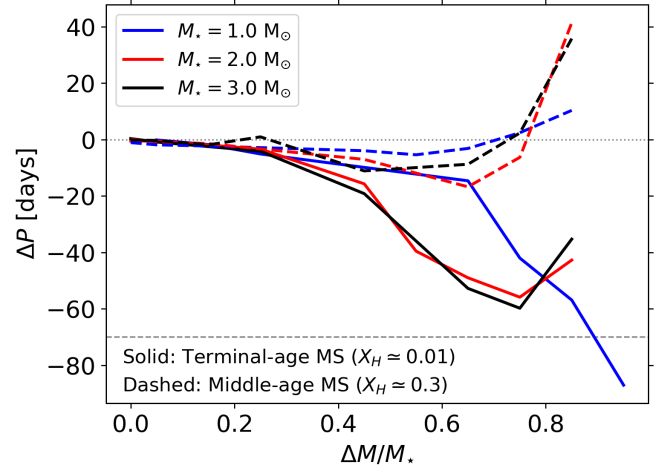


Fig. 4. Change in the orbital period ΔP (in days) for remnants in p TDEs of main sequence stars with mass of $M_{\star} = 1, 2, \text{ and } 3 M_{\odot}$ in hydrodynamics simulations, as a function of the fractional mass loss $\Delta M/M_{\star}$. The original stars are Solar metallicity main sequence stars with a core hydrogen mass fraction of $X_{\text{H}} \approx 0.01$ (Terminal age: solid lines) and 0.3 (Middle age: dashed lines). The simulations suggest that ΔP in severe p TDEs of terminal-age main-sequence stars can be compatible with the change in T_{recur} between cycles 1 and 2 (≈ -70 days, grey horizontal line) of J0456–20.

assumed value of 0.1. It is important to also emphasise that our simulation result merely suggests p TDE is a plausible mechanism for generating a transient like J0456–20 and does not rule out other potential mechanisms. For instance, Linial & Quataert (2024) summarized several plausible origins for observed period evolution in repeating nuclear transients. They suggested that the period evolution in ASASSN-14ko is consistent with orbital decay induced by hydrodynamic drag as the star passes through an accretion disk (see also Zhou et al. 2024). The repeating flares in ASASSN-14ko could then be powered primarily through dragging-induced stripping of mass from the star. This scenario, however, is unlikely to be the dominant process in J0456–20, as it requires an accretion disk with mass larger than $10 M_{\odot}$ (Eq. (20) in Linial & Quataert 2024, assuming $M_{\text{BH}} = 10^5 M_{\odot}$) around r_p to explain the observed changes in T_{recur} in J0456–20.

5. Summary

In this letter, we analyse new multi-wavelength observations for the promising repeating p TDE candidate J0456–20. We detected five repeating X-ray flares and repeating transient radio emission from J0456–20, providing additional strong evidence that J0456–20 is a repeating nuclear transient. In addition, the latest X-ray data also reveals changes in the recurrence time, T_{recur} , of the X-ray flare. We found that T_{recur} initially decreased rapidly from ~ 300 days to ~ 230 days and it continues to decrease by roughly 40 days per cycle, with an indication of constant values of ~ 190 days in the latest cycles. Our hydrodynamic simulations show that the large decrease in T_{recur} can be explained in the p TDE scenario, provided that the original star is a $1 M_{\odot}$ terminal age star with an initial fractional mass loss of around 80–90%. Our results suggest that precise estimations of T_{recur} in repeating p TDEs can provide additional constraints on the initial mass of the disrupted star and mass loss during each passage. They also indicate that repeating p TDEs could be effective tools to probe the stellar and gas dynamics around SMBHs beyond our own Galaxy.

³ We confirmed that simulations with different resolutions between 0.25M and 1M cells yield converging ΔP .

Acknowledgements. ZL is grateful to the *XMM-Newton*, *Swift*, and NICER teams for approving the ToO/DDT requests and arranging the follow-up observations. The hydrodynamics simulations were conducted using computational resources (and/or scientific computing services) at the Max-Planck Computing & Data Facility. DH acknowledges support from DLR grant FKZ 50 OR 2003. MK is supported by DFG grant KR 3338/4-1 and DLR grant 50 OR 2307. This work was supported by the Australian government through the Australian Research Council's Discovery Projects funding scheme (DP200102471).

References

- Arcodia, R., Merloni, A., Nandra, K., et al. 2021, *Nature*, 592, 704
- Arnaud, K. A. 1996, *ASP Conf. Ser.*, 101, 17
- Bortolas, E., Ryu, T., Broggi, L., & Sesana, A. 2023, *MNRAS*, 524, 3026
- CASA Team (Bean, B., et al.) 2022, *PASP*, 134, 114501
- Cash, W. 1979, *ApJ*, 228, 939
- Cufari, M., Coughlin, E. R., & Nixon, C. J. 2022, *ApJ*, 929, L20
- Cufari, M., Nixon, C. J., & Coughlin, E. R. 2023, *MNRAS*, 520, L38
- Davis, S. W., Narayan, R., Zhu, Y., et al. 2011, *ApJ*, 734, 111
- Evans, P. A., Beardmore, A. P., Page, K. L., et al. 2009, *MNRAS*, 397, 1177
- Evans, P. A., Nixon, C. J., Campana, S., et al. 2023, *Nat. Astron.*, 7, 1368
- Fruscione, A., McDowell, J. C., Allen, G. E., et al. 2006, *SPIE Conf. Ser.*, 6270, 62701V
- Gabriel, C., Denby, M., Fyfe, D. J., et al. 2004, in *Astronomical Data Analysis Software and Systems (ADASS) XIII*, eds. F. Ochsenbein, M. G. Allen, & D. Egret, *ASP Conf. Ser.*, 314, 759
- Giustini, M., Miniutti, G., & Saxton, R. D. 2020, *A&A*, 636, L2
- Godet, O., Lombardi, J. C., Antonini, F., et al. 2014, *ApJ*, 793, 105
- Guillochon, J., & Ramirez-Ruiz, E. 2013, *ApJ*, 767, 25
- Guolo, M., Pasham, D.R., Zajaček, M., et al. 2024, *Nat. Astron.*, <https://doi.org/10.1038/s41550-023-02178-4>
- Hayasaki, K., Stone, N., & Loeb, A. 2013, *MNRAS*, 434, 909
- Huang, S., Jiang, N., Shen, R.-F., Wang, T., & Sheng, Z. 2023, *ApJ*, 956, L46
- Krolik, J., Piran, T., & Ryu, T. 2020, *ApJ*, 904, 68
- Linial, I., & Quataert, E. 2024, *MNRAS*, 527, 4317
- Liu, Z., Malyali, A., Krumpel, M., et al. 2023, *A&A*, 669, A75
- Malyali, A., Liu, Z., Rau, A., et al. 2023, *MNRAS*, 520, 3549
- Melchor, D., Mockler, B., Naoz, S., Rose, S. C., & Ramirez-Ruiz, E. 2024, *ApJ*, 960, 39
- Miniutti, G., Saxton, R. D., Giustini, M., et al. 2019, *Nature*, 573, 381
- Miniutti, G., Giustini, M., Arcodia, R., et al. 2023, *A&A*, 670, A93
- Nixon, C. J., & Coughlin, E. R. 2022, *ApJ*, 927, L25
- Pakmor, R., Springel, V., Bauer, A., et al. 2016, *MNRAS*, 455, 1134
- Paxton, B., Bildsten, L., Dotter, A., et al. 2011, *ApJS*, 192, 3
- Paxton, B., Cantiello, M., Arras, P., et al. 2013, *ApJS*, 208, 4
- Paxton, B., Marchant, P., Schwab, J., et al. 2015, *ApJS*, 220, 15
- Paxton, B., Smolec, R., Schwab, J., et al. 2019, *ApJS*, 243, 10
- Payne, A. V., Shappee, B. J., Hinkle, J. T., et al. 2021, *ApJ*, 910, 125
- Payne, A. V., Shappee, B. J., Hinkle, J. T., et al. 2022, *ApJ*, 926, 142
- Planck Collaboration VI. 2020, *A&A*, 641, A6
- Ryu, T., Krolik, J., Piran, T., & Noble, S. C. 2020, *ApJ*, 904, 100
- Springel, V. 2010, *MNRAS*, 401, 791
- Strüder, L., Briel, U., Dennerl, K., et al. 2001, *A&A*, 365, L18
- Timmes, F. X., & Swesty, F. D. 2000, *ApJS*, 126, 501
- Turner, M. J. L., Abbey, A., Arnaud, M., et al. 2001, *A&A*, 365, L27
- Webb, N., Cseh, D., Lenc, E., et al. 2012, *Science*, 337, 554
- Webb, N. A., Barret, D., Godet, O., et al. 2023, *Astron. Nachr.*, 344, e20230051
- Weinberger, R., Springel, V., & Pakmor, R. 2020, *ApJS*, 248, 32
- Wevers, T., Coughlin, E. R., Pasham, D. R., et al. 2023, *ApJ*, 942, L33
- Zhou, C., Huang, L., Guo, K., Li, Y. P., & Pan, Z. 2024, *ArXiv e-prints* [arXiv:2401.11190]

Appendix A: *Chandra* astrometric correction

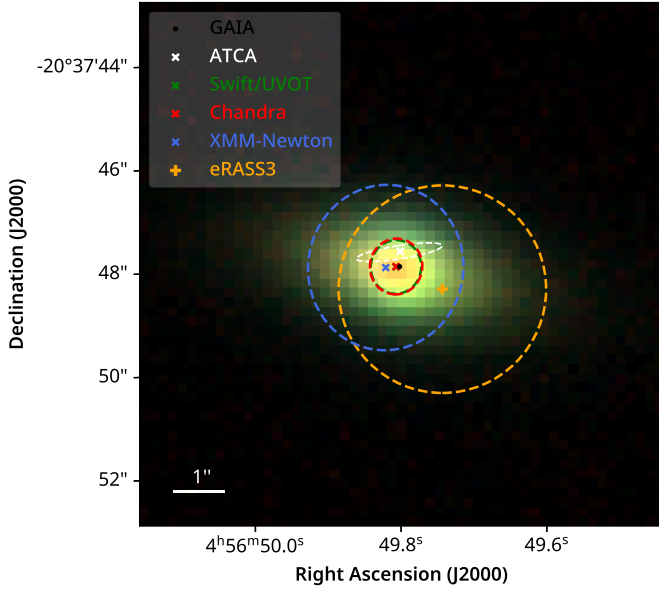


Fig. A.1. Updated multi-wavelength positions of J0456–20. The black dot marks the position given in the *Gaia* EDR3. The crosses represent the positions measured from different instruments, and the circles indicate the 2σ positional uncertainties: *Swift*/UVOT (green, $2\sigma = 0.52''$), *Chandra* (red, $2\sigma = 0.54''$), ATCA (white, $2\sigma = 1.0''$), XMM-Newton (royalblue, $2\sigma = 1.6''$), and eRASS3 (orange, $2\sigma = 2.0''$).

We ran the WAVDETECT tool on the *Chandra* data to generate a source list for each observation. J0456–20 was detected in all the three *Chandra* observations. We used the source positions provided in the Legacy Survey DR10 catalogue as a reference. The overall 90% absolute astrometry uncertainty of *Chandra* is ~ 1.11 arcsec⁴. We thus cross-matched the positions of the X-ray source measured from the *Chandra* observations with the source positions listed in the DR10 catalogue using a radius of 1.1 arcsec. We selected sources within 3 arcmin of the aim-point of the telescope. This resulted in three sources (excluding J0456–20, see A.1) that are detected in both X-ray and DR10 in the second *Chandra* observation (only two for the other two observations). The CIAO task WCS_MATCH and WCS_UPDATE were then used to correct and update the aspect ratio. The residual rms scatter in the corrected X-ray positions of the LS10 sources is 0.28 arcsec, which corresponds to a 2σ position error of ≈ 0.54 arcsec (assuming Rayleigh distribution). The astromet-

Table A.1. Astrometric corrections for *Chandra* observations.

	Object	Coordinates/Separations
LS DR10	J0456–20	04:56:49.80, $-20^{\circ}37'47.99''$
	Ref1	04:56:57.39, $-20^{\circ}35'12.75''$
	Ref2	04:56:58.64, $-20^{\circ}35'57.25''$
	Ref3	04:56:58.70, $-20^{\circ}37'47.65''$
<i>Chandra</i>	J0456–20	04:56:49.81, $-20^{\circ}37'47.98''$
	Ref1	04:56:57.39, $-20^{\circ}35'13.25''$
With correction	Ref2	04:56:58.66, $-20^{\circ}35'57.49''$
	Ref3	04:56:58.73, $-20^{\circ}37'48.58''$
	<hr/>	
<i>Chandra</i>	J0456–20	04:56:49.82, $-20^{\circ}37'48.54''$
	Ref1	04:56:57.38, $-20^{\circ}35'12.69''$
	Ref2	04:56:58.64, $-20^{\circ}35'56.94''$
No correction	Ref3	04:56:58.71, $-20^{\circ}37'48.03''$
	<hr/>	
	Separation	J0456–20
Ref1		0.18''
Ref2		0.32''
Ref3		0.41''
<hr/>		

Notes. Refs 1–3 denote the reference sources used for performing astrometric correction for *Chandra*. The Separations are calculated using the astrometric corrected *Chandra* positions and the LS DR10 positions.

ric corrected *Chandra* position is consistent with the centre of the host galaxy (see Fig. A.1).

Appendix B: Estimation of the recurrence time using the X-ray drop phase

The recurrence time can also be determined using the $P_{X, \text{drop}}$ phases. The start dates of the $P_{X, \text{drop}}$ phases, $t_{s, \text{drop}}$, can be well constrained in a model-independent way due to their short duration (i.e. $f_{X, \text{soft}}$ drops by a factor of ≥ 10 within one week). We estimated $t_{s, \text{drop}}$ in the range of MJD [59285, 59291], [59512, 59518], and [59699, 59706], and [59878, 59883] for cycles 1, 2, 3, and 4, respectively. The $P_{X, \text{drop}}$ phase was not observed in cycle 5 because J0456–20 was blocked by the Sun. However, a lower limit of $> \text{MJD } 60072$ can be given. We generated 10^5 realisations of $t_{s, \text{drop}}$ for each cycle in cycles 1–4, assuming uniform distributions of $t_{s, \text{drop}}$ in the estimated MJD ranges. T_{recur} and the 1σ intervals can be estimated using the median and the 16th and 84th percentiles of the difference between consecutive $t_{s, \text{drop}}$ for cycles 1–4. We calculated a 3σ upper limit of 189 days for T_{recur} between cycles 4 and 5. The estimated T_{recur} values are listed in Table 1.

⁴ <http://cxc.cfa.harvard.edu/cal/ASPECT/celmon>

Appendix C: Details of the radio and X-ray observations

Table C.1 lists the ATCA radio observations for J0456–20. J0456–20 was detected only in the $P_{X, \text{plat}}$ phase during cycles 3 and 4. The long-term radio variability is shown in Fig. C.1.

The details of the X-ray observations and the X-ray spectral fitting results are listed in Table C.2.

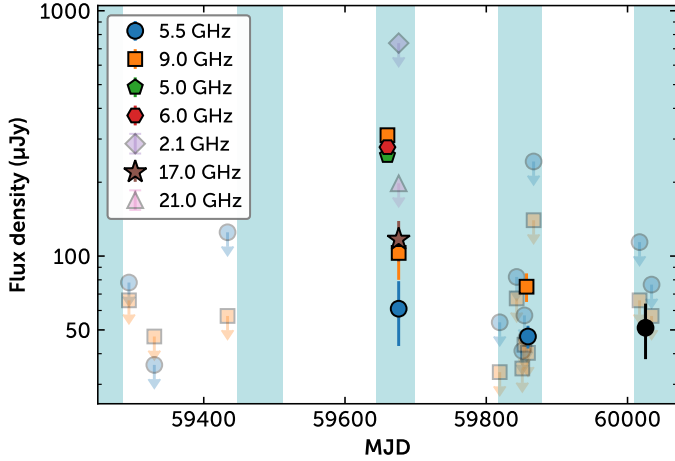


Fig. C.1. Evolution of the radio flux density. The error bars mark the 1σ uncertainties. The downward arrows represent the 3σ upper limits. The black circle shows the flux density at 5.5 GHz measured from the stacked observation from 2023 Mar. The light cyan regions indicate the $P_{X, \text{plat}}$ phase in each cycle.

Table C.1. ATCA radio observations of J0456–20

Date	Frequency (GHz)	Array config.	Flux Density (μJy)
2021-03-21	5.5	6D	< 78
	9		< 66
2021-04-26	5.5	6D	< 36
	9		< 47
2021-08-07	5.5	EW367	< 125
	9		< 57
2022-03-22	5	6A	257 ± 11
	6		278 ± 11
	9		311 ± 12
2022-04-06	2.1	6A	< 738
	5.5		61 ± 18
	9		103 ± 23
	17		117 ± 22
2022-08-28	21		< 198
	5.5	6D	< 53.7
9	< 33.6		
2022-09-21	5.5	6D	< 82.2
	9		< 67.2
2022-09-29	5.5	6D	< 41.1
	9		< 34.8
2022-10-02	5.5	6D	< 57.3
	9		< 43.5
2022-10-05	5.5	6D	< 46.5
	9		75 ± 10
2022-10-07	5.5	6D	47 ± 5
	9		< 40.3
2022-10-15	5.5	H214	< 243
	9		< 140
2023-03-14	5.5	750C	< 114
	9		< 66
2023-03-31	5.5	750C	< 76.5
	9		< 57
2022-10-02, 2022-10-05, 2022-10-07	5.5	6D	35 ± 5
2022-10-02, 2022-10-05, 2022-10-07	9	6D	28 ± 5
2023-03-14, 2023-03-31	5.5	750C	51 ± 13
2023-03-14, 2023-03-31	9	750C	< 58

Notes. Upper limits are reported at 3σ .

Table C.2. Log of X-ray observations.

MJD	T_{exp}	T_{in}/Γ	$f_{\text{X, soft}}$	ObsID	Mission	X-ray phase	cycle
58919.15	325	3.0	< 0.22	eRASS1	eROSITA	—	—
59101.73	340	64^{+29}_{-18}	$0.51^{+0.51}_{-0.26}$	eRASS2 ^a	eROSITA	$P_{\text{X, rise}}$	1
59272.63	194	$2.5^{+0.2}_{-0.2}$	$7.76^{+0.84}_{-0.76}$	eRASS3	eROSITA	$P_{\text{X, plat}}$	1
59281.86	123	$2.8^{+0.2}_{-0.2}$	$11.30^{+1.61}_{-1.40}$	eRASS3	eROSITA	$P_{\text{X, plat}}$	1
59284.89	1683	$2.5^{+0.1}_{-0.1}$	$11.64^{+1.66}_{-1.45}$	00014135001	<i>Swift</i>	$P_{\text{X, plat}}$	1
59290.94	1664	3.0	< 0.19	4604010101	<i>NICER</i>	$P_{\text{X, drop}}$	1
59291.53	9941	3.0	< 0.13	4604010102	<i>NICER</i>	$P_{\text{X, drop}}$	1
59292.21	6394	3.0	< 0.14	4604010103	<i>NICER</i>	$P_{\text{X, drop}}$	1
59298.15	4387	3.0	< 0.18	4604010201	<i>NICER</i>	$P_{\text{X, drop}}$	1
59300.20	10040	99^{+120}_{-40}	$0.03^{+0.06}_{-0.02}$	0862770201	<i>XMM-Newton</i>	$P_{\text{X, drop}}$	1
59305.09	2735	3.0	< 0.20	4604010301	<i>NICER</i>	$P_{\text{X, faint}}$	1
59320.20	3254	3.0	< 0.28	00014135002	<i>Swift</i>	$P_{\text{X, faint}}$	1
59322.59	1808	3.0	< 0.30	4604010501	<i>NICER</i>	$P_{\text{X, faint}}$	1
59323.49	4525	3.0	< 0.21	4604010502	<i>NICER</i>	$P_{\text{X, faint}}$	1
59325.27	230	3.0	< 0.35	4604010504	<i>NICER</i>	$P_{\text{X, faint}}$	1
59328.31	420	3.0	< 0.24	4604010507	<i>NICER</i>	$P_{\text{X, faint}}$	1
59329.73	3342	3.0	< 0.24	00014135003	<i>Swift</i>	$P_{\text{X, faint}}$	1
59340.45	1402	3.0	< 0.54	00014135004	<i>Swift</i>	$P_{\text{X, faint}}$	1
59391.16	7669	78	$0.18^{+0.18}_{-0.11}$	00014135005 ^a	<i>Swift</i>	$P_{\text{X, rise}}$	2
59399.00	6406	$4.3^{+1.3}_{-1.1}$	$0.47^{+0.70}_{-0.27}$	00014135006 ^a	<i>Swift</i>	$P_{\text{X, rise}}$	2
59405.13	1793	$5.1^{+1.9}_{-1.6}$	$1.65^{+4.34}_{-1.14}$	00014135007 ^a	<i>Swift</i>	$P_{\text{X, rise}}$	2
59413.03	1641	$2.6^{+0.7}_{-0.7}$	$0.68^{+0.53}_{-0.29}$	00014135008 ^a	<i>Swift</i>	$P_{\text{X, rise}}$	2
59422.51	4304	$3.5^{+0.1}_{-0.1}$	$2.45^{+0.21}_{-0.16}$	4595020102 ^{a,b}	<i>NICER</i>	$P_{\text{X, rise}}$	2
59423.35	2589	$3.5^{+0.1}_{-0.1}$	$2.45^{+0.21}_{-0.16}$	4595020103 ^{a,b}	<i>NICER</i>	$P_{\text{X, rise}}$	2
59427.10	1631	$2.9^{+0.6}_{-0.5}$	$1.21^{+0.74}_{-0.45}$	00014135009 ^a	<i>Swift</i>	$P_{\text{X, rise}}$	2
59428.95	788	$3.6^{+0.2}_{-0.5}$	$3.05^{+0.84}_{-0.91}$	4595020105 ^a	<i>NICER</i>	$P_{\text{X, rise}}$	2
59432.96	764	$3.7^{+0.3}_{-0.2}$	$3.37^{+1.00}_{-0.64}$	4595020107 ^{a,b}	<i>NICER</i>	$P_{\text{X, rise}}$	2
59433.12	999	$3.7^{+0.3}_{-0.2}$	$3.37^{+1.00}_{-0.64}$	4595020108 ^{a,b}	<i>NICER</i>	$P_{\text{X, rise}}$	2
59434.71	1968	$3.5^{+0.5}_{-0.5}$	$3.07^{+1.45}_{-0.96}$	00014135010 ^a	<i>Swift</i>	$P_{\text{X, rise}}$	2
59441.95	514	$2.9^{+0.1}_{-0.1}$	$4.55^{+0.28}_{-0.32}$	4595020109 ^{a,b}	<i>NICER</i>	$P_{\text{X, rise}}$	2
59442.05	224	$2.9^{+0.1}_{-0.1}$	$4.55^{+0.28}_{-0.32}$	4595020110 ^{a,b}	<i>NICER</i>	$P_{\text{X, rise}}$	2
59445.50	2121	$3.2^{+0.1}_{-0.1}$	$6.15^{+0.19}_{-0.18}$	4595020111 ^a	<i>NICER</i>	$P_{\text{X, rise}}$	2
59447.51	40200	—	$4.79^{+1.10}_{-0.90}$	0891801101	<i>XMM-Newton</i>	$P_{\text{X, plat}}$	2
59448.38	1179	$3.2^{+0.1}_{-0.1}$	$5.06^{+0.23}_{-0.21}$	4595020112	<i>NICER</i>	$P_{\text{X, plat}}$	2
59450.80	3350	$2.9^{+0.0}_{-0.0}$	$4.48^{+0.13}_{-0.13}$	4595020113	<i>NICER</i>	$P_{\text{X, plat}}$	2
59453.89	2954	$2.8^{+0.2}_{-0.2}$	$3.20^{+0.72}_{-0.59}$	00014135011	<i>Swift</i>	$P_{\text{X, plat}}$	2
59460.31	345	$3.4^{+0.2}_{-0.2}$	$5.26^{+0.76}_{-0.67}$	eRASS4	eROSITA	$P_{\text{X, plat}}$	2
59467.45	1568	$2.8^{+0.3}_{-0.3}$	$2.39^{+0.42}_{-0.29}$	4604010901	<i>NICER</i>	$P_{\text{X, plat}}$	2
59468.45	445	$2.9^{+0.9}_{-0.9}$	$1.73^{+2.05}_{-0.91}$	00014135012	<i>Swift</i>	$P_{\text{X, plat}}$	2
59470.50	341	$4.1^{+1.1}_{-0.9}$	$1.67^{+1.21}_{-0.61}$	4604010902	<i>NICER</i>	$P_{\text{X, plat}}$	2
59472.51	2542	$2.6^{+0.4}_{-0.4}$	$1.71^{+0.61}_{-0.44}$	00014135013	<i>Swift</i>	$P_{\text{X, plat}}$	2
59476.22	1560	$2.9^{+0.4}_{-0.4}$	$1.23^{+0.24}_{-0.17}$	4604010903	<i>NICER</i>	$P_{\text{X, plat}}$	2
59479.33	929	$3.0^{+0.3}_{-0.3}$	$2.81^{+0.49}_{-0.35}$	4604010904	<i>NICER</i>	$P_{\text{X, plat}}$	2
59481.30	85960	—	$2.40^{+0.76}_{-0.36}$	0891801701	<i>XMM-Newton</i>	$P_{\text{X, plat}}$	2
59481.49	2490	$2.7^{+0.4}_{-0.4}$	$1.48^{+0.58}_{-0.41}$	00014135014	<i>Swift</i>	$P_{\text{X, plat}}$	2
59482.46	4637	$2.9^{+0.3}_{-0.3}$	$2.33^{+0.37}_{-0.26}$	4604010905	<i>NICER</i>	$P_{\text{X, plat}}$	2
59485.04	1183	$2.7^{+0.3}_{-0.3}$	$2.03^{+0.31}_{-0.23}$	4604010906	<i>NICER</i>	$P_{\text{X, plat}}$	2

Table C.2. continued.

MJD	T_{exp}	T_{in}/Γ	$f_{\text{X, soft}}$	ObsID	Mission	X-ray phase	cycle
59488.08	1532	$3.0^{+0.3}_{-0.3}$	$2.78^{+0.57}_{-0.38}$	4604010907	NICER	$P_{\text{X, plat}}$	2
59491.05	1410	$2.7^{+0.3}_{-0.3}$	$2.94^{+0.49}_{-0.34}$	4604010908	NICER	$P_{\text{X, plat}}$	2
59494.25	811	$2.5^{+0.3}_{-0.3}$	$2.34^{+0.31}_{-0.24}$	4604010909	NICER	$P_{\text{X, plat}}$	2
59496.67	3079	$2.7^{+0.3}_{-0.3}$	$2.05^{+0.64}_{-0.49}$	00014135016	Swift	$P_{\text{X, plat}}$	2
59497.25	1133	$2.9^{+0.3}_{-0.3}$	$2.63^{+0.44}_{-0.31}$	4604010910	NICER	$P_{\text{X, plat}}$	2
59499.80	1703	$2.5^{+0.3}_{-0.3}$	$2.19^{+0.31}_{-0.24}$	4604010911	NICER	$P_{\text{X, plat}}$	2
59500.64	3647	$2.9^{+0.3}_{-0.3}$	$2.47^{+0.41}_{-0.28}$	4604010912	NICER	$P_{\text{X, plat}}$	2
59501.35	10186	$2.9^{+0.2}_{-0.2}$	$2.13^{+0.31}_{-0.22}$	4604010913	NICER	$P_{\text{X, plat}}$	2
59502.49	7885	$2.7^{+0.3}_{-0.3}$	$1.96^{+0.24}_{-0.18}$	4604010914	NICER	$P_{\text{X, plat}}$	2
59503.48	7906	$2.9^{+0.2}_{-0.2}$	$2.48^{+0.34}_{-0.24}$	4604010915	NICER	$P_{\text{X, plat}}$	2
59504.51	4370	$2.8^{+0.3}_{-0.3}$	$2.23^{+0.35}_{-0.24}$	4604010916	NICER	$P_{\text{X, plat}}$	2
59505.52	3600	$2.7^{+0.3}_{-0.3}$	$2.36^{+0.35}_{-0.25}$	4604010917	NICER	$P_{\text{X, plat}}$	2
59506.22	826	$2.8^{+0.3}_{-0.3}$	$2.41^{+0.40}_{-0.29}$	4604010918	NICER	$P_{\text{X, plat}}$	2
59508.15	553	$3.3^{+0.5}_{-0.5}$	$1.95^{+0.60}_{-0.39}$	4604010920	NICER	$P_{\text{X, plat}}$	2
59510.21	3079	$2.8^{+0.3}_{-0.3}$	$2.31^{+0.38}_{-0.26}$	4604010921	NICER	$P_{\text{X, plat}}$	2
59510.83	2777	$2.3^{+0.3}_{-0.3}$	$1.71^{+0.51}_{-0.39}$	00014135017	Swift	$P_{\text{X, plat}}$	2
59511.91	2492	$2.9^{+0.3}_{-0.3}$	$1.91^{+0.27}_{-0.20}$	4604010922	NICER	$P_{\text{X, plat}}$	2
59517.60	2745	3.0	< 0.15	4604011001	NICER	$P_{\text{X, drop}}$	2
59520.47	3000	3.0	< 0.22	4604011002	NICER	$P_{\text{X, faint}}$	2
59523.54	1200	3.0	< 0.27	4604011003	NICER	$P_{\text{X, faint}}$	2
59524.53	1371	3.0	< 1.50	00014135018	Swift	$P_{\text{X, faint}}$	2
59526.63	936	3.0	< 0.29	4604011004	NICER	$P_{\text{X, faint}}$	2
59527.63	3924	3.0	< 0.24	00014135019	Swift	$P_{\text{X, faint}}$	2
59529.83	636	3.0	< 0.30	4604011005	NICER	$P_{\text{X, faint}}$	2
59529.87	1402	3.0	< 0.69	00014135021	Swift	$P_{\text{X, faint}}$	2
59532.54	1143	3.0	< 0.29	4604011006	NICER	$P_{\text{X, faint}}$	2
59535.32	1817	3.0	< 0.28	4604011007	NICER	$P_{\text{X, faint}}$	2
59538.23	2041	3.0	< 0.19	4604011008	NICER	$P_{\text{X, faint}}$	2
59541.33	1884	3.0	< 0.14	4604011009	NICER	$P_{\text{X, faint}}$	2
59543.75	1996	3.0	< 0.39	00014135022	Swift	$P_{\text{X, faint}}$	2
59557.41	2372	3.0	< 0.41	00014135023	Swift	$P_{\text{X, faint}}$	2
59562.50	193	3.0	< 3.60	00014135024	Swift	$P_{\text{X, faint}}$	2
59566.74	614	3.0	< 1.60	00014135025	Swift	$P_{\text{X, faint}}$	2
59572.58	2635	3.0	< 0.38	00014135026	Swift	$P_{\text{X, faint}}$	2
59584.90	2886	3.0	< 0.39	00014135027	Swift	$P_{\text{X, faint}}$	2
59601.40	819	180	< 0.27	4595020114	NICER	$P_{\text{X, rise}}$	3
59602.56	3132	180	< 0.05	4595020115 ^a	NICER	$P_{\text{X, rise}}$	3
59603.21	1684	180	< 0.11	4595020116	NICER	$P_{\text{X, rise}}$	3
59604.76	432	120	< 0.21	4595020117	NICER	$P_{\text{X, rise}}$	3
59605.47	425	120	< 0.37	4595020118	NICER	$P_{\text{X, rise}}$	3
59607.27	765	120	< 0.19	4595020119	NICER	$P_{\text{X, rise}}$	3
59608.60	2918	120	< 0.08	4595020120	NICER	$P_{\text{X, rise}}$	3
59609.72	1146	80	< 0.23	4595020121	NICER	$P_{\text{X, rise}}$	3
59610.47	2152	80	< 0.13	4595020122	NICER	$P_{\text{X, rise}}$	3
59611.79	754	80	< 0.29	4595020123	NICER	$P_{\text{X, rise}}$	3
59612.47	758	80	< 0.08	4595020124 ^a	NICER	$P_{\text{X, rise}}$	3

Table C.2. continued.

MJD	T_{exp}	T_{in}/Γ	$f_{\text{X, soft}}$	ObsID	Mission	X-ray phase	cycle
59613.37	1443	80	< 0.19	4595020125	NICER	$P_{\text{X, rise}}$	3
59619.47	5808	78^{+24}_{-18}	$0.23^{+0.12}_{-0.05}$	4595020126 ^a	NICER	$P_{\text{X, rise}}$	3
59625.99	787	$3.5^{+0.3}_{-0.2}$	$0.67^{+0.11}_{-0.09}$	4595020127 ^{a,b}	NICER	$P_{\text{X, rise}}$	3
59626.06	1584	$3.5^{+0.3}_{-0.2}$	$0.67^{+0.11}_{-0.09}$	4595020128 ^{a,b}	NICER	$P_{\text{X, rise}}$	3
59633.19	3669	$3.6^{+0.2}_{-0.2}$	$1.11^{+0.11}_{-0.11}$	4595020129 ^a	NICER	$P_{\text{X, rise}}$	3
59635.13	10129	$3.2^{+0.3}_{-0.3}$	$0.77^{+0.27}_{-0.20}$	00014135099 ^a	Swift	$P_{\text{X, rise}}$	3
59640.03	3707	$3.1^{+0.1}_{-0.1}$	$1.43^{+0.10}_{-0.10}$	4604010104 ^a	NICER	$P_{\text{X, rise}}$	3
59640.03	3707	$3.1^{+0.1}_{-0.1}$	$1.43^{+0.10}_{-0.10}$	4604010105 ^a	NICER	$P_{\text{X, rise}}$	3
59642.13	4069	$3.2^{+0.1}_{-0.1}$	$1.40^{+0.08}_{-0.13}$	4604010106	NICER	$P_{\text{X, plat}}$	3
59643.68	2485	$3.2^{+0.5}_{-0.5}$	$1.78^{+0.88}_{-0.58}$	00014135033	Swift	$P_{\text{X, plat}}$	3
59645.48	2460	$3.2^{+0.3}_{-0.3}$	$1.71^{+0.38}_{-0.26}$	4604010107	NICER	$P_{\text{X, plat}}$	3
59648.20	1991	$3.2^{+0.4}_{-0.4}$	$1.54^{+0.36}_{-0.24}$	4604010108	NICER	$P_{\text{X, plat}}$	3
59650.19	2977	$3.2^{+0.5}_{-0.5}$	$1.58^{+0.88}_{-0.56}$	00014135034	Swift	$P_{\text{X, plat}}$	3
59651.90	668	$2.6^{+0.6}_{-0.6}$	$1.39^{+0.35}_{-0.24}$	4604010109	NICER	$P_{\text{X, plat}}$	3
59652.06	720	$3.6^{+0.6}_{-0.5}$	$2.12^{+0.91}_{-0.52}$	4604010110	NICER	$P_{\text{X, plat}}$	3
59654.83	1787	$3.7^{+0.4}_{-0.4}$	$1.83^{+0.59}_{-0.37}$	4604010111	NICER	$P_{\text{X, plat}}$	3
59656.16	2665	$3.0^{+0.4}_{-0.4}$	$1.48^{+0.68}_{-0.47}$	00014135036	Swift	$P_{\text{X, plat}}$	3
59657.15	—	—	$1.92^{+0.04}_{-0.04}$	0884960601	XMM-Newton	$P_{\text{X, plat}}$	3
59663.82	3172	$2.8^{+0.4}_{-0.4}$	$1.52^{+0.58}_{-0.42}$	00014135037	Swift	$P_{\text{X, plat}}$	3
59670.56	3127	$2.5^{+0.4}_{-0.4}$	$1.22^{+0.44}_{-0.32}$	00014135038	Swift	$P_{\text{X, plat}}$	3
59678.08	4305	$2.8^{+0.5}_{-0.4}$	$0.68^{+0.34}_{-0.22}$	00014135039	Swift	$P_{\text{X, plat}}$	3
59684.37	2922	$2.6^{+0.5}_{-0.5}$	$0.88^{+0.44}_{-0.29}$	00014135040	Swift	$P_{\text{X, plat}}$	3
59691.98	6391	$3.1^{+0.4}_{-0.3}$	$1.08^{+0.39}_{-0.28}$	00014135041	Swift	$P_{\text{X, plat}}$	3
59698.54	2627	$3.5^{+0.8}_{-0.8}$	$1.18^{+1.06}_{-0.56}$	00014135042	Swift	$P_{\text{X, plat}}$	3
59705.30	3014	$3.0^{+3.0}_{-3.0}$	$0.12^{+0.13}_{-0.08}$	00014135043	Swift	$P_{\text{X, drop}}$	3
59752.82	1459	3.0	< 0.50	00014135044	Swift	$P_{\text{X, faint}}$	3
59756.64	2618	3.0	< 0.28	00014135045	Swift	$P_{\text{X, faint}}$	3
59759.19	3092	3.0	< 0.25	00014135046	Swift	$P_{\text{X, faint}}$	3
59766.09	2668	3.0	< 0.31	00014135047	Swift	$P_{\text{X, faint}}$	3
59773.49	2680	3.0	< 0.43	00014135048	Swift	$P_{\text{X, faint}}$	3
59780.34	3377	3.0	< 0.25	00014135049	Swift	$P_{\text{X, rise}}$	4
59787.41	2976	3.0	< 0.40	00014135050	Swift	$P_{\text{X, rise}}$	4
59794.63	2720	3.0	< 0.51	00014135051	Swift	$P_{\text{X, rise}}$	4
59801.23	4023	$3.1^{+2.2}_{-2.2}$	$0.12^{+0.46}_{-0.09}$	00014135052 ^a	Swift	$P_{\text{X, rise}}$	4
59806.58	2627	$3.0^{+102.0}_{-102.0}$	< 0.15	5202950108 ^a	NICER	$P_{\text{X, rise}}$	4
59811.17	187	$3.5^{+1.3}_{-0.9}$	$0.77^{+0.41}_{-0.39}$	5202950109 ^a	NICER	$P_{\text{X, rise}}$	4
59811.48	3179	$2.3^{+0.9}_{-0.9}$	$0.24^{+0.24}_{-0.12}$	00014135053 ^a	Swift	$P_{\text{X, rise}}$	4
59813.97	366	$3.4^{+0.8}_{-0.7}$	$0.55^{+0.27}_{-0.24}$	5202950110 ^a	NICER	$P_{\text{X, rise}}$	4
59814.03	256	$2.8^{+0.7}_{-0.6}$	$0.53^{+0.23}_{-0.18}$	5202950111 ^a	NICER	$P_{\text{X, rise}}$	4
59814.12	9662	$3.17^{+0.06}_{-0.06}$	$0.70^{+0.03}_{-0.03}$	0884962601 ^a	XMM-Newton	$P_{\text{X, rise}}$	4
59819.86	2570	$2.4^{+0.7}_{-0.6}$	$0.43^{+0.33}_{-0.19}$	00014135455	Swift	$P_{\text{X, plat}}$	4
59825.17	3384	$2.7^{+0.7}_{-0.7}$	$0.38^{+0.33}_{-0.18}$	00014135056	Swift	$P_{\text{X, plat}}$	4
59828.19	3303	$4.0^{+0.4}_{-0.3}$	$0.78^{+0.17}_{-0.10}$	5202950114	NICER	$P_{\text{X, plat}}$	4
59832.46	3117	$2.7^{+0.5}_{-0.5}$	$0.68^{+0.38}_{-0.24}$	00014135057	Swift	$P_{\text{X, plat}}$	4
59839.22	2647	$2.9^{+0.7}_{-0.7}$	$0.58^{+0.49}_{-0.26}$	00014135058	Swift	$P_{\text{X, plat}}$	4
59839.53	2717	$3.0^{+0.2}_{-0.2}$	$0.63^{+0.07}_{-0.07}$	5202950115	NICER	$P_{\text{X, plat}}$	4
59842.32	1380	$4.4^{+1.8}_{-1.0}$	$0.64^{+0.42}_{-0.25}$	5202950116	NICER	$P_{\text{X, plat}}$	4
59845.39	1529	$3.6^{+0.5}_{-0.5}$	$0.62^{+0.14}_{-0.18}$	5202950117	NICER	$P_{\text{X, plat}}$	4
59846.51	2605	$3.4^{+1.2}_{-1.2}$	$0.56^{+0.82}_{-0.31}$	00014135059	Swift	$P_{\text{X, plat}}$	4

Table C.2. continued.

MJD	T_{exp}	T_{in}/Γ	$f_{X, \text{soft}}$	ObsID	Mission	X-ray phase	cycle
59847.94	841	$3.1^{+0.6}_{-0.5}$	$0.57^{+0.19}_{-0.18}$	5202950118	<i>NICER</i>	$P_{X, \text{plat}}$	4
59848.10	2940	$2.8^{+0.3}_{-0.3}$	$0.65^{+0.09}_{-0.20}$	5202950119	<i>NICER</i>	$P_{X, \text{plat}}$	4
59851.44	1555	$3.8^{+0.4}_{-0.4}$	$0.81^{+0.20}_{-0.15}$	5202950120	<i>NICER</i>	$P_{X, \text{plat}}$	4
59852.96	341	3.0	< 0.73	5202950121	<i>NICER</i>	$P_{X, \text{plat}}$	4
59853.86	2640	$3.3^{+0.9}_{-0.8}$	$0.67^{+0.77}_{-0.35}$	00014135060	<i>Swift</i>	$P_{X, \text{plat}}$	4
59857.19	2144	$3.7^{+0.5}_{-0.3}$	$0.75^{+0.20}_{-0.13}$	5202950123	<i>NICER</i>	$P_{X, \text{plat}}$	4
59860.20	1766	$3.8^{+0.5}_{-0.3}$	$0.71^{+0.19}_{-0.12}$	5202950124	<i>NICER</i>	$P_{X, \text{plat}}$	4
59860.82	2555	$3.4^{+0.8}_{-0.7}$	$0.82^{+0.79}_{-0.39}$	00014135061	<i>Swift</i>	$P_{X, \text{plat}}$	4
59863.58	4048	$3.3^{+0.2}_{-0.3}$	$0.57^{+0.06}_{-0.10}$	5202950125	<i>NICER</i>	$P_{X, \text{plat}}$	4
59867.30	2122	$3.5^{+0.8}_{-0.5}$	$0.57^{+0.10}_{-0.17}$	5202950127	<i>NICER</i>	$P_{X, \text{plat}}$	4
59869.51	977	$4.1^{+0.6}_{-0.5}$	$0.83^{+0.29}_{-0.20}$	5202950128	<i>NICER</i>	$P_{X, \text{plat}}$	4
59872.21	392	3.0	< 0.56	5202950129	<i>NICER</i>	$P_{X, \text{plat}}$	4
59874.88	2650	$2.8^{+0.8}_{-0.7}$	$0.42^{+0.39}_{-0.20}$	00014135062	<i>Swift</i>	$P_{X, \text{plat}}$	4
59874.91	2416	$2.6^{+0.3}_{-0.3}$	$0.65^{+0.17}_{-0.11}$	5202950130	<i>NICER</i>	$P_{X, \text{plat}}$	4
59875.49	316	3.0	< 0.33	5202950131	<i>NICER</i>	$P_{X, \text{plat}}$	4
59875.49	1211	$3.4^{+1.4}_{-1.0}$	$0.24^{+0.15}_{-0.15}$	5202950131	<i>NICER</i>	$P_{X, \text{plat}}$	4
59876.52	1326	$3.9^{+0.8}_{-0.6}$	$0.44^{+0.23}_{-0.12}$	5202950132	<i>NICER</i>	$P_{X, \text{plat}}$	4
59876.52	459	$3.7^{+1.2}_{-0.9}$	$0.49^{+0.29}_{-0.18}$	5202950132	<i>NICER</i>	$P_{X, \text{plat}}$	4
59877.30	2150	$3.0^{+0.3}_{-0.2}$	$0.47^{+0.08}_{-0.07}$	5202950133	<i>NICER</i>	$P_{X, \text{plat}}$	4
59877.30	1266	$3.1^{+0.5}_{-0.4}$	$0.53^{+0.13}_{-0.10}$	5202950133	<i>NICER</i>	$P_{X, \text{plat}}$	4
59878.36	1955	$4.3^{+0.6}_{-0.5}$	$0.49^{+0.17}_{-0.12}$	5202950134	<i>NICER</i>	$P_{X, \text{drop}}$	4
59879.59	3164	3.0	< 0.55	5202950135	<i>NICER</i>	$P_{X, \text{drop}}$	4
59879.59	1564	$4.1^{+0.7}_{-0.6}$	$0.43^{+0.16}_{-0.12}$	5202950135	<i>NICER</i>	$P_{X, \text{drop}}$	4
59881.55	1119	$2.3^{+0.7}_{-0.7}$	$0.33^{+0.08}_{-0.07}$	5202950136	<i>NICER</i>	$P_{X, \text{drop}}$	4
59881.55	3311	$1.4^{+0.6}_{-1.4}$	$0.17^{+0.06}_{-0.09}$	5202950136	<i>NICER</i>	$P_{X, \text{drop}}$	4
59882.80	8366	$3.0^{+3.0}_{-3.0}$	$0.07^{+0.06}_{-0.04}$	14136364	<i>Swift</i>	$P_{X, \text{drop}}$	4
59884.59	3046	$3.0^{+102.0}_{-102.0}$	< 0.11	5202950137	<i>NICER</i>	$P_{X, \text{drop}}$	4
59884.59	2552	3.0	< 0.14	5202950137	<i>NICER</i>	$P_{X, \text{drop}}$	4
59887.94	2868	3.0	< 0.36	00014135065	<i>Swift</i>	$P_{X, \text{faint}}$	4
59895.56	2688	3.0	< 0.35	00014135066	<i>Swift</i>	$P_{X, \text{faint}}$	4
59920.62	3455	3.0	< 0.31	00014135067	<i>Swift</i>	$P_{X, \text{faint}}$	4
59941.75	4054	3.0	< 0.32	00014135068	<i>Swift</i>	$P_{X, \text{faint}}$	4
59962.62	3984	3.0	< 0.23	00014135069	<i>Swift</i>	$P_{X, \text{faint}}$	4
59980.96	2963	200	< 0.25	00014135070	<i>Swift</i>	$P_{X, \text{rise}}$	5
59985.53	15381	193^{+43}_{-25}	$0.021^{+0.005}_{-0.003}$	0915390401 ^a	<i>XMM-Newton</i>	$P_{X, \text{rise}}$	5
59990.59	2926	100	< 0.67	00014135071	<i>Swift</i>	$P_{X, \text{rise}}$	5
59999.79	3384	$3.4^{+2.4}_{-2.3}$	$0.26^{+0.89}_{-0.17}$	00014135072	<i>Swift</i>	$P_{X, \text{rise}}$	5
60007.25	11300	$3.06^{+0.07}_{-0.07}$	$0.44^{+0.03}_{-0.02}$	0915390501 ^a	<i>XMM-Newton</i>	$P_{X, \text{rise}}$	5
60009.45	2690	$3.2^{+1.3}_{-1.3}$	$0.53^{+0.75}_{-0.27}$	00014135073	<i>Swift</i>	$P_{X, \text{rise}}$	5
60021.39	3189	$2.2^{+0.9}_{-0.9}$	$0.27^{+0.25}_{-0.13}$	00014135074	<i>Swift</i>	$P_{X, \text{plat}}$	5
60023.00	9948	$2.6^{+0.4}_{-0.4}$	$0.29^{+0.24}_{-0.12}$	27737	<i>Chandra</i>	$P_{X, \text{plat}}$	5
60031.16	2680	$3.2^{+0.8}_{-0.8}$	$0.63^{+0.58}_{-0.30}$	00014135075	<i>Swift</i>	$P_{X, \text{plat}}$	5
60045.09	10059	$2.6^{+0.5}_{-0.5}$	$0.25^{+0.27}_{-0.12}$	27738	<i>Chandra</i>	$P_{X, \text{plat}}$	5
60048.22	9948	$2.5^{+0.5}_{-0.5}$	$0.19^{+0.20}_{-0.09}$	27798	<i>Chandra</i>	$P_{X, \text{plat}}$	5
60072.18	4795	$3.0^{+0.9}_{-0.8}$	$0.28^{+0.32}_{-0.15}$	00014135076	<i>Swift</i>	$P_{X, \text{plat}}$	5

Notes. *MJD* is the mid-date of the coverage for each observation; T_{exp} is the effective exposure time in units of seconds. Exposure for *XMM-Newton* ObsID 0862770201 is calculated from combined MOS data, while the pn exposures are given for the other *XMM-Newton* observations; T_{in}/Γ : the inner temperature of a multi-colour disk or the photon index of the power law. A value without an uncertainty means the parameter is fixed at the given value during spectral fitting; $f_{X, \text{soft}}$ is the rest frame intrinsic 0.2 – 2.0 keV flux in units of $10^{-12} \text{ erg cm}^{-2} \text{ s}^{-1}$. The 3σ upper limits are given for observations in which the J0456–20 is not detected; *ObsID* is the observation ID for each observation; *Mission* refers to the telescopes used to draw the data; *X-ray phase* marks the phases of the J0456–20 during the observations; *Cycle* indicates the particular cycle of the X-ray flare when the data were taken. Quoted uncertainties are at the 90% confidence level. Upper limits are reported at 3σ . a: observations used in modelling the profile of the $P_{X, \text{rise}}$ phase. b: the X-ray spectral fitting results were from jointly fitting of the two consecutive observations.